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Physics with  
magnetized branes

String Phenomenology and  
Dynamical Vacuum Selection

Liverpool, 27-29 March 2008

# Outline

- Framework

Type I string with internal magnetic fields

- Moduli stabilization

Oblique magnetic fluxes

- Supersymmetry breaking

D-term gauge mediation

- A SUSY  $SU(5)$  GUT with stabilized moduli

## General framework

Type I string theory with magnetic fluxes on 2-cycles of the compactification manifold

- Dirac quantization:  $H = \frac{m}{nA} \equiv \frac{p}{A}$

$H$ : constant magnetic field

$m$ : units of magnetic flux

$n$ : brane wrapping

$A$ : area of the 2-cycle

- Spin-dependent mass shifts for charged states

$\Rightarrow$  SUSY breaking

- Exact open string description:

$qH \rightarrow \theta = \arctan qH\alpha'$  weak field  $\Rightarrow$  field theory

- T-dual representation: branes at angles

$(m, n)$ : wrapping numbers around the 2-cycle directions

Moduli stabilization with 3-form fluxes:  
significant progress but

- no exact string description  
low energy SUGRA approximation
- fix only complex structure

Type I with internal magnetic fluxes:  
alternative/complementary approach

- exact string description
- Kähler class stabilization  
 $T^6$ : all geometric moduli fixed
- natural implementation in intersecting  
D-brane models

Magnetic fluxes can be used to stabilize moduli

I.A.-Maillard '04, I.A.-Kumar-Maillard '05, '06

e.g.  $T^6$ : 36 moduli (geometric deformations)

internal metric:  $6 \times 7/2 = 21 = 9 + 2 \times 6$

type IIB RR 2-form:  $6 \times 5/2 = 15 = 9 + 2 \times 3$

complexification  $\Rightarrow$   $\left\{ \begin{array}{ll} \text{Kähler class} & J \\ \text{complex structure} & \tau \end{array} \right.$

9 complex moduli for each

magnetic flux:  $6 \times 6$  antisymmetric matrix  $F$

complexification  $\Rightarrow$

$F_{(2,0)}$  on holomorphic 2-cycles: potential for  $\tau$

$F_{(1,1)}$  on mixed (1,1)-cycles: potential for  $J$

$T^6$  parametrization/complexification

$$x^i \equiv x^i + 1 \quad y_i \equiv y_i + 1 \quad i = 1, 2, 3$$

$$z^i = x^i + \tau^{ij} y_j$$

$\tau$ :  $3 \times 3$  complex structure matrix

$\delta g_{i\bar{j}}$  : Kähler deformations

$$\rightarrow J = \delta g_{i\bar{j}} i dz_i \wedge d\bar{z}_j$$

$W$  : covering map

of the brane world-volume over  $T^6$

$N = 1$  SUSY conditions:

1.  $F_{(2,0)} = 0 \Rightarrow \tau$

$$\tau^\top p_{xx} \tau - (\tau^\top p_{xy} + p_{yx} \tau) + p_{yy} = 0$$

2.  $J \wedge J \wedge F_{(1,1)} = F_{(1,1)} \wedge F_{(1,1)} \wedge F_{(1,1)} \Rightarrow J$

vanishing of a Fayet-Iliopoulos term

$$\xi \sim F \wedge F \wedge F - J \wedge J \wedge F$$

e.g.  $T^6 = \prod_{i=1}^3 T_i^2 \leftarrow$  orthogonal 2-torus

$$\tau_i = iR_i^x / R_i^y \quad J_i = R_i^x R_i^y \quad H_i^a = F_i^a / J_i$$

$$H_1 + H_2 + H_3 = H_1 H_2 H_3 \Leftrightarrow \theta_1 + \theta_2 + \theta_3 = 0$$

3.  $\det W(J \wedge J \wedge J - J \wedge F \wedge F) > 0$

action positivity

Main ingredients for moduli stabilization

- “oblique” (non-commuting) magnetic fields  
⇒ fix off-diagonal components of the metric  
e.g. can be made diagonal
- Non linear DBI action ⇒ fix overall volume  
not valid in six dimensions:  $J \wedge F = 0$

