

D3/D7-brane inflation revisited

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Work in progress with R. Kallosh, A. Krause, A. Linde, D. Lüst, M. Zagermann
and hep-th/0404087, hep-th/0508043 (with M. Berg and B. Körs)

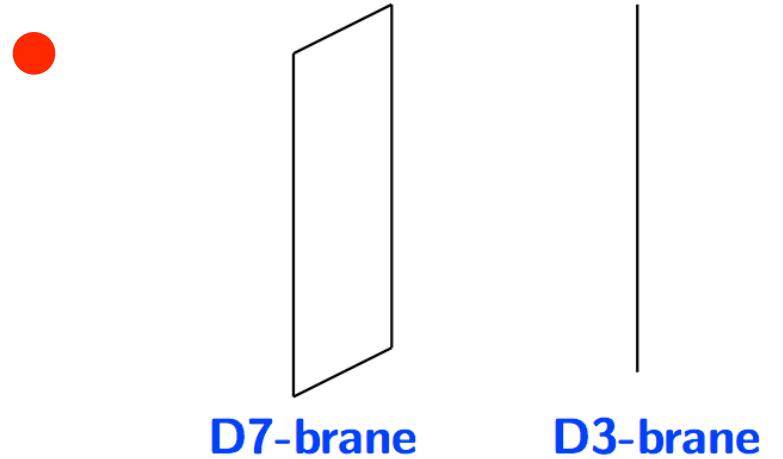
Motivation

- Important problem in string phenomenology:
Derive (semi)realistic, consistent and controllable
models for inflation in string theory
- Prime example: D3/D7 inflation
(relatively good control:
basic model has $\mathcal{N} = 2$ and
only mild warping)
[Dasgupta, Herdeiro,
Hirano, Kallosh]

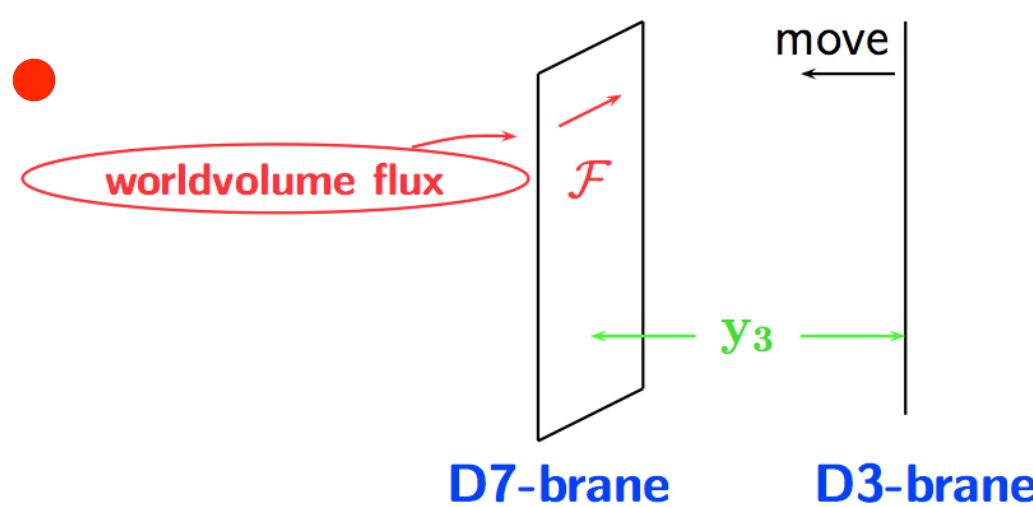
Overview

- Review of D3/D7 inflation
- Why should it be revisited?
- 1-loop corrections to Kähler potential and D7-brane gauge couplings in the D3/D7-system
- Insights for inflation
- Conclusion

D3/D7 inflation: Basic idea



If the branes are mutually BPS, there is no interbrane force



Non-selfdual worldvolume fluxes break supersymmetry and lead to a potential for y_3

A compactified example

[Dasgupta, Herdeiro, Hirano, Kallosh]

- Type IIB orientifold on $\mathbb{R}^{1,3} \times K3 \times T^2/\mathbb{Z}_2$
(T-dual to the models discussed by
[Antoniadis, Bachas, Fabre, Partouche, Taylor]
cf. also [Bianchi, Sagnotti; Gimon, Polchinski])
 $\Omega(-1)^{F_L} I_2$
- Leads to $\mathcal{N} = 2$ supergravity in 4D
- Local D3/D7-pair:

