# Astounding Wonders of Ancient Indian Vedic Mathematics 

## Satish V. Malik

wuwu.cems.uwe.ac.uk/~svmalik

## What are we going to do today?

We shall learn to carry out difficult arithmetic operations such as:

Multiplication:
Multiply 87265 by 32117.


Reciprocals:
Express 1/19 up to certain number of decimal places.

Division:
Divide 7031985 by 823.


Find Square roots and Cube roots:
Extract square root of 738915489 .
Find cube root of 9989.
EACH OF THESE IN MATTER OF SECONDS!!!

## Multiplication

## Lets start with an easy examplleo



Multiply 23 by 21

21
$4: 2+6: 3$
$=483$

$\bullet$
$\rightarrow$ Multiply the left-hand-most digit 2 of the multiplicand vertically by the left-handmost digit 2 of the multiplier, get their product 4 and set it down as the left-hand-most part of the answer.
$\rightarrow$ Then multiply 2 and 1 , and 2 and 3 crosswise, add the two, get 8 as the sum and set it down as the middle part of the answer.
$\rightarrow$ Multiply 3 and 1 vertically, get 3 as their product and put it down as the last, the right-hand-most, part of the answer.

Activity:
Multiply 16 by 11.


## Multiplication



Multiply 37 by 33

37
33

901
32
1221

Activity:
Multiply 35 by 36 .
-Multiply the left-hand-most digit 3 of the multiplicand vertically by the left-handmost digit 3 of the multiplier, get their product 9 and set it down as the left-hand-most part of the answer.
$\cdot$ Then multiply 3 and 3 , and 7 and 3 crosswise, add the two to get 30 as the sum.
-The right-hand-most digit is to be put down there and the preceding i.e. left-hand-side digit or digits should be carried over to the left and placed under the previous digit or digits of the upper row.
-Multiply 7 and 3 vertically, get 21 as their product and follow the previous step.
-Add the numbers in the two rows thus obtained to get the required product.

## Multiplication

Lets talke a step forward:


Activity
Multiply 621 by 547.
Multiply 795 by 362.


This merely means that we are multiplying
$\left(a x^{2}+b x+c\right) b y\left(d x^{2}+e x+f\right)$
(where $x=10)$.
Let us try to multiply this!

$$
\begin{aligned}
& \mathbf{a x}^{2}+\mathbf{b x}+\mathbf{c} \\
& \mathbf{d} \mathbf{x}^{2}+\mathbf{e x}+\mathbf{f}
\end{aligned}
$$

$\mathbf{a d x} \mathbf{x}^{4}+(\mathbf{a e}+\mathbf{b d}) \mathbf{x}^{3}$
$+($ af + be $+c d) \mathbf{x}^{2}$
$+(b f+c e) x+c f$

## Reciprocal

Find the reciprocals of 19,29 and 49 by division of 1 by 19, 29 and 49.


$$
\text { 1/19 = o. o 5 } 2631578947368421
$$

1/29
= o.0344827586206896551724137931

1/49
= 0.02040816326530612244897959183673 4693877551

## Reciprocal

We shall now find reciprocal of 19 by using a formula from vedic mathematics.
$1 / 19=$
$\begin{array}{llllllllll}\text { O. } & 0 & 5 & 2 & 6 & 3 & 1 & 5 & 7 & 8\end{array}$

| 1 | 1 |  |  |  | 1 | 1 | 1 | 1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $\mathbf{1}$ | $\mathbf{4}$ | 7 | $\mathbf{3}$ | $\mathbf{6}$ | $\mathbf{8}$ | $\mathbf{4}$ | $\mathbf{2}$ | $\mathbf{1}$ |

$1 \quad 1 \quad 1$

Activity:
Find 1/29 and 1/49.

- Put down 1 as the right-hand most digit
- Multiply the last digit 1 by 2 and put the 2 down as the immediately preceding digit.
- Multiply that 2 by 2 and put 4 down as the next previous digit.
- Multiply that 4 by 2 and put 8 down as the next digit.
- Multiply that 8 by 2 and we get 16. Put 6 immediately to the left of the 8 and keep the 1 on hand to be carried forward over to the left at the next step.
- We continue this until we reach the $18^{\text {th }}$ digit counting leftwards from the right.

