

125 GeV techni-dilaton at the LHC

Shinya Matsuzaki

Maskawa Institute (Kyoto Sangyo U)

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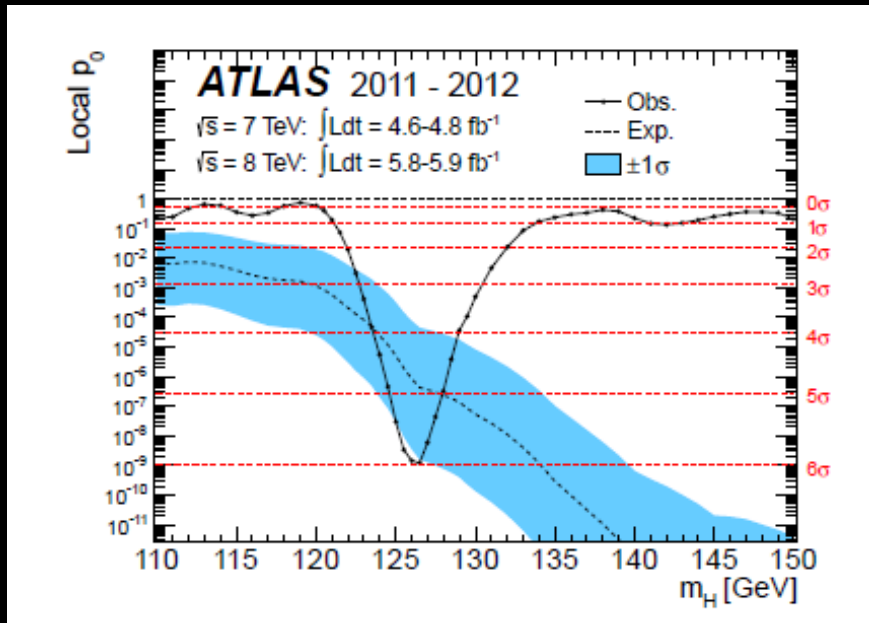
- ★ Introduction
- ★ Walking technicolor and TD
- ★ 125 GeV TD signal at LHC
- ★ Summary

Based on
S.M. and K. Yamawaki (KMI, Nagoya U.),
PRD85 (2012);
PRD86 (2012);
arXiv:1207.5911
arXiv:1209.2017

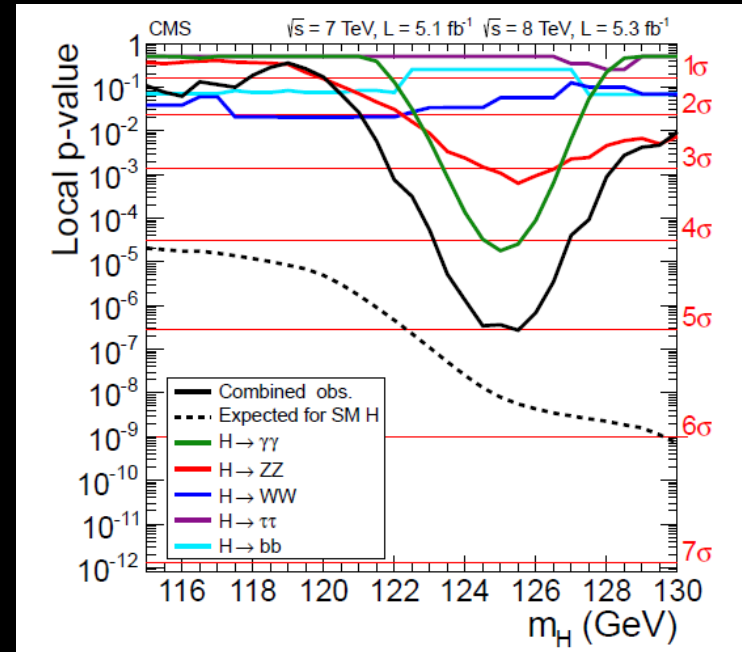
Lattice Meets Experiment 2012:
Beyond the Standard Model
26—27 October 2012, University of Colorado
at Boulder

★ Introduction & brief summary

ATLAS (arXiv: 1207.7214)



CMS (arXiv: 1207.7235)

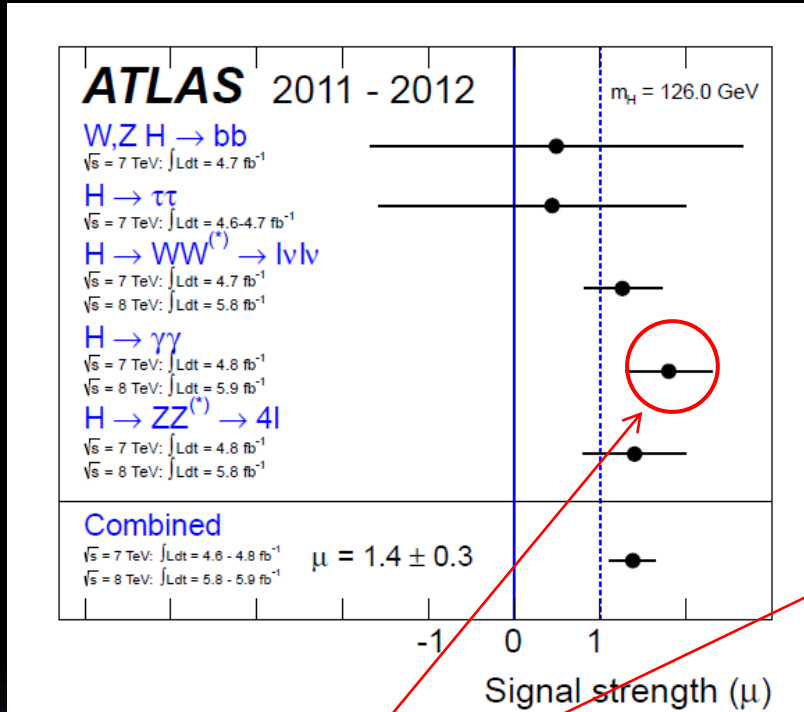


This year is exciting!!

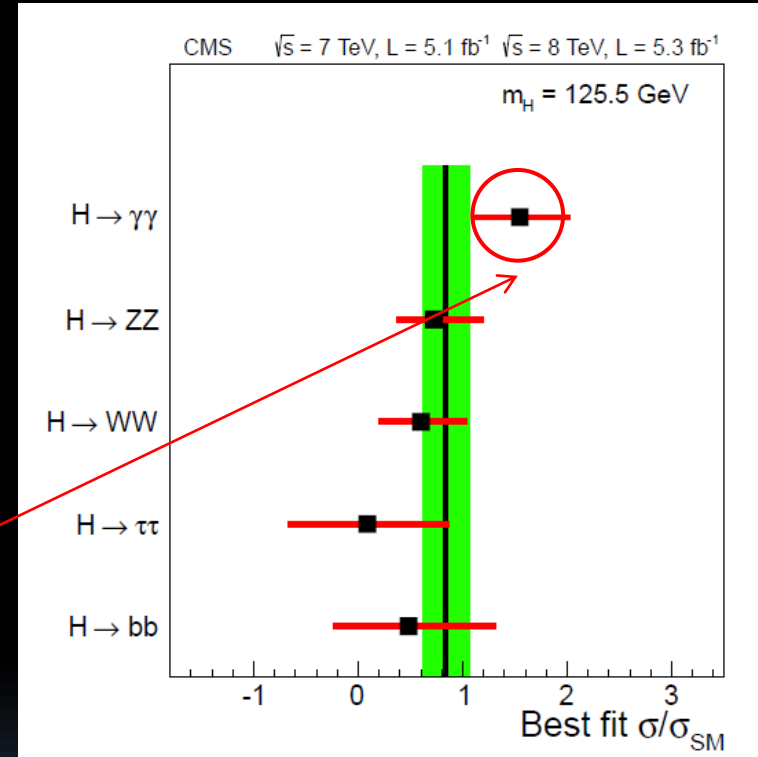
A new boson at around 125 GeV was observed at LHC, through $\gamma\gamma$, $ZZ^*(4l)$, $WW^*(2l2\nu)$

The signal strengths ($\mu = \sigma/\sigma_{SM}$)

ATLAS (arXiv: 1207.7214)



CMS (arXiv: 1207.7235)



Somewhat large diphoton event rate:
 μ (diphoton) ~ 2 implies a "new Higgs boson" (impostor)
 beyond the SM!

Is it Techni-dilaton (TD) ?

* **TD : composite scalar;**

Yamawaki et al (1986); Bando et al (1986)

predicted in walking technicolor ,

arising as a pNGB for (approximate) scale symmetry

spontaneously broken by techni-fermion condensate ;

its lightness is protected by the scale symmetry,

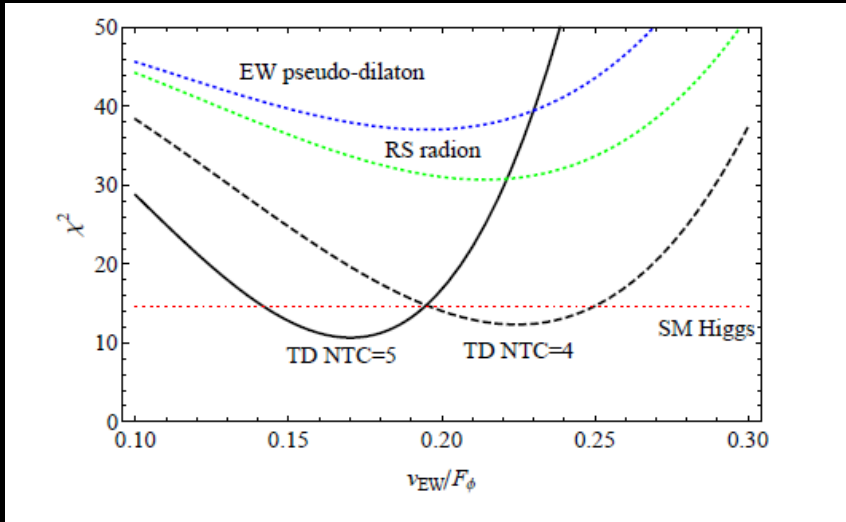
and hence can be, say, ~ 125 GeV.