	$\mathbb{R}^{1,3}$	K3	T^2/\mathbb{Z}_2
D7	X	X	
D3	X		
\mathcal{F}		X	

Provide inflaton y_3
(= interbrane distance on T^2/\mathbb{Z}_2)
→ Fayet-Iliopoulos D-term

Masses of charged chiral multiplets

- The masses of D3/D7-states depend on position y_3 and \mathcal{F}

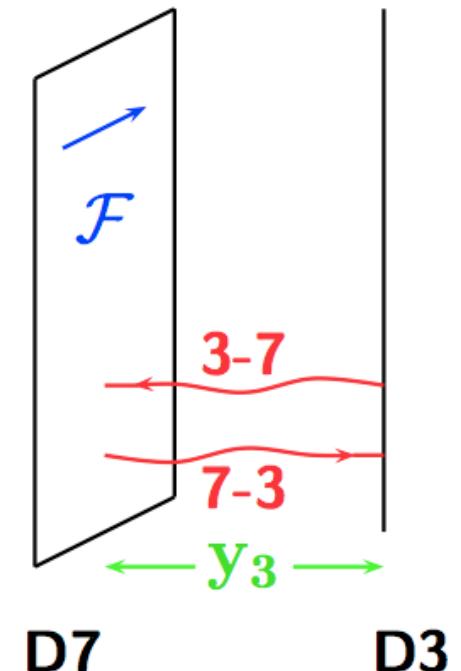
$$\arctan(\mathcal{F}_{45}) - \arctan(\mathcal{F}_{67})$$

- Scalars ϕ_{\pm} : $M_{\pm}^2 \sim |y_3|^2 \pm \xi(\mathcal{F})$

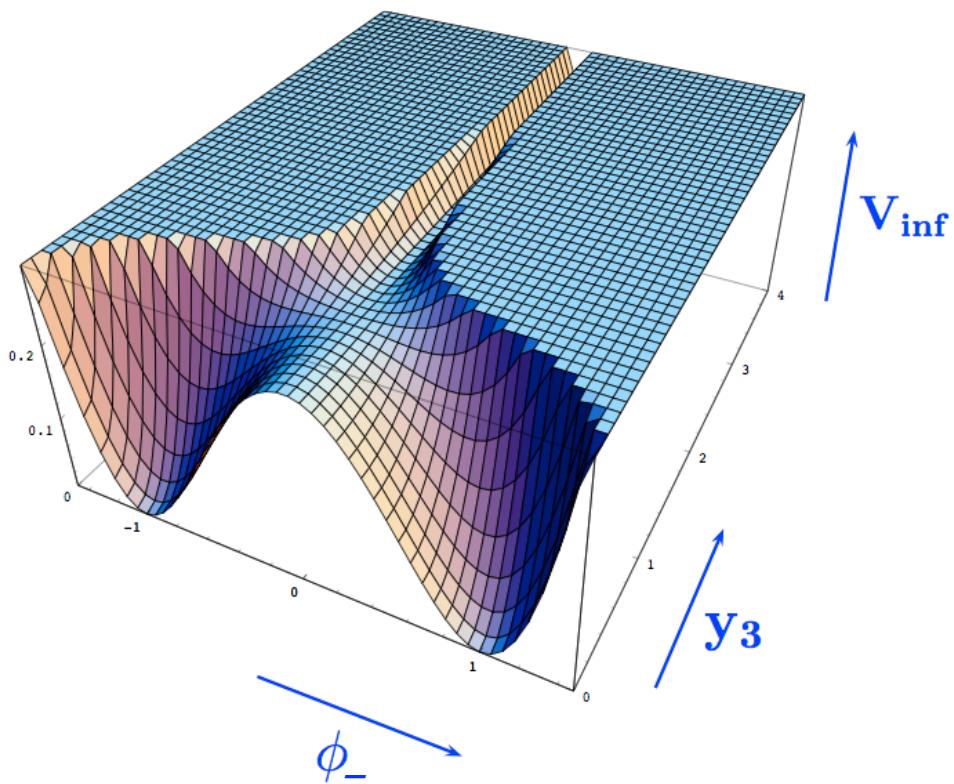
Fermions: $M^2 \sim |y_3|^2$

- For $|y_3| > |y_{3,c}| = \sqrt{|\xi(\mathcal{F})|}$
all scalars non-tachyonic

- For $|y_3| < |y_{3,c}|$ one scalar becomes tachyonic and condenses



Hybrid D-term inflation



- $|y_3| > |y_{3,c}| \Rightarrow \langle \phi_{\pm} \rangle = 0$

F.I.-term

- $V_{\text{infl}}|_{\phi_{\pm}=0} = \frac{1}{2}g^2\xi^2 \left(1 + \frac{g^2}{8\pi^2} \ln \frac{|y_3|^2}{|y_{3,c}|^2} \right)$