Stabilization of RR moduli

- Kähler class: absorbed by massive  $U(1)$ 's  
kinetic mixing with magnetized  $U(1)$ 's  
10d :  $dC_2 \wedge \star(A^a \wedge \langle F^a \rangle)$   
⇒ need at least 9 brane stacks
- Complex structure: get potential  
through mixing with NS moduli

Bianchi-Trevigne '05



Stack #	Fluxes	Fixed moduli	5 – brane localization
#1 $N_1 = 1$	$(F_{x_1 y_2}^1, F_{x_2 y_1}^1) = (1, 1)$	$\tau_{31} = \tau_{32} = 0$ $\tau_{11} = \tau_{22}$ $\text{Re}J_{1\bar{2}} = 0$	$[x_3, y_3]$
#2 $N_2 = 1$	$(F_{x_1 y_3}^2, F_{x_3 y_1}^2) = (1, 1)$	$\tau_{21} = \tau_{23} = 0$ $\tau_{11} = \tau_{33}$ $\text{Re}J_{1\bar{3}} = 0$	$[x_2, y_2]$
#3 $N_3 = 1$	$(F_{x_1 x_2}^3, F_{y_1 y_2}^3) = (1, 1)$	$\tau_{13} = 0, \tau_{11}\tau_{22} = -1$ $\text{Im}J_{1\bar{2}} = 0$	$[x_3, y_3]$
#4 $N_4 = 1$	$(F_{x_2 x_3}^4, F_{y_2 y_3}^4) = (1, 1)$	$\tau_{12} = 0$ $\text{Im}J_{2\bar{3}} = 0$	$[x_1, y_1]$
#5 $N_5 = 1$	$(F_{x_1 x_3}^5, F_{y_1 y_3}^5) = (1, 1)$	$\text{Im}J_{1\bar{3}} = 0$	$[x_2, y_2]$
#6 $N_6 = 1$	$(F_{x_2 y_3}^6, F_{x_3 y_2}^6) = (1, 1)$	$\text{Re}J_{2\bar{3}} = 0$	$[x_1, y_1]$

Last column: 5-brane charge localization on the 2-cycles  $[x_i, y_i]$

Fix areas of the 3  $T^2$ 's  $\Rightarrow$  add 3 more stacks:

Stack #	Multiplicity	Fluxes
#7	$N_7 = 1$	$(F_{x_1y_1}^7, F_{x_2y_2}^7, F_{x_3y_3}^7) = (-4, -4, 3)$
#8	$N_8 = 2$	$(F_{x_1y_1}^8, F_{x_2y_2}^8, F_{x_3y_3}^8) = (-3, 1, 1)$
#9	$N_9 = 3$	$(F_{x_1y_1}^9, F_{x_2y_2}^9, F_{x_3y_3}^9) = (-2, 3, 0)$

$$\Rightarrow \begin{pmatrix} F_1^7 & F_2^7 & F_3^7 \\ F_1^8 & F_2^8 & F_3^8 \\ F_1^9 & F_2^9 & F_3^9 \end{pmatrix} \begin{pmatrix} J_2 J_3 \\ J_1 J_3 \\ J_1 J_2 \end{pmatrix} = \begin{pmatrix} F_1^7 F_2^7 F_3^7 \\ F_1^8 F_2^8 F_3^8 \\ F_1^9 F_2^9 F_3^9 \end{pmatrix}$$

here:  $i = 1, 2, 3 \equiv i\bar{i}$

$$\Rightarrow \tau_{ij} = i\delta_{ij} \quad (J_{x_1y_1}, J_{x_2y_2}, J_{x_3y_3}) = 4\pi^2\alpha' \sqrt{\frac{3}{22}}(44, 66, 19)$$

• large volume:

- rescale all fluxes and all  $J_i \Rightarrow$  three large  $T^2$   
tadpole conditions remain invariant

## Tadpole conditions

$$Q_9 = \sum_a N_a \det W_a = 16 \leftarrow \text{O9 charge}$$

$$Q_5 = \sum_a N_a \det W_a \epsilon^{\alpha\beta\gamma\delta\sigma\tau} p_{\gamma\delta}^a p_{\sigma\tau}^a = 0$$

$$\forall \text{ 2-cycle } \alpha, \beta = 1, \dots, 6$$

SUSY + tadpole conditions seem incompatible

- use 9 magnetized branes to fix all moduli

impose SUSY conditions

- introduce an extra brane(s)

to satisfy RR tadpole cancellation

$\Rightarrow$  dilaton potential from the FI D-term

$\Rightarrow$  two possibilities:

- keep SUSY by turning on charged scalar VEVs

I.A.-Kumar-Maillard '06

D-term condition (2) is modified to:

$$qv^2(J \wedge J \wedge J - J \wedge F \wedge F) = -(F \wedge F \wedge F - F \wedge J \wedge J)$$

- EFT validity  $\Rightarrow v < 1$  in string units
- Infinite family of (large volume) solutions

invariance:  $\{F_a, J\} \rightarrow \{\Lambda F_a, \Lambda J\}$  for  $\Lambda \in \mathbb{N}$

- fixing the dilaton?

combine magnetic and 3-form fluxes

3-brane charge  $\Rightarrow T^6/\mathbb{Z}_2$  with O3 planes

magnetized D7-branes

## Tadpole cancellations + fix charged scalar VEVs

Stack #	Multiplicity	Fluxes
#7	$N_7 = 1$	$(F_{x_1y_1}^7, F_{x_2y_2}^7, F_{x_3y_3}^7) = (-4, -4, 3)$
#8	$N_8 = 2$	$(F_{x_1y_1}^8, F_{x_2y_2}^8, F_{x_3y_3}^8) = (-3, 1, 1)$
#9	$N_9 = 3$	$(F_{x_1y_1}^9, F_{x_2y_2}^9, F_{x_3y_3}^9) = (-2, 3, 0)$
#10	$N_{10} = 2$	$(F_{x_1y_1}^{10}, F_{x_2y_2}^{10}, F_{x_3y_3}^{10}) = (5, 1, 2)$
#11	$N_{11} = 2$	$(F_{x_1y_1}^{11}, F_{x_2y_2}^{11}, F_{x_3y_3}^{11}) = (0, 4, 1)$

$$\Rightarrow \tau_{ij} = i\delta_{ij} \quad (J_{x_1y_1}, J_{x_2y_2}, J_{x_3y_3}) = 4\pi^2\alpha' \sqrt{\frac{3}{22}}(44, 66, 19)$$

$$v_{10}^2\alpha' \simeq \frac{0.71}{q} \simeq 0.35 \quad v_{11}^2\alpha' \simeq \frac{0.31}{q} \simeq 0.15$$

$v_{10}, v_{11}$ : antisymmetric reps ( $q = 2$ )  $\Rightarrow$

$$SU(2) \times SU(3) \times U(2)^2 \rightarrow SU(2) \times SU(3) \times SU(2)^2$$

- break SUSY in a dS or AdS vacuum

I.A.-Derendinger-Maillard to appear

General form of the localized dilaton potential:

$$V(\phi, d) = \frac{e^{-\phi}}{g^2} \left\{ \left( \sqrt{1 - d^2} - 1 \right) + \xi d + \delta T \right\}$$

DBI action
FI-term

$d$ : D-auxiliary in  $2\pi\alpha'$ -units

$\delta T$ : tension leftover RR tadpole cancellation

$$\Rightarrow \delta T = 1 - \sqrt{1 - \xi^2}$$

$$d \text{ elimination } \Rightarrow d = \frac{\xi}{\sqrt{1 + \xi^2}}$$

$$V_{\min} = \delta \bar{T} e^{-\phi} \quad ; \quad \delta \bar{T} = \sqrt{1 + \xi^2} - \sqrt{1 - \xi^2}$$

Dilaton fixing:

1) by 3-form fluxes in a SUSY way

⇒ dS vacuum with positive energy

D-term uplifting possible from flat space

2) add a 'non-critical' (bulk) dilaton potential

⇒ AdS vacuum with tunable string coupling

$$V_{\text{non-crit}} = \delta c e^{-2\phi}$$

central charge deficit

minimization of  $V = V_{\text{non-crit}} + V_{\text{min}} \Rightarrow \delta c < 0$

$$e^{\phi_0} = -\frac{2\delta c}{3\delta T} \quad V_0 = \frac{\delta c^3}{3\delta T^2} \quad R_0 = -\delta T e^{3\phi_0}$$

curvature in Einstein frame

e.g. replace a free coordinate by a CFT minimal model

with central charge  $1 + \delta c$

D-term SUSY breaking  $\Rightarrow$

problem with Majorana gaugino masses

- lowest order: exact R-symmetry
- higher orders: suppressed by the string scale

I.A.-Taylor '04, I.A.-Narain-Taylor '05

However in toroidal models:

- gauge multiplets have extended SUSY
- $\Rightarrow$  Dirac gaugino masses without  $\mathcal{R}$
- non chiral intersections have  $N = 2$  SUSY

$\Rightarrow$  Higgs in  $N = 2$  hypermultiplet

$\Rightarrow$  New gauge mediation mechanism

I.A.-Benakli-Delgado-Quiros '07



## Spectrum multiplicities

$$(N_a, \bar{N}_b): I_{ab} = \det W_a \det W_b \int_{T^6} (F_{(1,1)}^a - F_{(1,1)}^b)^3$$

$$(N_a, N_b): I_{ab^*} \leftarrow F^{b^*} = -F^b$$

$$T^6 = \prod_i T_i^2 \Rightarrow I_{ab} = \prod_i (m_i^a n_i^b - n_i^a m_i^b)$$

$$I_{aa^*} = \prod_i \left\{ \frac{1}{2} (2m_i^a n_i^a \mp 2m_i^a) \pm 2m_i^a \right\}$$

number of intersections along orientifold axis  $(0, x)$

$$= \begin{cases} \text{Antisymmetric} : \frac{1}{2} \left( \prod_i 2m_i^a \right) \left( \prod_j n_j^a + 1 \right) \\ \text{Symmetric} : \frac{1}{2} \left( \prod_i 2m_i^a \right) \left( \prod_j n_j^a - 1 \right) \end{cases}$$

- non-chiral multiplicity: extract the vanishing factors
- $I_{ab^*} = 0 \rightarrow I_{ab}$  even  $\Rightarrow$   
 odd nb of generations: constant NS  $B$ -field  
 quantization  $\rightarrow$  magnetic fluxes  $m$  half-integers

## SUSY $SU(5)$ with stabilized moduli

I.A.-Panda-Kumar '07

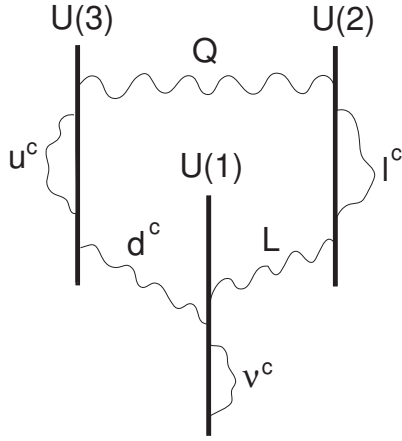
Model A of 3 brane-stacks with  $U(3)$  on top of  $U(2)$

12 brane-stacks:  $U_5, U_1, O_1, \dots, O_8, A, B$   
 $U(5) \times U(1) \times U(1)^{10}$

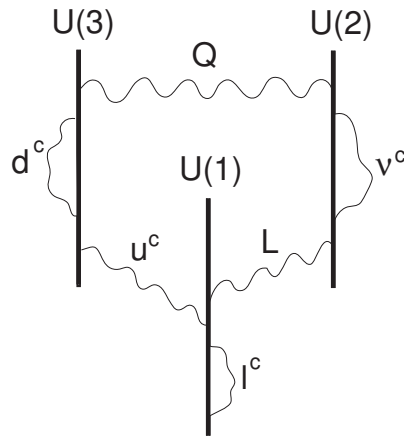
winding matrix  $W = \mathbf{1}$ ,  $B$ -field  $B_{x_i y_i} = \frac{1}{2}$

- $I_{U_5 U_5^*} = I_{U_5^* U_1} = 3 \Rightarrow 3$  generations ( $10 + \bar{5}$ )
- $I_{U_5 U_1} = 0 \Rightarrow$  Higgs pairs ( $5 + \bar{5}$ )
- $I_{U_5 a} + I_{U_5 a^*} = 0, \forall a \neq U_5, U_1$   
 $\Rightarrow$  no other  $SU(5)$  chiral states
- $O_1, \dots, O_8$ : set of oblique fluxes for  $B \neq 0$   
with diagonal induced 5-brane tadpoles