* **125 GeV TD signatures at LHC are
consistent with current data!!**

S.M. and K. Yamawaki, PRD85 (2012);
PRD86 (2012); arXiv:1207.5911
arXiv:1209.2017

Quick view of main result

S.M. and K. Yamawaki, arXiv:1207.5911



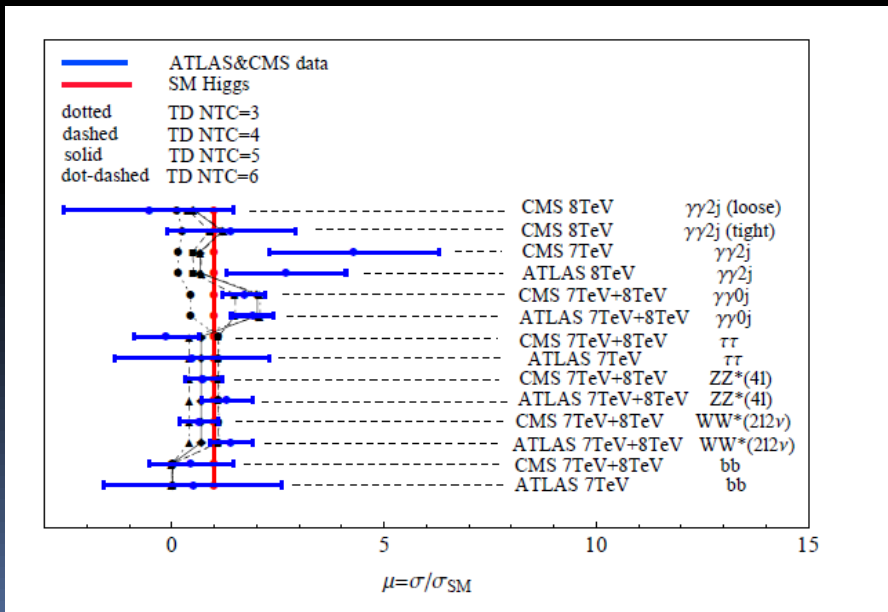
$$\chi^2 = \sum_{i \in \text{events}} \left(\frac{\mu_i - \mu_i^{\text{exp}}}{\sigma_i} \right)^2$$

TD (in 1FM) is favored by the current data !!

*** diphoton rate enhanced by techni-fermions (> W loop contribution)**

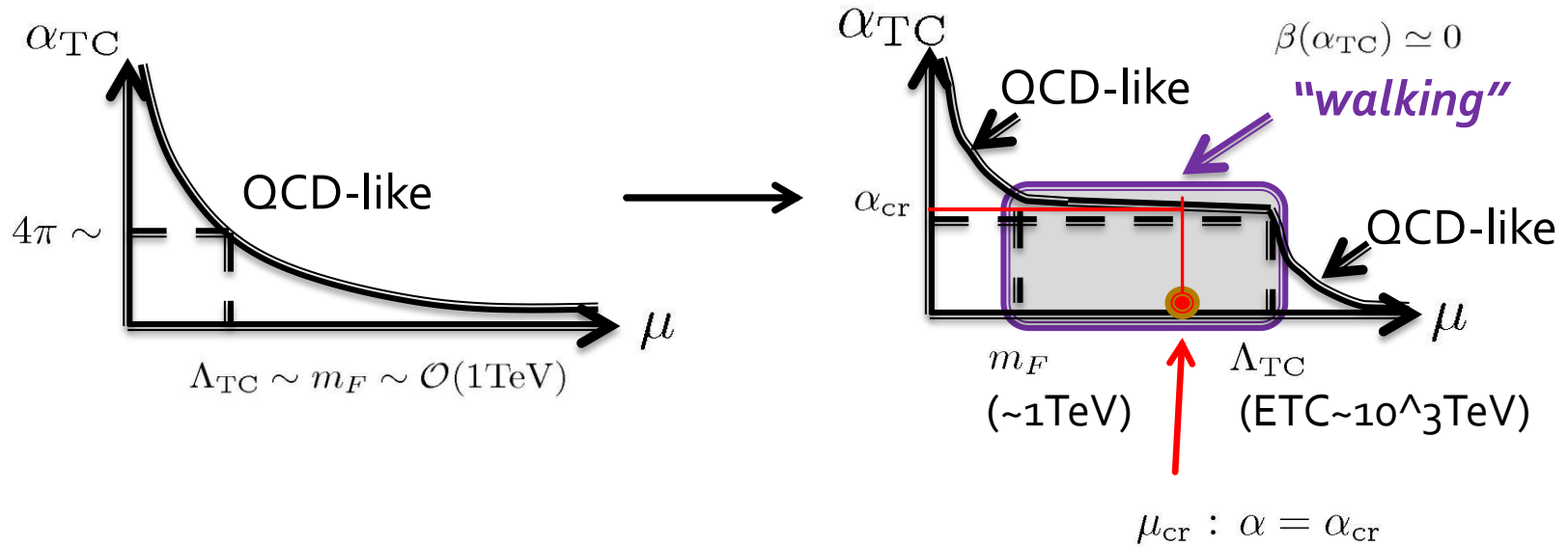
*** goodness-of-fit performed for each search category**

TD can be better than the SM Higgs



 **Walking technicolor and TD**

★ A schematic view of Walking TC



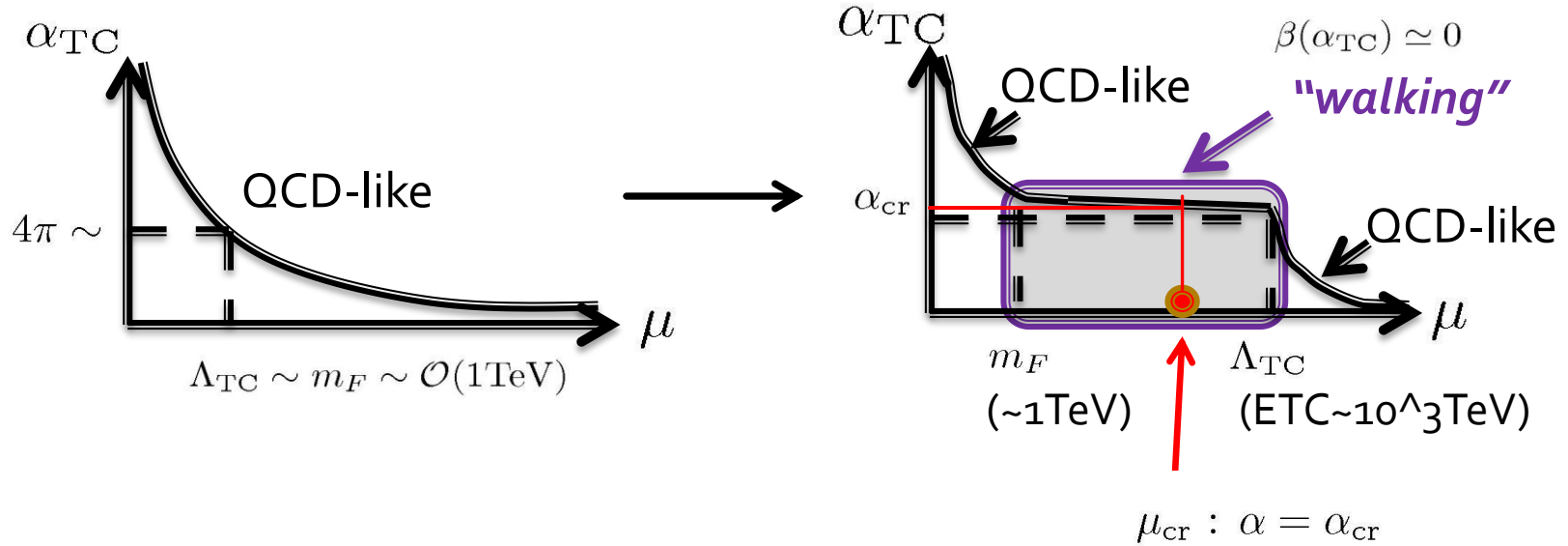
* Chiral/EW sym. breaking by dynamical generation of TF mass @ μ_{cr}

$$m_F \sim \Lambda_{TC} e^{-\frac{\pi}{\sqrt{\alpha/\alpha_{cr}-1}}} \text{ for } \alpha > \alpha_{cr} \quad \text{"Miransky scaling"} \quad \text{Miransky (1985)}$$

$$\langle \bar{F}F \rangle_{\Lambda_{TC}} \sim \frac{N_{TC}}{4\pi^2} m_F^2 \Lambda_{TC} \longrightarrow \gamma_m \simeq 1 \quad (\text{solve FCNC problem})$$

wide range walking $m_F < \mu < \Lambda_{TC}$ \longrightarrow (naturalness)
 (approx. scale invariance)

★ Walking TC and techni-dilaton



* Techni-dilaton (TD) emerges as (p)NGB for approx. scale symmetry

$$m_F \sim \Lambda_{TC} e^{-\frac{\pi}{\sqrt{\alpha/\alpha_{cr}-1}}} \text{ for } \alpha > \alpha_{cr}$$

SSB of (approximate) scale sym.

→ α starts "running" (walking) up to m_F

$$\beta(\alpha) = \Lambda_{TC} \frac{\partial \alpha}{\partial \Lambda_{TC}} = -\frac{2\alpha_{cr}}{\pi} \left(\frac{\alpha}{\alpha_{cr}} - 1 \right)^{3/2}$$

→ Nonpert. scale anomaly induced by m_F itself

$$\partial_\mu D^\mu = \frac{\beta(\alpha)}{4\alpha^2} \langle \alpha G_{\mu\nu}^2 \rangle \neq 0 : \text{TD gets massive}$$

★ Ladder estimate of TD mass

* LSD + BS in large Nf QCD

Harada et al (1989); Kurachi et al (2006)

* LSD via gauged NJL

*Shuto et al (1990); Bardeen et al (1992);
Carena et al (1992); Hashimoto (1998)*

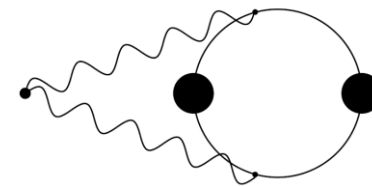
A composite Higgs mass

$$M_\phi \sim 4F_\pi$$

~500 GeV
for one-family model (1FM)
still larger than ~125 GeV

* This is reflected in PCDC (partially conserved dilatation current)

$$F_\phi^2 M_\phi^2 = -4\langle\theta_\mu^\mu\rangle = \frac{\beta(\alpha)}{\alpha}\langle G_{\mu\nu}^2\rangle \simeq 3\eta m_F^4$$



*Miransky et al (1989);
Hashimoto et al (2011):*

where $\eta \simeq \frac{N_{TC}N_{TF}}{2\pi^2} = \mathcal{O}(1)$



$$\frac{F_\phi^2}{m_F^2} \cdot \frac{M_\phi^2}{m_F^2} = \text{finite}$$

$$M_\phi/m_F \rightarrow 0,$$

only when $F_\phi/m_F \rightarrow \infty$, i.e., a decoupled limit.