One-loop
gauge theory
effect

Some phenomenology

- Hybrid D-term inflation
⇒ A priori no supergravity “eta”-problem
- Condensation of ϕ_- spontaneously breaks $U(1)_D$
⇒ Cosmic string formation after inflation
- $G\mu, n_s$ depend on value of g (coupling of $U(1)_D$)
 - ★ $g \geq 2 \times 10^{-3} \Rightarrow n_s \cong 0.98, G\mu \cong 2.5 \times 10^{-6}$ (A)
 - ★ $g \ll 2 \times 10^{-3} \Rightarrow n_s \cong 1, G\mu \leq 10^{-7}$ (B)

[Kallosh, Linde]

Reasons to revisit D3/D7 inflation

- Taking into account stabilization of moduli (in particular of the volume) could change the story [cf. also McAllister]
(e.g.: what is the inflaton candidate?)
- Inflaton range was not carefully discussed in the literature until now

Moduli

- (Abelian) Vector multiplet scalars:

[Antoniadis, Bachas, Fabre, Partouche, Taylor; D'Auria, Ferrara, Trigiante]

$$y_3^i = y_{3,1}^i + U y_{3,2}^i , \quad y_7^r = y_{7,1}^r + U y_{7,2}^r$$

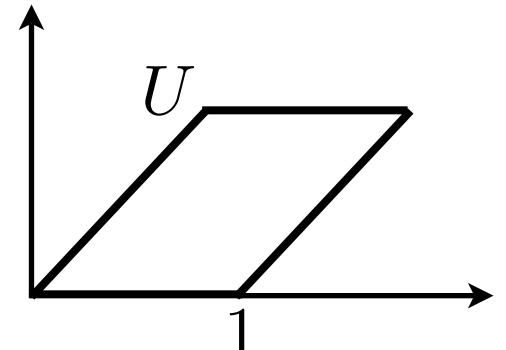
$$U = \frac{g_{12}}{g_{11}} + i \frac{\sqrt{\det g}}{g_{11}}$$

$$S = C_{(0)} - ie^{-\phi} + \frac{1}{2} \sum_r y_{7,2}^r y_7^r$$

$$T = C_{(4)} - i\mathcal{V}_{K3}^{(0)} + \frac{1}{2} \sum_i y_{3,2}^i y_3^i$$

Only depends on $\text{Im}(y_3)$!

$$\begin{aligned} K^{(0)} &= -\ln \left[(S - \bar{S})(T - \bar{T})(U - \bar{U}) \right. \\ &\quad \left. - \frac{1}{2}(S - \bar{S})(y_3 - \bar{y}_3)^2 - \frac{1}{2}(T - \bar{T})(y_7 - \bar{y}_7)^2 \right] \end{aligned}$$



Moduli stabilization

- Assume: 3-form Fluxes break supersymmetry to $\mathcal{N} = 1$
- Fluxes and non-perturbative effects (e.g. gaugino condensation on D7) lead to superpotential