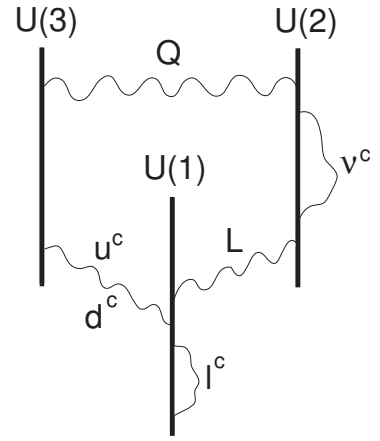
- SUSY conditions on  $U_5, O_1, \dots, O_8 \Rightarrow$   
fix all geometric moduli to diagonal metric  
 $U(1)^9$  massive (absorb the RR Kähler moduli)
  - Tadpole cancellation  $\Rightarrow$  add branes  $A, B$
  - SUSY D-flatness on  $U_1, A, B \Rightarrow$   
charged scalar VEVs  $\neq 0$  on their intersections:
    - satisfy perturbativity constraint
    - break  $U(1)^3$
- $\Rightarrow$  leftover gauge group:  $SU(5)$
- gauge non-singlet chiral spectrum:  
three generations of quarks + leptons



Model A



Model B



Model C

$Q$	$(\mathbf{3}, \mathbf{2}; 1, 1, 0)_{1/6}$	$(\mathbf{3}, \mathbf{2}; 1, \varepsilon_Q, 0)_{1/6}$	$(\mathbf{3}, \mathbf{2}; 1, \varepsilon_Q, 0)_{1/6}$
$u^c$	$(\bar{\mathbf{3}}, \mathbf{1}; 2, 0, 0)_{-2/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, 1)_{-2/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, 1)_{-2/3}$
$d^c$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, \varepsilon_d)_{1/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; 2, 0, 0)_{1/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, -1)_{1/3}$
$L$	$(\mathbf{1}, \mathbf{2}; 0, -1, \varepsilon_L)_{-1/2}$	$(\mathbf{1}, \mathbf{2}; 0, \varepsilon_L, 1)_{-1/2}$	$(\mathbf{1}, \mathbf{2}; 0, \varepsilon_L, 1)_{-1/2}$
$l^c$	$(\mathbf{1}, \mathbf{1}; 0, 2, 0)_1$	$(\mathbf{1}, \mathbf{1}; 0, 0, -2)_1$	$(\mathbf{1}, \mathbf{1}; 0, 0, -2)_1$
$\nu^c$	$(\mathbf{1}, \mathbf{1}; 0, 0, 2\varepsilon_\nu)_0$	$(\mathbf{1}, \mathbf{1}; 0, 2\varepsilon_\nu, 0)_0$	$(\mathbf{1}, \mathbf{1}; 0, 2\varepsilon_\nu, 0)_0$

$$Y_A = -\frac{1}{3}Q_3 + \frac{1}{2}Q_2$$

$$Y_{B,C} = \frac{1}{6}Q_3 - \frac{1}{2}Q_1$$

$$\text{Model A} \quad : \quad \sin^2 \theta_W = \frac{1}{2 + 2\alpha_2/3\alpha_3} \Big|_{\alpha_2=\alpha_3} = \frac{3}{8}$$

$$\text{Model B, C} \quad : \quad \sin^2 \theta_W = \frac{1}{1 + \alpha_2/2\alpha_1 + \alpha_2/6\alpha_3} \Big|_{\alpha_2=\alpha_3} = \frac{6}{7 + 3\alpha_2/\alpha_1}$$

## Conclusions

Internal magnetic fields:

simple framework, exact string description,  
 $N = 1$  SUSY with chiral fermions

Moduli stabilization: 'oblique' magnetic fluxes

general: Kähler  $\Rightarrow$  complem. to 3-form fluxes

toroidal: all geometric + eventually the dilaton

Model building

natural implementation in intersecting branes

D-term SUSY breaking  $\Rightarrow$

new mechanism of gauge mediation

Dirac gauginos,  $N = 2$  Higgs potential