No exactly massless NGB limit:

★ Holographic estimate w/ techni-gluonic effects

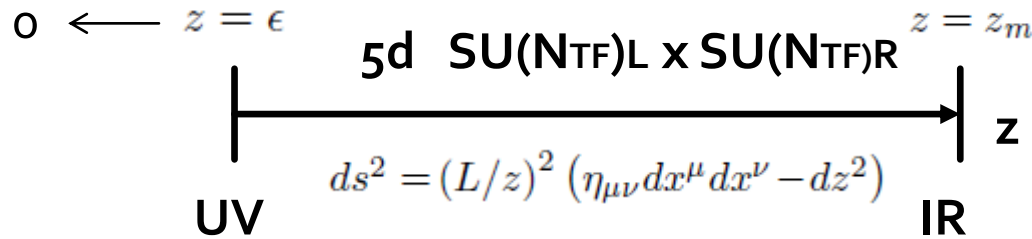
K. Haba et al PRD82 (2010); S.M. and K.Yamawaki, 1209.2017

* Ladder approximation: gluonic dynamics is neglected

* Deformation of successful AdS/QCD model (Bottom-up approach)

Da Rold and Pomarol (2005); Erlich, Katz, Son and Stephanov (2005)

incorporates nonperturbative gluonic effects



$$S_5 = \int d^4x \int_{\epsilon}^{z_m} dz \sqrt{-g} \frac{1}{g_5^2} e^{c g_5^2 \Phi_X(z)} \left(-\frac{1}{4} \text{Tr} [L_{MN} L^{MN} + R_{MN} R^{MN}] \right. \\ \left. + \text{Tr} [D_M \Phi^\dagger D^M \Phi - m_\Phi^2 \Phi^\dagger \Phi] + \frac{1}{2} \partial_M \Phi_X \partial^M \Phi_X \right)$$

$$m_\Phi^2 = -(3 - \gamma_m)(1 + \gamma_m) / \tilde{L}^2 \quad \left\{ \begin{array}{l} \text{QCD} \quad \gamma_m = 0 \\ \text{WTC} \quad \gamma_m = 1 \end{array} \right.$$

* QCD-fit w/ $\gamma_m = 0$

input

$$\begin{aligned} f_\pi &= 92.4 \text{ MeV} \\ M_\rho &= 775 \text{ MeV} \\ \langle \alpha G \mu^2 \rangle / \pi &= 0.012 \text{ GeV}^4 \end{aligned}$$

fix



model parameters

$$\begin{aligned} \xi &= 3.1 \\ G &= 0.25 \\ z m^{-1} &= 347 \text{ MeV} \end{aligned}$$

Model predictions

M_{a_1}	[a_1 meson]	:	1.3 GeV
$M_{f_0(1370)}$	[$q\bar{q}$ bound state]	:	1.2 GeV
M_G	[glueball]	:	1.3 GeV
$S = -16 \pi L_{10}$	[S parameter]	:	0.31
$[-\langle \bar{q}q \rangle]^{1/3}$	[chiral condensate]	:	277 MeV

measured

1.2 --- 1.3 GeV
1.1 --- 1.2 GeV
1.4 --- 1.7 GeV (lat.)
0.29 --- 0.37
200 --- 250 MeV

Monitoring QCD works well!

***WTC-case with $\gamma_m = 1$**

--- TD mass (lowest pole of dilatation current correlator)

$$\frac{M_\phi}{4\pi F_\pi} \simeq \sqrt{\frac{3}{N_{\text{TC}}}} \frac{\sqrt{3}/2}{1+G} \quad \frac{M_\phi}{F_\pi} \rightarrow 0 \quad \text{as} \quad G \rightarrow \infty.$$

125 GeV TD is realized by a large gluonic effect : $G \sim 10$
 for one-family model w/ $F_\pi = 123 \text{ GeV}$ (c.f. QCD case, $G \sim 0.25$)

--- TD decay constant (pole residue)

$$\begin{aligned} \frac{F_\phi}{F_\pi} &\simeq \sqrt{2N_{\text{TF}}} \cdot \sqrt{J_0^2(x) + J_1^2(x)} \Big|_{x=(M_\phi z_m) \ll 1} \\ &\simeq \underline{\sqrt{2N_{\text{TF}}}} \quad \text{free from model-parameters !!} \end{aligned}$$

→ **Exactly-massless NGB limit ("conformal limit") is realized:**

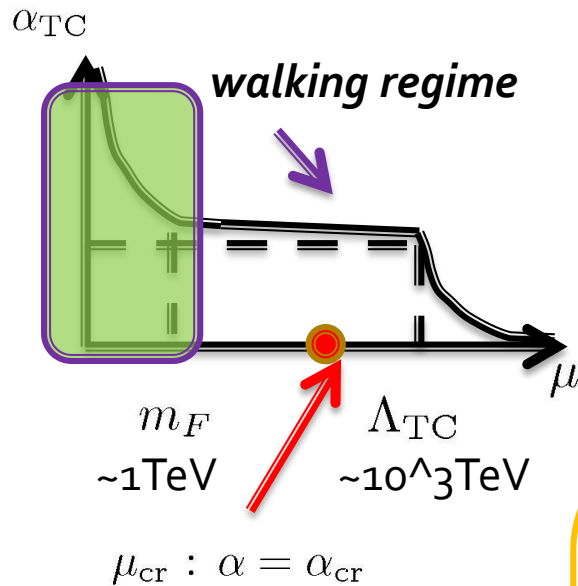
$$\frac{M_\phi}{F_\pi} \rightarrow 0 \quad \text{and} \quad \frac{F_\phi}{F_\pi} \rightarrow \text{finite}, \quad \text{as} \quad G \rightarrow \infty. \quad \left[\beta(\alpha) \sim \frac{1}{G(1+G)^2} \rightarrow 0 \right]$$

in contrast to ladder approximation

Lattice calcs will give a conclusive answer

★ TD Lagrangian below m_F

S.M. and K. Yamawaki, PRD86 (2012)



* effective theory below m_F
after TF decoupled/integrated out
& confinement :

governed by TD and other light TC hadrons

* Nonlinear realization of scale and
chiral symmetries

Nonlinear base χ for scale sym. w/ TD field Φ

$$\chi = e^{\phi/F_\phi}, \quad \delta\chi = (1 + x^\nu \partial_\nu)\chi$$

TD decay constant F_Φ

$$\delta\phi = F_\phi + x^\nu \partial_\nu \phi$$

Nonlinear base U for chiral sym. w/ TC pion field π

$$U = e^{2i\pi/F_\pi}$$

$$\delta U = x^\nu \partial_\nu U$$

eff. TD Lagrangian $\mathcal{L} = \mathcal{L}_{\text{inv}} + \mathcal{L}_S - V_\chi$

i) The scale anomaly-free part:

$$\mathcal{L}_{\text{inv}} = \frac{F_\pi^2}{4} \chi^2 \text{Tr}[\mathcal{D}_\mu U^\dagger \mathcal{D}^\mu U] + \frac{F_\phi^2}{2} \partial_\mu \chi \partial^\mu \chi$$

ii) The anomalous part (made invariant by including spurion field "S"):

$$\mathcal{L}_S = -m_f \left(\left(\frac{\chi}{S} \right)^{2-\gamma_m} \cdot \chi \right) \bar{f} f \quad \longrightarrow \text{reflecting ETC-induced TF 4-fermi w/ } (3-\gamma_m)$$

$$+ \log \left(\frac{\chi}{S} \right) \left\{ \frac{\beta_F(g_s)}{2g_s} G_{\mu\nu}^2 + \frac{\beta_F(e)}{2e} F_{\mu\nu}^2 \right\} + \dots$$

iii) The scale anomaly part:

$$V_\chi = \frac{F_\phi^2 M_\phi^2}{4} \chi^4 \left(\log \chi - \frac{1}{4} \right)$$

β_F : TF-loop contribution to beta function

which correctly reproduces the PCDC relation:

$$\langle \theta_\mu^\mu \rangle = -\delta_D V_\chi \Big|_{\text{vacuum}} = -\frac{F_\phi^2 M_\phi^2}{4} \langle \chi^4 \rangle \Big|_{\text{vacuum}} = -\frac{F_\phi^2 M_\phi^2}{4}$$

TD couplings to the SM particles

* TD couplings to W/Z boson (from L_inv)

$$g_{\phi WW/ZZ} = \frac{2m_{W/Z}}{F_{\phi}}$$

* TD couplings to $\gamma\gamma$ and gg (from L_S)

$$g_{\phi\gamma\gamma} = \frac{\beta_F(e)}{e} \frac{1}{F_{\phi}}$$

$$g_{\phi gg} = \frac{\beta_F(g_s)}{g_s} \frac{1}{F_{\phi}}$$

β_F : TF-loop contribution
to beta function

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- * TD couplings to W/Z boson (from L_inv)

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$$g_{\phi gg} = \frac{\beta_F(g_s)}{g_s} \frac{1}{F_{\phi}}$$

β_F : TF-loop contribution
to beta function

The same form as
SM Higgs couplings
except F_{ϕ} and betas

* TD couplings to SM fermions

$$-\frac{(3 - \gamma_m)m_f}{F_\phi} \phi \bar{f} f$$

* $\gamma_m \simeq 1$

in **WTC** to get realitic masses w/o FCNC concerning **1st and 2nd generations**

$$\frac{g_{\phi ff}}{g_{h_{SM} ff}} = \mathbf{2} \frac{v_{EW}}{F_\phi}$$

Miransky et al (1989); Matsumoto (1989); Appelquist et al (1989)

* $\gamma_m \simeq 2$,

in **Strong ETC** to accommodate masses of the **3rd generations (t, b, tau)**

$$\frac{g_{\phi ff}}{g_{h_{SM} ff}} = \mathbf{1} \frac{v_{EW}}{F_\phi}$$

Thus, the TD couplings to SM particles essentially take the same form as those of the SM Higgs! :

Just a *simple scaling* from the SM Higgs:

$$\frac{g_{\phi WW/ZZ}}{g_{h_{SM} WW/ZZ}} = \frac{v_{EW}}{F_{\phi}},$$

$$\frac{g_{\phi ff}}{g_{h_{SM} ff}} = \frac{v_{EW}}{F_{\phi}}, \quad \text{for } f = t, b, \tau.$$

But, note ϕ - gg , ϕ - $\gamma\gamma$ depending highly on particle contents of WTC models.