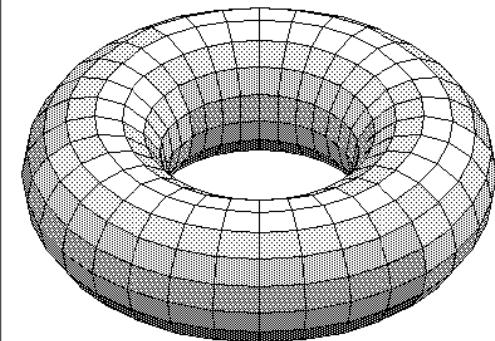
$$W = W_{\text{flux}} + W_{\text{np}}$$

$\sim e^{-af_{\text{D7}}}$ f_{D7} : D7 gauge kinetic function

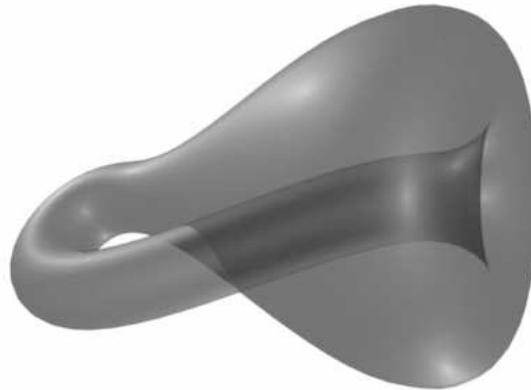
- At leading order: $f_{\text{D7}} = iT$ (independent of y_3)
 W_{flux} independent of y_3 , $K^{(0)}$ independent of $\text{Re}(y_3)$
 $\implies \text{Re}(y_3)$ good inflaton candidate?

- Two reasons to reconsider this point:
 - ★ g_s corrections could introduce y_3 dependence, leading higher order corrections from:

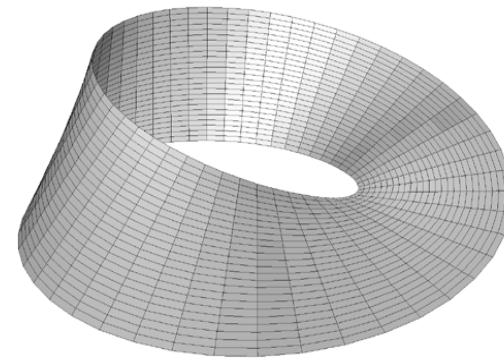
Torus:



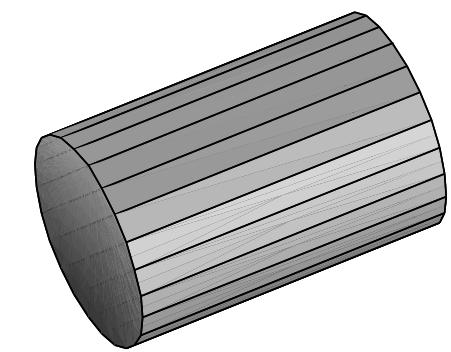
Klein bottle:



Möbius strip:



Annulus:



- ★ $SL(2, \mathbb{Z})$ symmetry: $U \rightarrow -U^{-1}$ mixes real and imaginary part of y_3

- Both problems are actually connected;
 $SL(2, \mathbb{Z})$ is broken by leading order terms

$$f_{D7} = iT \text{ & } K^{(0)}$$

- E.g.: Under $U \rightarrow -U^{-1}$
 one has $K^{(0)} \rightarrow K^{(0)} + \ln |U|^2$ ($= K^{(0)} + \ln U + \ln \bar{U}$)
 only for $y_7 = 0$!
- These points can be addressed qualitatively
 in the case without fluxes

Result for $K3 \times T^2/\mathbb{Z}_2$

[Berg, Haack, Körs; Bachas, Fabre; Antoniadis, Bachas, Dudas;
Haack, Kallosh, Krause, Linde, Lüst, Zagermann]

- $f_{D7} \sim iT - \frac{1}{8\pi^2} \sum_i \ln \vartheta_1(y_3^i, U) + \frac{3}{\pi^2} \ln \eta(U)$


depends on y_3 holomorphically!

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leading order  **depends on y_3 holomorphically!** 
- $K = -\ln[\dots - c(U - \bar{U})\mathcal{E}_2(y_3, y_7, U)]$

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 - leading order
 - depends on y_3 holomorphically!
- $K = -\ln[\dots - c(U - \bar{U})\mathcal{E}_2(y_3, y_7, U)]$
- $\mathcal{E}_2 = \sum_{i,r} [E_2(y_3^i - y_7^r, U) + E_2(y_7^r - y_3^i, U)] + (\text{other } E_2 \text{ terms})$
- $E_2(y, U) = \sum_{(n,m) \neq (0,0)} \frac{U_2^2}{|n + mU|^4} \exp \left[2\pi i \frac{y(n + m\bar{U}) - \bar{y}(n + mU)}{U - \bar{U}} \right]$

Generalized Eisenstein series

Result for $K3 \times T^2 / \mathbb{Z}_2$

[Berg, Haack, Körs; Bachas, Fabre; Antoniadis, Bachas, Dudas;
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 - Generalized Eisenstein series
- I-loop corrections restore $SL(2, \mathbb{Z})$
invariance of gauge coupling and Kähler potential

Field range

- Is there a flat direction? [Work in progress]
- What could be maximal range?
- Important because of Lyth bound:
- In literature (square 6-torus, analog of $U = i$):
- In range of validity ($L/\sqrt{\alpha'} \gg 1, g_s \ll 1$) this implies

constant of $\mathcal{O}(1/10)$

$$r \leq C \left(\frac{\Delta\phi}{M_P} \right)^2$$

$$\frac{\Delta\phi}{M_P} \leq \frac{\sqrt{g_s}\alpha'}{L^2}$$

length of torus

$$r \ll 1$$

- Kinetic term of y_3 (for $y_7 = 0$):

$$M_P^2 \frac{\partial_\mu y_3 \partial^\mu \bar{y}_3}{4\text{Im } T\text{Im } U - 2(\text{Im } y_3)^2}$$

\implies canonically normalized field:

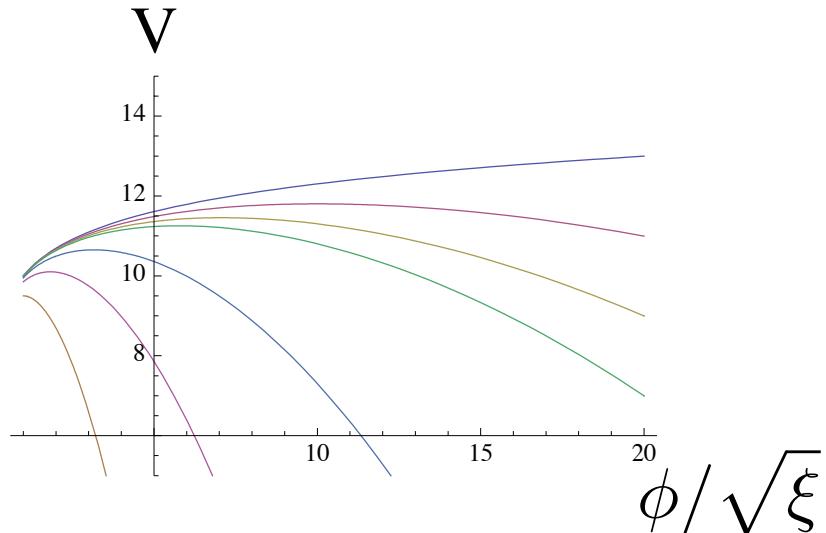
$$y_3^c = \frac{M_P y_3}{\sqrt{2\text{Im } T\text{Im } U - (\text{Im } y_3)^2}}$$

- $\frac{\Delta \text{Re } y_3^c}{M_P} \leq \frac{1+U_1}{\sqrt{U_2}} \frac{\sqrt{g_s} \alpha'}{\sqrt{\mathcal{V}_{K3}^{(0)}}}$, $\frac{\Delta \text{Im } y_3^c}{M_P} \leq \sqrt{U_2} \frac{\sqrt{g_s} \alpha'}{\sqrt{\mathcal{V}_{K3}^{(0)}}}$
- Independent of $\mathcal{V}_{T^2/\mathbb{Z}_2}$
- One or the other gets large for $U_2 \ll 1$ or $U_2 \gg 1$

Phenomenology revisited

- For small ϕ

$$V = \frac{g^2 \xi^2}{2} \left(1 + \frac{g^2}{4\pi^2} \ln \frac{\phi}{\sqrt{\xi}} \right) \rightarrow \frac{g^2 \xi^2}{2} \left(1 + \frac{g^2}{4\pi^2} \ln \frac{\phi}{\sqrt{\xi}} \right) - \frac{m^2}{2} \phi^2$$



$\implies V'$ smaller,
 $V(\phi \sim \sqrt{\xi})$
almost unchanged

- $\delta \sim \frac{V^{3/2}}{V'}$ \implies suppression of cosmic strings relative to inflationary perturbations
- $n_s \sim 0.96$ possible even for $g \ll 2 \times 10^{-3}$

Conclusions

- 1-loop corrections important for D3/D7-inflation (also for $SL(2, \mathbb{Z})$)
- usual assumption of $\text{Re } y_3$ as the inflaton should be reconsidered
- Kinematical field range can be large
- Phenomenology?