β_F : TF-loop contribution to beta function

$$\mathcal{L}_{\phi\gamma\gamma,gg} = \frac{\phi}{F_{\phi}} \left[\frac{\beta_F(e)}{2e^3} F_{\mu\nu}^2 + \frac{\beta_F(g_s)}{2g_s^3} G_{\mu\nu}^2 \right]$$

To be concrete, we consider the *one-family model (1FM)*

★ Estimate of $\frac{v_{EW}}{F_\phi}$: #1 – Ladder approximation

* PCDC (partially conserved dilatation current)

$$F_\phi^2 M_\phi^2 = -4 \langle \theta_\mu^\mu \rangle \quad \langle \theta_\mu^\mu \rangle = 4 \mathcal{E}_{\text{vac}} = -\kappa_V \left(\frac{N_{\text{TC}} N_{\text{TF}}}{2\pi^2} \right) m_F^4$$

* **criticality condition** Appellequist et al (1996)

$$N_{\text{TF}} \simeq 4N_{\text{TC}}$$

* **Pagels-Stokar formula**

$$F_\pi \simeq v_{EW} / \sqrt{N_D}$$

of EW doublets

$$F_\pi^2 = \kappa_F^2 \frac{N_{\text{TC}}}{4\pi^2} m_F^2$$

$$\frac{v_{EW}}{F_\phi} \simeq \frac{1}{8\sqrt{2}\pi} \sqrt{\frac{\kappa_F^4}{\kappa_V} N_D} \frac{M_\phi}{v_{EW}}$$

* **Recent ladder SD analysis (large Nf QCD)**

$$\kappa_V \simeq 0.7, \quad \kappa_F \simeq 1.4$$

Hashimoto et al (2011)

* Inclusion of theoretical uncertainties

Ladder approximation is subject to **about 30% uncertainty** for estimate of critical coupling and QCD hadron spectrum

critical coupling : T. Appelquist et al (1988);

Hadron spectrum : K. -I. Aoki et al (1991); M. Harada et al (2004).

$$\frac{N_{\text{TF}}}{4N_{\text{TC}}} \simeq 1 \pm \underline{0.3} \quad \langle \theta_{\mu}^{\mu} \rangle = 4\mathcal{E}_{\text{vac}} = \underline{\kappa_V} \left(\frac{N_{\text{TC}} N_{\text{TF}}}{2\pi^2} \right) m_F^4$$

30%

$$F_{\pi}^2 = \underline{\kappa_F^2} \frac{N_{\text{TC}}}{4\pi^2} m_F^2$$

30%

Estimate
w/ uncertainty included

$$\frac{v_{\text{EW}}}{F_{\phi}} \simeq \underline{(0.1 - 0.3)} \times \left(\frac{N_D}{4} \right) \left(\frac{M_{\phi}}{125 \text{ GeV}} \right)$$

★ Estimate of $\frac{v_{EW}}{F_\phi}$:#2 -- Holographic approach

* TD decay constant for the light TD case w/ $G \sim 10$:

$$\begin{aligned} \frac{F_\phi}{F_\pi} &\simeq \sqrt{2N_{TF}} \cdot \sqrt{J_0^2(x) + J_1^2(x)} \Big|_{x=(M_\phi z_m) \ll 1} \\ &\simeq \underline{\sqrt{2N_{TF}}} \quad \text{free from model-parameters !!} \end{aligned}$$

Inclusion of typical size of $1/N_{TC}$ (20% ~ 30%) corrections:

$$\left. \frac{v_{EW}}{F_\phi} \right|_{\text{holo}}^{+1/N_{TC}} \sim 0.2 - 0.4$$

This is consistent with ladder estimate:

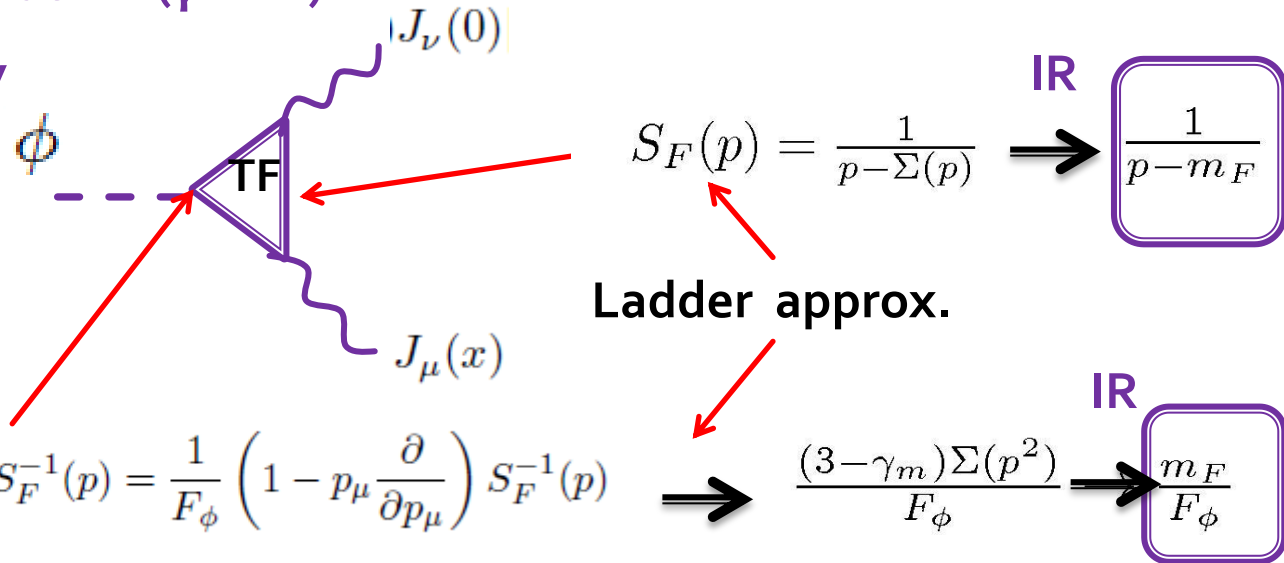
$$\frac{v_{EW}}{F_\phi} \stackrel{\text{ladder}}{\simeq} \underline{(0.1 - 0.3)} \times \left(\frac{N_D}{4} \right) \left(\frac{M_\phi}{125 \text{ GeV}} \right)$$

* Calculation of beta functions

$$\mathcal{L}_{\phi\gamma\gamma,gg} = \frac{\phi}{F_\phi} \left[\frac{\beta_F(e)}{2e^3} F_{\mu\nu}^2 + \frac{\beta_F(g_s)}{2g_s^3} G_{\mu\nu}^2 \right]$$

The loop is dominated at IR ($\gamma_m = 2$)

(well approximated by constant mass)



Yukawa vertex

$$\chi_{\phi FF}(p, q=0) = \frac{1}{F_\phi} \delta_D S_F^{-1}(p) = \frac{1}{F_\phi} \left(1 - p_\mu \frac{\partial}{\partial p_\mu} \right) S_F^{-1}(p) \Rightarrow \frac{(3 - \gamma_m) \Sigma(p^2)}{F_\phi} \Rightarrow \frac{m_F}{F_\phi}$$

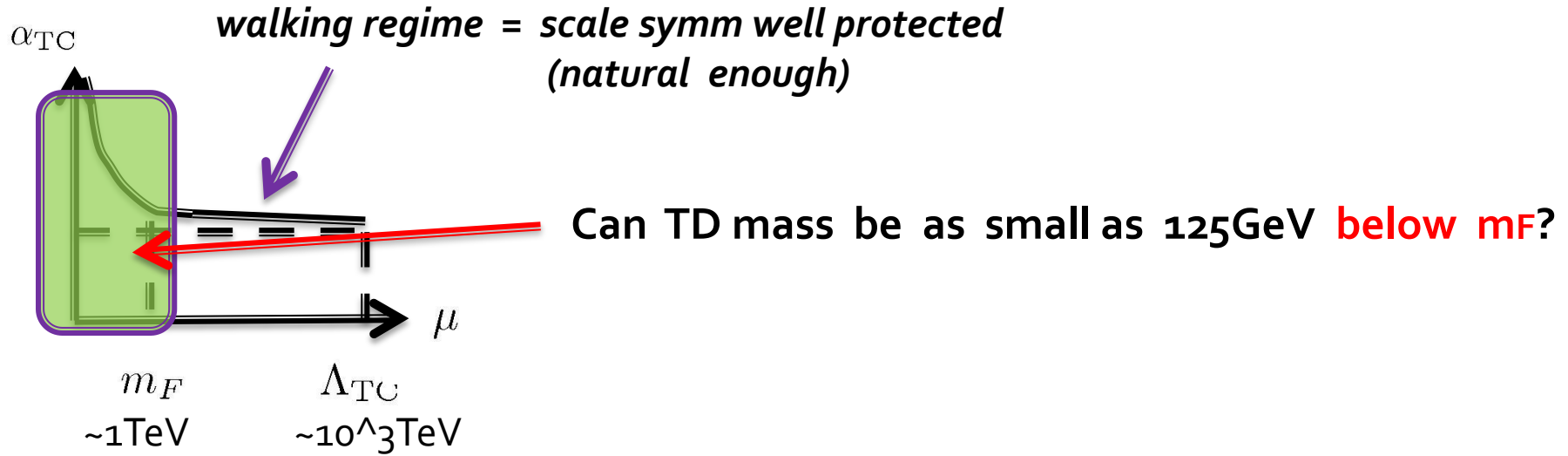
The resultant betas coincide just one-loop perturbative expressions:

$$\beta_F(g_s) = \frac{g_s^3}{(4\pi)^2} \frac{4}{3} N_{TC}$$

$$\beta_F(e) = \frac{e^3}{(4\pi)^2} \frac{16}{9} N_{TC}$$

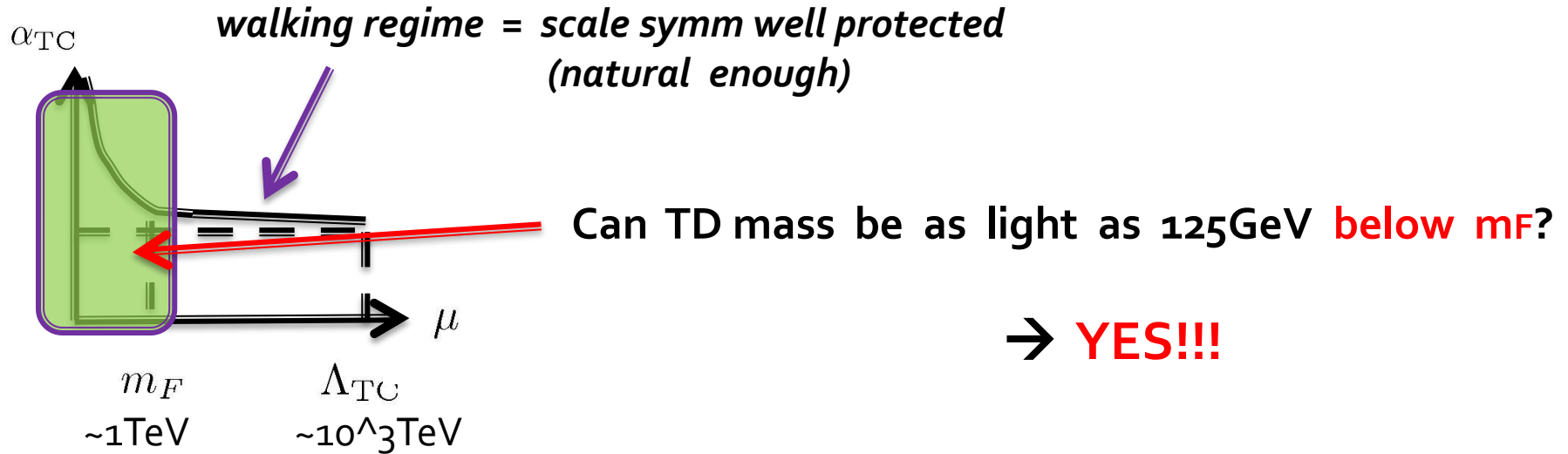
★ TD mass stability below m_F

S.M. and K. Yamawaki, PRD86 (2012)



★ TD mass stability below m_F

S.M. and K. Yamawaki, PRD86 (2012)



Work on the eff. TD Lagrangian: $\mathcal{L} = \mathcal{L}_{\text{inv}} + \mathcal{L}_S - V_\chi$

Dominant corrections come from top-loop

cutoff by $m_F \sim 4 \pi F \pi \sim 1 \text{ TeV} (\sim F\Phi)$

w/ $m_t^2 \simeq 2M_\phi^2$ $\frac{\delta M_\phi}{M_\phi(125 \text{ GeV})} \approx -\frac{3}{4\pi^2} \frac{m_F^2}{F_\phi^2} \approx \mathcal{O}(10^{-2} - 10^{-1})$

naturally light thanks to large $F\Phi$

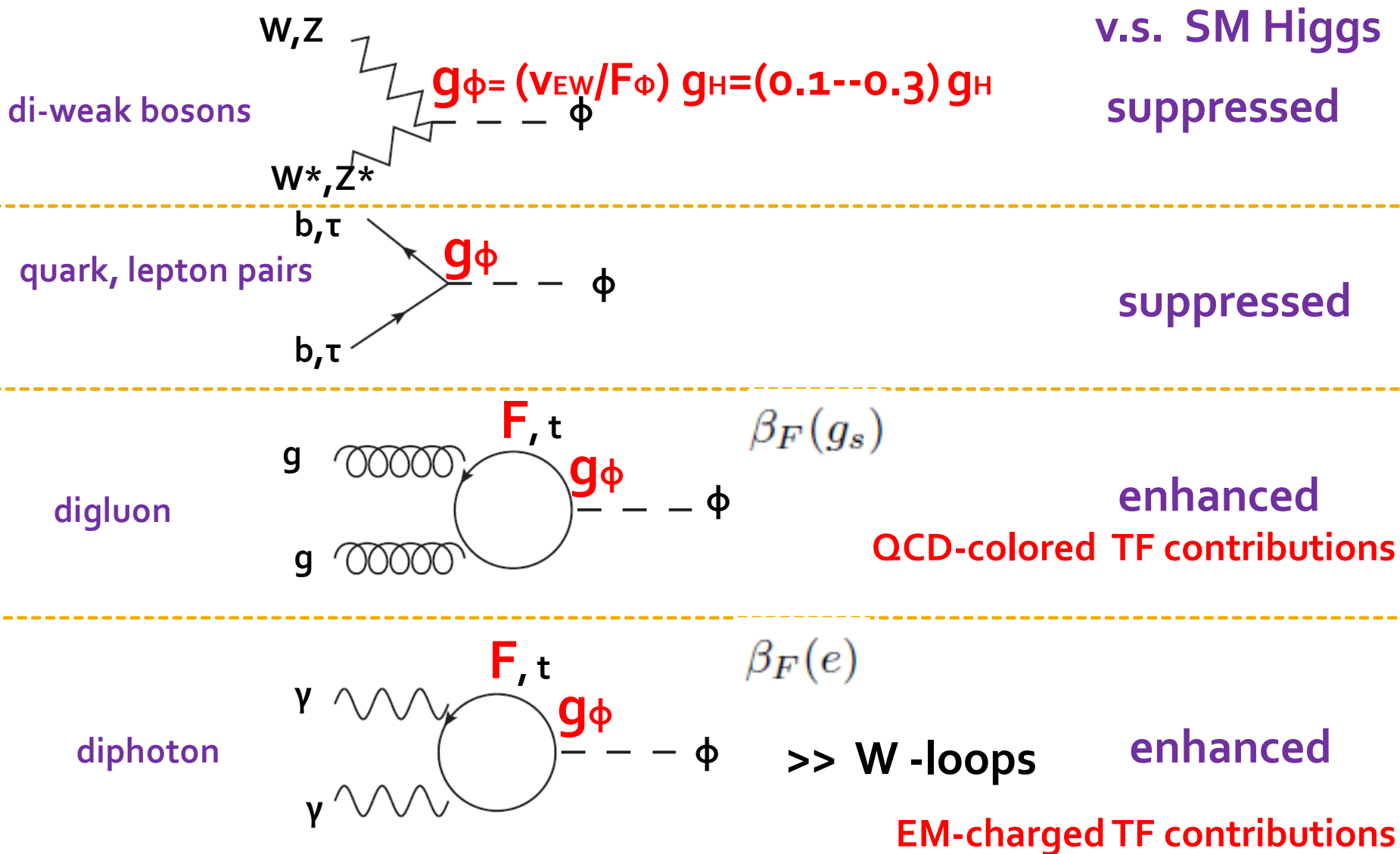


125 GeV TD signal at the LHC

S.M. and K. Yamawaki

PRD85 (2012);
PRD86 (2012);
arXiv:1207.5911;
arXiv:1209.2017

★ Characteristic features of 125 GeV TD in 1FM (w/ $N_{TC}=4,5$) at LHC



★ The 125 GeV TD signal strengths

* decays to bb, tau tau, WW*, ZZ*, diphoton

bb:

$$\begin{aligned}\mu_{b\bar{b}} &= \frac{\sigma_{\text{VBA}}^{\phi}(s) \text{BR}(\phi \rightarrow b\bar{b})}{\sigma_{\text{VBA}}^{h_{\text{SM}}}(s) \text{BR}(h_{\text{SM}} \rightarrow b\bar{b})} \\ &= \frac{\sigma_{W\phi}(s) + \sigma_{Z\phi}(s)}{\sigma_{Wh_{\text{SM}}}(s) + \sigma_{Zh_{\text{SM}}}(s)} \frac{\text{BR}(\phi \rightarrow b\bar{b})}{\text{BR}(h_{\text{SM}} \rightarrow b\bar{b})}\end{aligned}$$

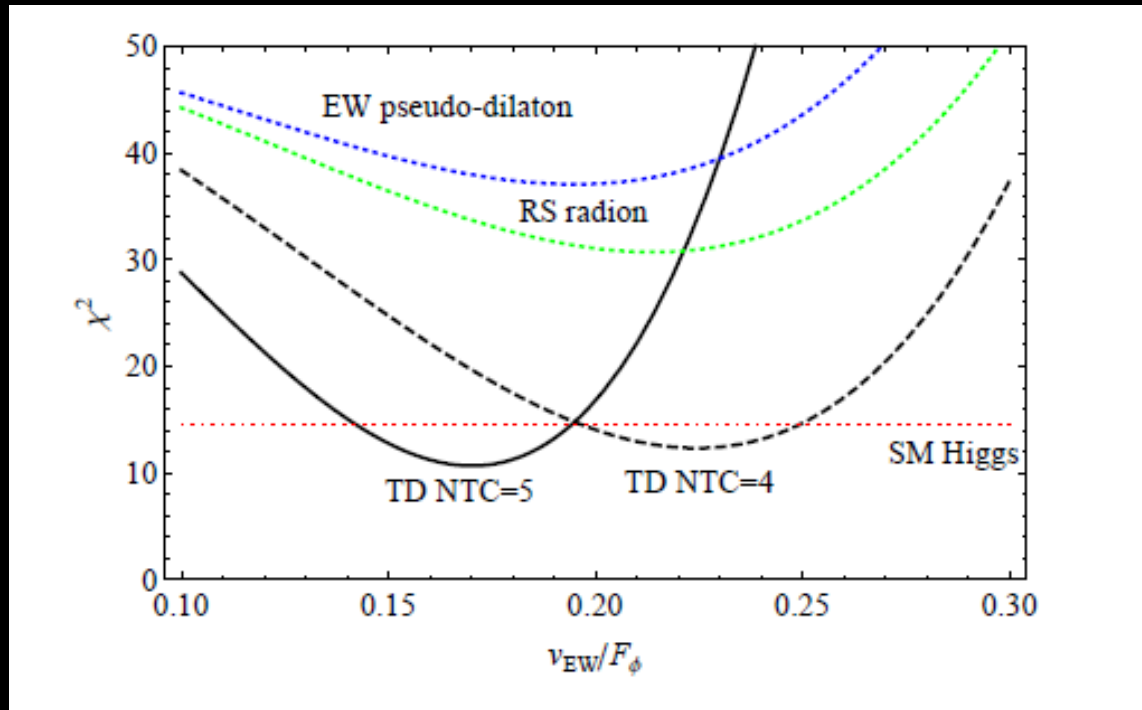
X= tautau, WW*, ZZ*:

$$\mu_X = \frac{\sigma_{\text{GF}}^{\phi}(s) + \sigma_{\text{VBF}}^{\phi}(s)}{\sigma_{\text{GF}}^{h_{\text{SM}}}(s) + \sigma_{\text{VBF}}^{h_{\text{SM}}}(s)} \frac{\text{BR}(\phi \rightarrow X)}{\text{BR}(h_{\text{SM}} \rightarrow X)}$$

diphoton

$$\begin{aligned}\mu_{\gamma\gamma 0j} &= \frac{\sigma_{\text{GF}}^{\phi}(s) \text{BR}(\phi \rightarrow X)}{\sigma_{\text{GF}}^{h_{\text{SM}}}(s) \text{BR}(h_{\text{SM}} \rightarrow X)}, \\ \mu_{\gamma\gamma 2j} &= \frac{\xi_{\text{GF}} \cdot \sigma_{\text{GF}}^{\phi}(s) + \xi_{\text{VBF}} \cdot \sigma_{\text{VBF}}^{\phi}(s)}{\xi_{\text{GF}} \cdot \sigma_{\text{GF}}^{h_{\text{SM}}}(s) + \xi_{\text{VBF}} \cdot \sigma_{\text{VBF}}^{h_{\text{SM}}}(s)} \\ &\quad \times \frac{\text{BR}(\phi \rightarrow \gamma\gamma)}{\text{BR}(h_{\text{SM}} \rightarrow \gamma\gamma)},\end{aligned}$$

* χ^2 fit based on the current data on Higgs search categories



$$\chi^2 = \sum_{i \in \text{events}} \left(\frac{\mu_i - \mu_i^{\text{exp}}}{\sigma_i} \right)^2$$

N_{TC}	$(v_{\text{EW}}/F_\phi)_{\text{best}}$	$\chi^2_{\text{min}}/\text{d.o.f}$
4	0.22	12/13 \simeq 0.9
5	0.17	10/13 \simeq 0.7

* **TD** can be **better** than the SM Higgs ($\chi^2/\text{d.o.f} = 1.0$), due to **the enhanced diphoton rate**, in contrast to *other dilaton/radion scenarios* w/o extra BSM contributions like **TF**

* The best-fit signal strengths (for each category)

$$\underline{\mu_{Vbb} = 0.006 \text{ -- } 0.01}$$

$$\mu_{WW^*} = 0.9 \text{ -- } 1.0$$

$$\mu_{ZZ^*} = 0.7 \text{ -- } 1.1$$

$$\mu_{\tau\tau} = 0.7 \text{ -- } 1.1$$

$$\underline{\mu_{\gamma\gamma\phi j} = 1.5 \text{ -- } 2.0}$$

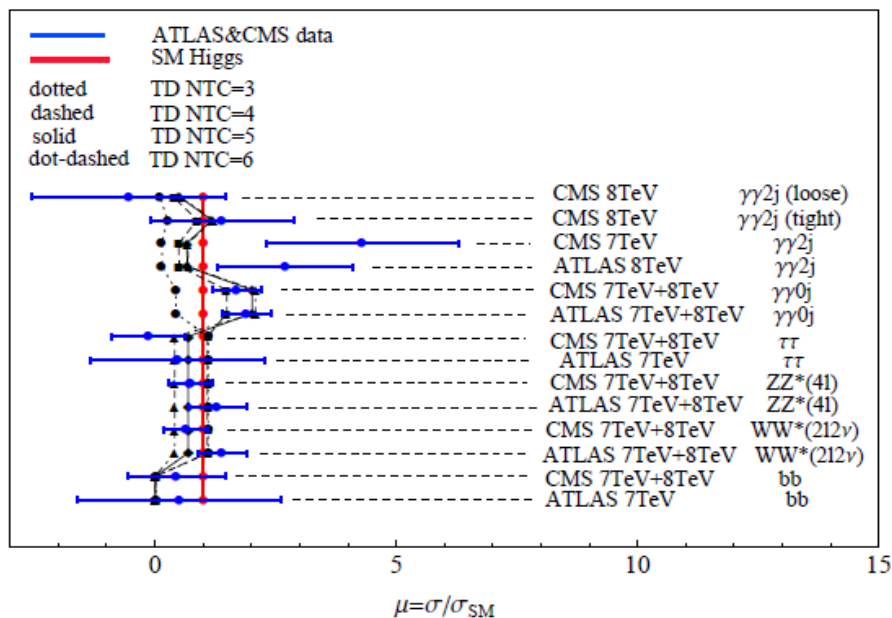
$$\mu_{\gamma\gamma z j} = 0.5 \text{ -- } 0.7$$

N_{TC}	$(v_{EW}/F_\phi)_{best}$	$\chi^2_{min}/d.o.f$
4	0.22	12/13 \approx 0.9
5	0.17	10/13 \approx 0.7

Characteristic feature:

V_{bb} : **suppressed**

$\gamma\phi j$: **enhanced**



★ Summary

- * TD is the characteristic light scalar in WTC: the mass can be 125 GeV; protected by approximate scale invariance.
- * The couplings to the SM particles take essentially the same forms as those for the SM Higgs, except couplings to diphoton and digluon.
- * The 125 GeV TD in 1FM gives the LHC signal favored by current LHC data, notably somewhat large diphoton event rate thanks to extra TF contributions.
- * More precise measurements on exclusive categories (e.g., Vbb , $\tau\tau$ +jets) will draw a definite conclusion that the TD is favored, or not.

Backup Slides

$$S_5 = \int d^4x \int_{\epsilon}^{z_m} dz \sqrt{-g} \frac{1}{g_5^2} e^{cg_5^2 \Phi_X(z)} \left(-\frac{1}{4} \text{Tr} [L_{MN} L^{MN} + R_{MN} R^{MN}] \right. \\ \left. + \text{Tr} [D_M \Phi^\dagger D^M \Phi - m_\Phi^2 \Phi^\dagger \Phi] + \frac{1}{2} \partial_M \Phi_X \partial^M \Phi_X \right)$$

$$\Phi(x, z) = \frac{1}{\sqrt{2}} (v(z) + \sigma(x, z)) \exp[i\pi(x, z)/v(z)]$$

$$\Phi_X(z) = v_X(z),$$

AdS/CFT dictionary:

*** UV boundary values = sources**

$$\alpha M = \lim_{\epsilon \rightarrow 0} Z_m \left(\frac{L}{z} v(z) \right) \Big|_{z=\epsilon}, \quad Z_m = Z_m(L/z) = \left(\frac{L}{z} \right)^{\gamma_m}$$

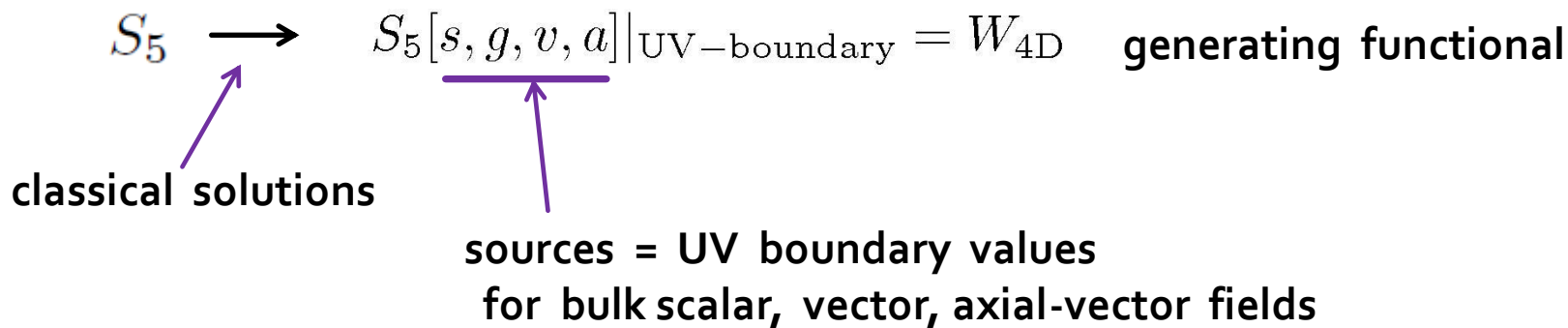
$$M' = \lim_{\epsilon \rightarrow 0} L v_X(z) \Big|_{z=\epsilon}$$

*** IR boundary values:**

$$\xi = L v(z) \Big|_{z=z_m} \longleftrightarrow \text{chiral condensate } \langle \bar{T} T \rangle$$

$$\mathcal{G} = L v_X(z) \Big|_{z=z_m} \longleftrightarrow \text{gluon condensate } \langle \alpha G_{\mu\nu}^2 \rangle$$

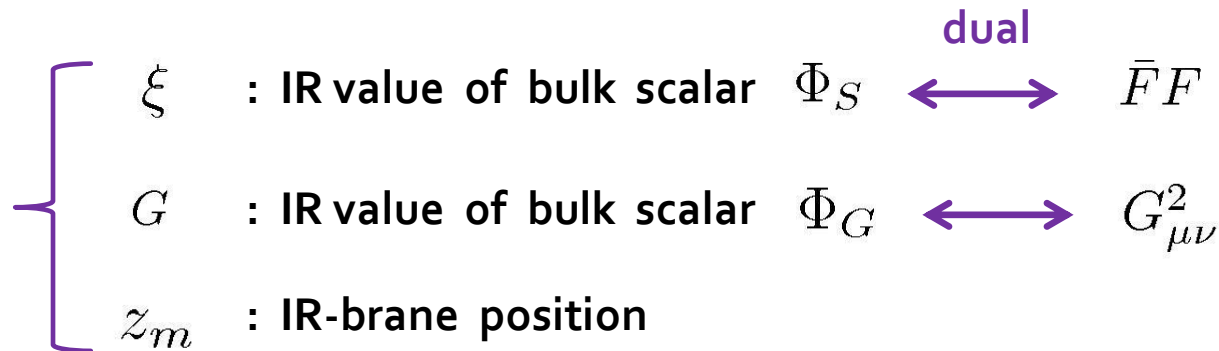
* AdS/CFT recipe:



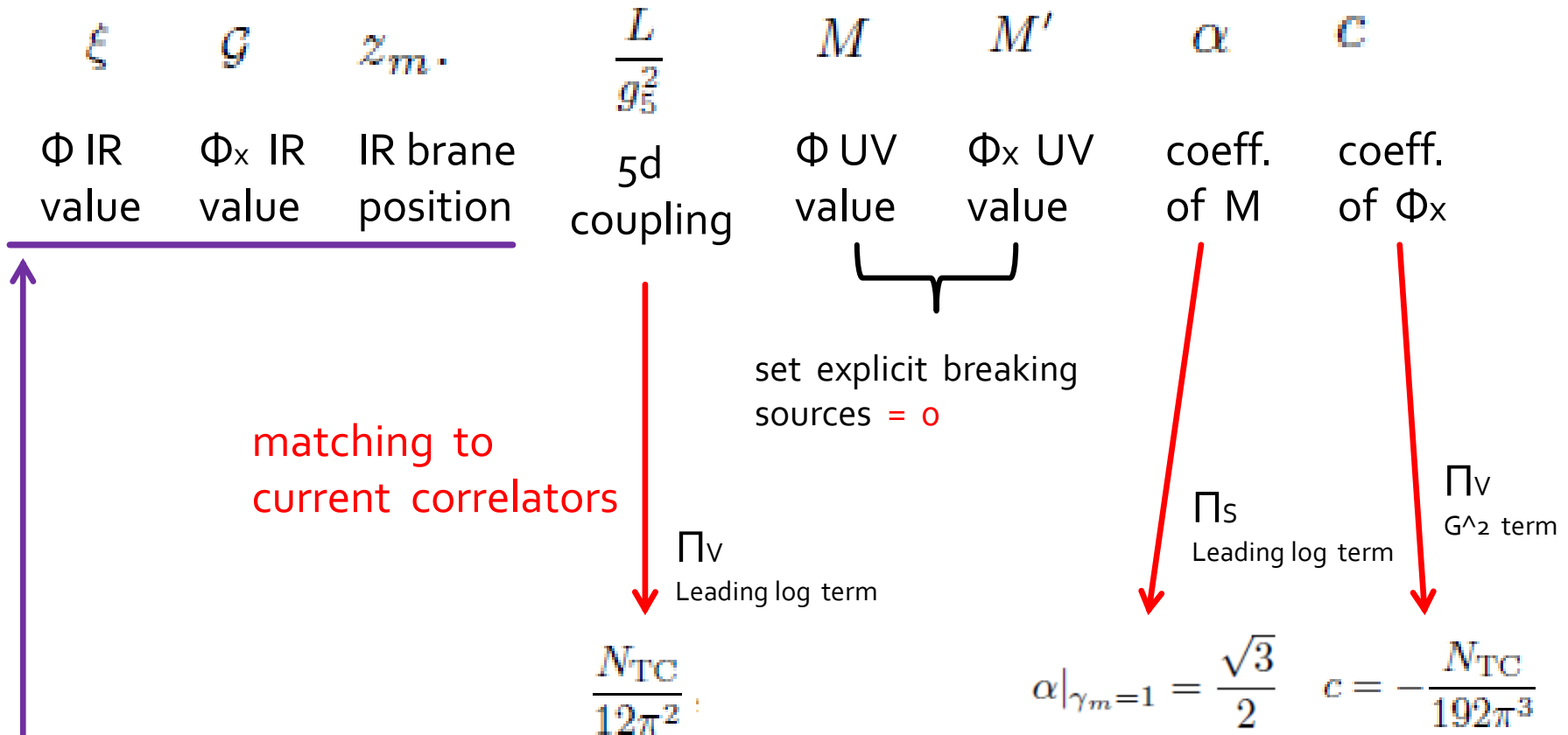
$$W_{4\text{D}} \longrightarrow \langle T J(x) J(0) \rangle \quad J = \bar{F}F, G_{\mu\nu}^2, \bar{F}\gamma_\mu T^a F, \bar{F}\gamma_\mu\gamma_5 T^a F$$

Current correlators $\Pi_S, \Pi_G, \Pi_V, \Pi_A$

are calculated as a function of three IR-boundary values and γ_m :



The model parameters:



3 phenomenological input values

$$F_\pi = 246 \text{ GeV}/\sqrt{N_D} = 123 \text{ GeV} \quad (1\text{FM})$$

$$M_\Phi = 125 \text{ GeV}$$

$$S = 0.1$$

Other holographic predictions (1FM w/ S=0.1)NTC = 3

Techni- ρ , a_1 masses	:	$M_\rho = M_{a_1} = 3.5$ TeV
Techni-glueball (TG) mass	:	$M_G = 19$ TeV
TG decay constant	:	$F_G = 135$ TeV
dynamical TF mass m_F	:	$m_F = 1.0$ TeV

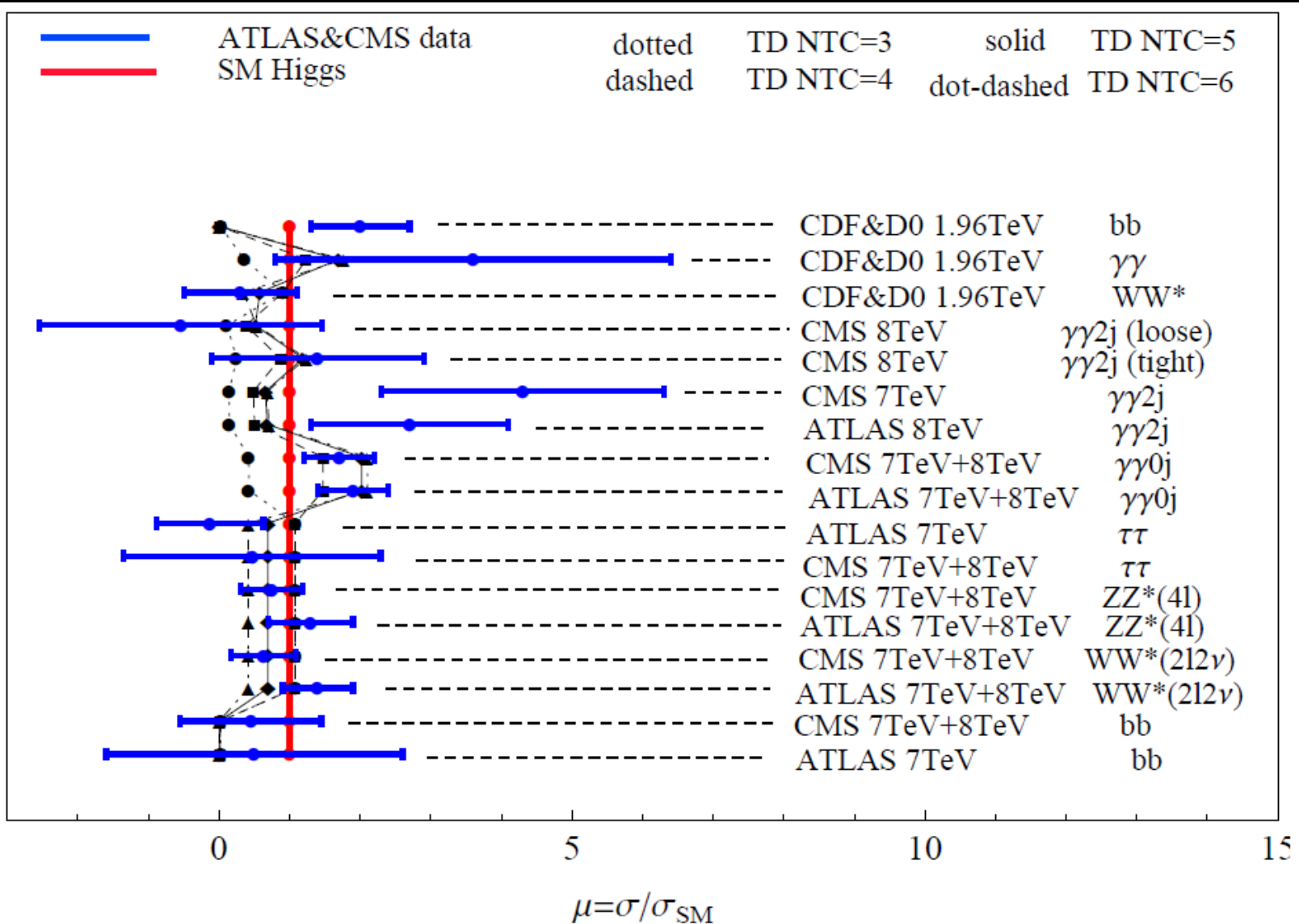
NTC = 4

Techni- ρ , a_1 masses	:	$M_\rho = M_{a_1} = 3.6$ TeV
Techni-glueball (TG) mass	:	$M_G = 18$ TeV
TG decay constant	:	$F_G = 156$ TeV
dynamical TF mass m_F	:	$m_F = 0.95$ TeV

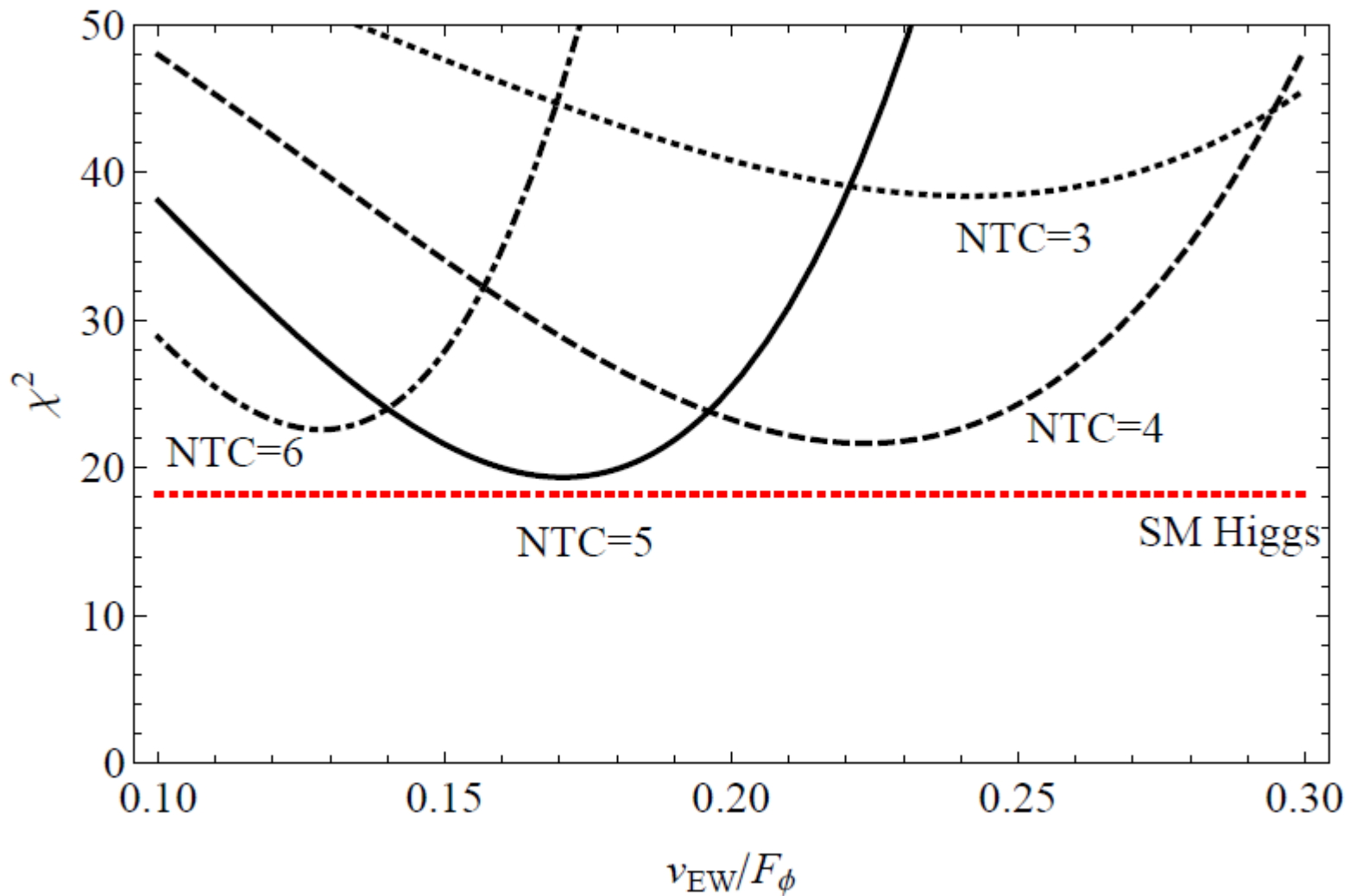
NTC = 5

Techni- ρ , a_1 masses	:	$M_\rho = M_{a_1} = 3.9$ TeV
Techni-glueball (TG) mass	:	$M_G = 18$ TeV
TG decay constant	:	$F_G = 174$ TeV
dynamical TF mass m_F	:	$m_F = 0.85$ TeV

W/ Tevatron data included:



W/ Tevatron data included:



Farhi et al (1981)

One-doublet model (1DM)

TF_{EW}	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$
$\begin{pmatrix} U \\ D \end{pmatrix}_L$	1	2	0
U_R	1	1	1/2
D_R	1	1	-1/2

One-family model (1FM)

TF_{EW}	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$
$Q_L = \begin{pmatrix} U \\ D \end{pmatrix}_L$	3	2	1/6
$L_L = \begin{pmatrix} N \\ E \end{pmatrix}_L$	1	2	-1/2
U_R	3	1	2/3
D_R	3	1	-1/3
N_R	1	1	0
E_R	1	1	-1

Total # of techni-fermions

$$N_{TF} = (N_{TF})_{EW-singlet} + 2N_D$$

w/ critical # for mass generation
in WTC

$$N_{TF} \simeq 4N_{TC}$$

Appelquist et al (1996)

★ Other pheno. issues in TC scenarios

S parameter

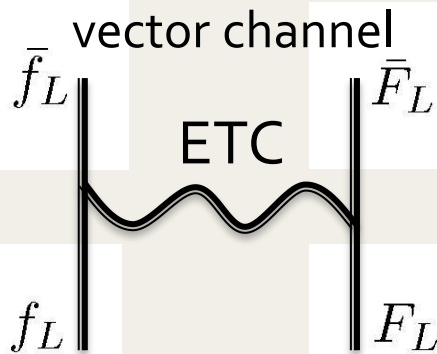
$$S \approx N_D \cdot \frac{8\pi F^2}{M_\rho^2} \simeq \underline{0.3 \cdot N_D} \quad (\text{for QCD-like})$$

N_D : # EW doublets

too large! Cf: $S(\text{exp}) < 0.1$ around $T=0$

One resolution: *ETC-induced "delocalization" operator*

Chivukula et al (2005)



$$-\frac{1}{\Lambda_{\text{ETC}}^2} J_{\mu\text{SM}_L}^a J_{\text{TC}_L}^{\mu a}$$

in low-energy

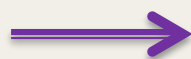
$$J_{\text{TC}_L}^{\mu a} \rightarrow \text{Tr}[U^\dagger \frac{\sigma^a}{2} iD^\mu U]$$

$$\text{w/ } U = e^{2i\pi_{\text{eaten}}/v_{\text{EW}}}$$

$$\ni g_W W_\mu - g_Y B_\mu$$

modifies SM f-couplings to W, Z

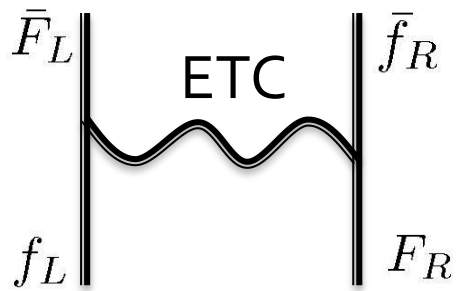
contributes to S "negatively"



$$\Delta S \sim \ominus \frac{8\pi}{g_W^2} \left(\frac{v_{\text{EW}}}{\Lambda_{\text{ETC}}} \right)^2$$

$$S_{\text{total}} \rightarrow 0 \text{ ("ideal delocalization")}$$

Top quark mass generation



$$m_t \approx \frac{\langle \bar{U}U \rangle_{\text{ETC}}}{\Lambda_{\text{ETC}}^2} \approx \left(\frac{\Lambda_{\text{TC}}}{\Lambda_{\text{ETC}}} \right)^2 \Lambda_{\text{TC}}$$

ETC scale associated w/ top mass

$$\Lambda_{\text{ETC}}^{\text{top}} \approx 1\text{TeV} \left(\frac{\Lambda_{\text{TC}}}{1\text{TeV}} \right)^{3/2} \left(\frac{172\text{GeV}}{m_t} \right)^{1/2}$$

too small!

One resolution: **Strong ETC** Miransky et al (1989)

--- makes induced 4-fermi (tt UU) coupling large enough to trigger chiral symm. breaking (almost by NJL dynamics)

$$\langle \bar{U}U \rangle_{\text{ETC}} \approx \left(\frac{\Lambda_{\text{ETC}}}{\Lambda_{\text{TC}}} \right)^{\gamma_m} \langle \bar{U}U \rangle_{\text{TC}} \quad 1 < \gamma_m \leq 2$$

boost-up



$$m_t \approx \left(\frac{\Lambda_{\text{TC}}}{\Lambda_{\text{ETC}}} \right)^{2-\gamma_m} \Lambda_{\text{TC}} \leq \Lambda_{\text{TC}} \sim 1\text{TeV}$$

T parameter (Strong) ETC generates large isospin breaking
 → highly model-dependent issue

★ Direct consequences of Ward-Takahashi identities

S.M. and K. Yamawaki, PRD86 (2012)

* Coupling to techni-fermions

$$\begin{aligned} \lim_{q_\mu \rightarrow 0} \int d^4 y e^{iqy} \langle 0 | T \partial^\mu D_\mu(y) F(x) \bar{F}(0) | 0 \rangle &= i \delta_D \langle 0 | T F(x) \bar{F}(0) | 0 \rangle \\ &= i (2d_F + x^\nu \partial_\nu) \langle 0 | T F(x) \bar{F}(0) | 0 \rangle \end{aligned}$$

Dilaton pole dominance

$$F_\phi \cdot \langle \phi(q=0) | T F(x) \bar{F}(0) | 0 \rangle = \delta_D \langle 0 | T F(x) \bar{F}(0) | 0 \rangle.$$

w/ TD decay constant F_ϕ

$$\langle 0 | D_\mu(x) | \phi(q) \rangle = -i F_\phi q_\mu e^{-iqx}$$

Yukawa vertex func.

$$\chi_{\phi FF}(p, q=0) = \frac{1}{F_\phi} \delta_D S_F^{-1}(p) = \frac{1}{F_\phi} \left(1 - p_\mu \frac{\partial}{\partial p_\mu} \right) S_F^{-1}(p)$$

* Couplings to SM fermions

No direct coupling TC

$$\langle f(p) | \theta_\mu^\mu(0) | f(p) \rangle = 0.$$

~~transform~~

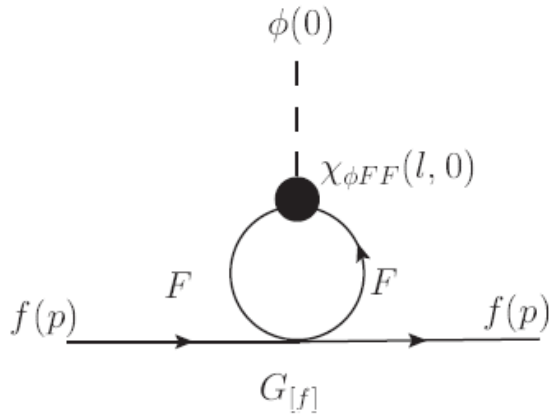
Techni-fermion loop induces

$$-\frac{iG_{[f]}}{F_\phi} \int \frac{d^4l}{(2\pi)^4} \text{Tr}[S_F(l) \cdot \delta_D S_F^{-1}(l) \cdot S_F(l)]$$

$$= \frac{iG_{[f]}}{F_\phi} \cdot \delta_D \int \frac{d^4l}{(2\pi)^4} \text{Tr}[S_F(l)]$$

$$= -i \frac{G_{[f]}}{F_\phi} \delta_D \langle \bar{F} F \rangle$$

$$\delta_D \langle \bar{F} F \rangle = (3 - \gamma_m) \langle \bar{F} F \rangle$$



ETC induced
4-fermi

$$\mathcal{L}_{\text{ETC}}^{\text{eff}} = G_{[f]} \bar{F} F \bar{f} f$$

f-fermion mass:

$$m_f = -G_{[f]} \langle \bar{F} F \rangle$$

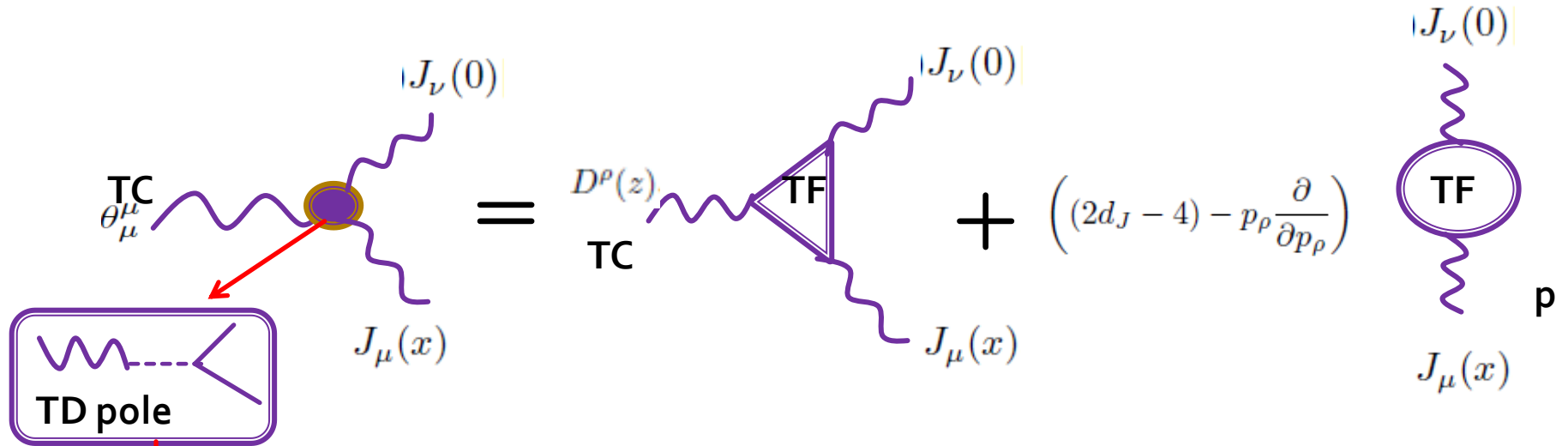
Yukawa coupling to SM-fermion

$$g_{\phi f f} = \frac{(3 - \gamma_m) m_f}{F_\phi}$$

* Couplings to SM gauge bosons

WT identity \rightarrow scale anomaly term + anomaly-free term

$$\lim_{q_\rho \rightarrow 0} \int d^4 z e^{iqz} \langle 0 | T \partial_\rho D^\rho(z) J_\mu(x) J_\nu(0) | 0 \rangle = \lim_{q_\rho \rightarrow 0} \left(-iq_\rho \int d^4 z e^{iqz} \langle 0 | T D^\rho(z) J_\mu(x) J_\nu(0) | 0 \rangle + i\delta_D \langle 0 | T J_\mu(x) J_\nu(0) | 0 \rangle \right)$$



The loop integrals are actually saturated by **IR contributions** ($\gamma_m = 2$)

$$ig_W^2 \text{F.T.} \langle \phi(0) | T J_L^{\mu a}(x) J_L^{\nu b}(0) | 0 \rangle = \frac{2\beta_F(g)}{F_\phi g^3} (p^2 g_{\mu\nu} - p_\mu p_\nu) \quad \beta_F: \text{TF-loop contribution to beta function}$$

$$+ \frac{2i}{F_\phi} \left(g_{\mu\nu} - \frac{p_\mu p_\nu}{p^2} \right) [\Pi_{LL}(0) + \mathcal{O}(p^4 \Pi''(0))]$$

$$ig_W^2 \text{F.T.} \langle \phi(0) | T J_L^{\mu a}(x) J_L^{\nu b}(0) | 0 \rangle = \frac{2\beta_F(g)}{F_\phi g^3} (p^2 g_{\mu\nu} - p_\mu p_\nu) + \frac{2i}{F_\phi} \left(g_{\mu\nu} - \frac{p_\mu p_\nu}{p^2} \right) [\Pi_{LL}(0) + \mathcal{O}(p^4 \Pi''(0))]$$

β_F: TF-loop contribution to beta function

* For SU(2)W gauge bosons: W –“broken” currents

$$\Pi_{LL}(0) = N_D \frac{F_\pi^2}{4} = \frac{v_{EW}^2}{4}$$

N_D = TF -EW-doublets

Coupling to W

$$\mathcal{L}_{\phi WW} = \frac{2m_W^2}{F_\phi} \phi W_\mu^a W^{\mu a}$$

* For unbroken currents coupled to photon, gluon:

$$\Pi(0) = 0.$$

Coupling to γγ & gluons

$$\mathcal{L}_{\phi\gamma\gamma,gg} = \frac{\phi}{F_\phi} \left[\frac{\beta_F(e)}{2e^3} F_{\mu\nu}^2 + \frac{\beta_F(g_s)}{2g_s^3} G_{\mu\nu}^2 \right]$$