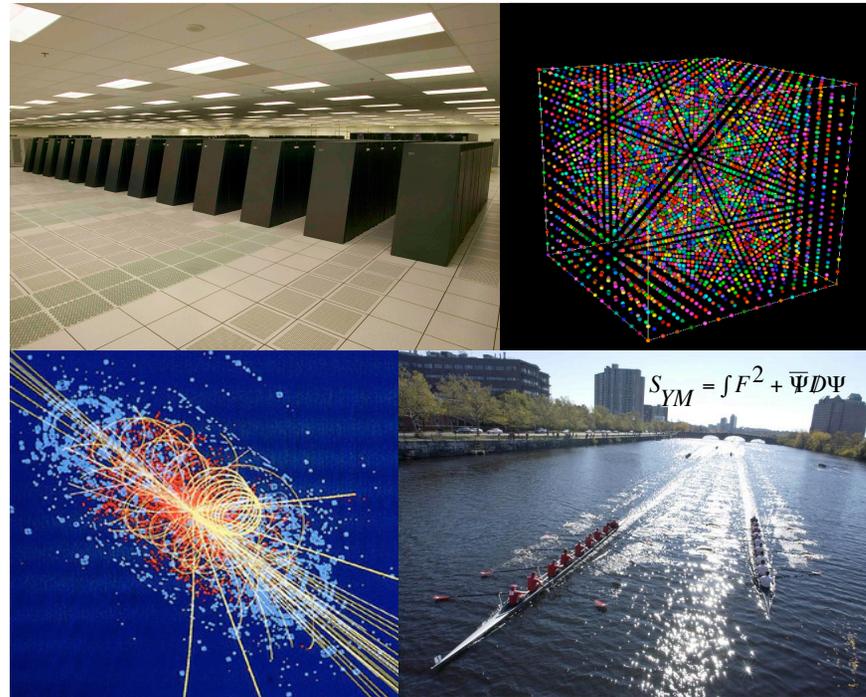


# Latest results from the LSD collaboration

**Pavlos Vranas for the LSD collaboration**

# The Lattice Strong Dynamics collaboration

T. Appelquist (Yale U.),  
A. Avakian (Boston U.)  
R. Babich (Boston U.),  
R. Brower (Boston U.),  
M. Cheng (LLNL),  
M. Clark (Harvard U.),  
S. Cohen (Jlab, BU),  
G. Fleming (Yale U.),  
J. Kiskis (UCD),  
M. Lin (Yale),  
E. Neil (Yale U.),  
J. Osborn (ANL),  
C. Rebbi (Boston U.),  
D. Schaich (Boston U.),  
R. Soltz (LLNL),  
P. Vranas (LLNL).



# LHC

## TeV physics



# Our first thoughts

- ◆ TC and ETC models can use lattice non-perturbative input.
- ◆ How do the properties of gauge theory change with  $N_f$ ,  $N_C$  and  $R$  ?

- ★ Chiral condensate enhancement  $\frac{\langle \bar{\psi}\psi \rangle}{F^3}$
- ★ S parameter
- ★ Particle spectrum
- ★ Dirac operator eigenvalue spectrum

**How should we proceed?**

# A slice of ETC



**M = many TeV**

**Lattice cutoff (1/a)**

**Gauge Theory**

**TeV**

**Confinement  
TC Hadrons**

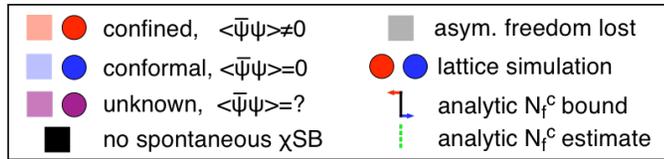
# Choices

- ⌘ ETC is complicated enough:  
**stay with fundamental reps**
- ⌘ Start from something we know:  
**lattice QCD -- SU(3) color**
- ⌘ Move slowly away from QCD and not too close to  $N_{fc}$ :  
**first do 6 flavors**
- ⌘ Chiral and flavor symmetries are crucial:  
**use DWF**
- ⌘ To be able to observe enhancement:  
**use large cutoff (small  $a$ )**
- ⌘ To be able to make direct comparisons:  
**Do a 2-flavor simulation at the same cutoff**

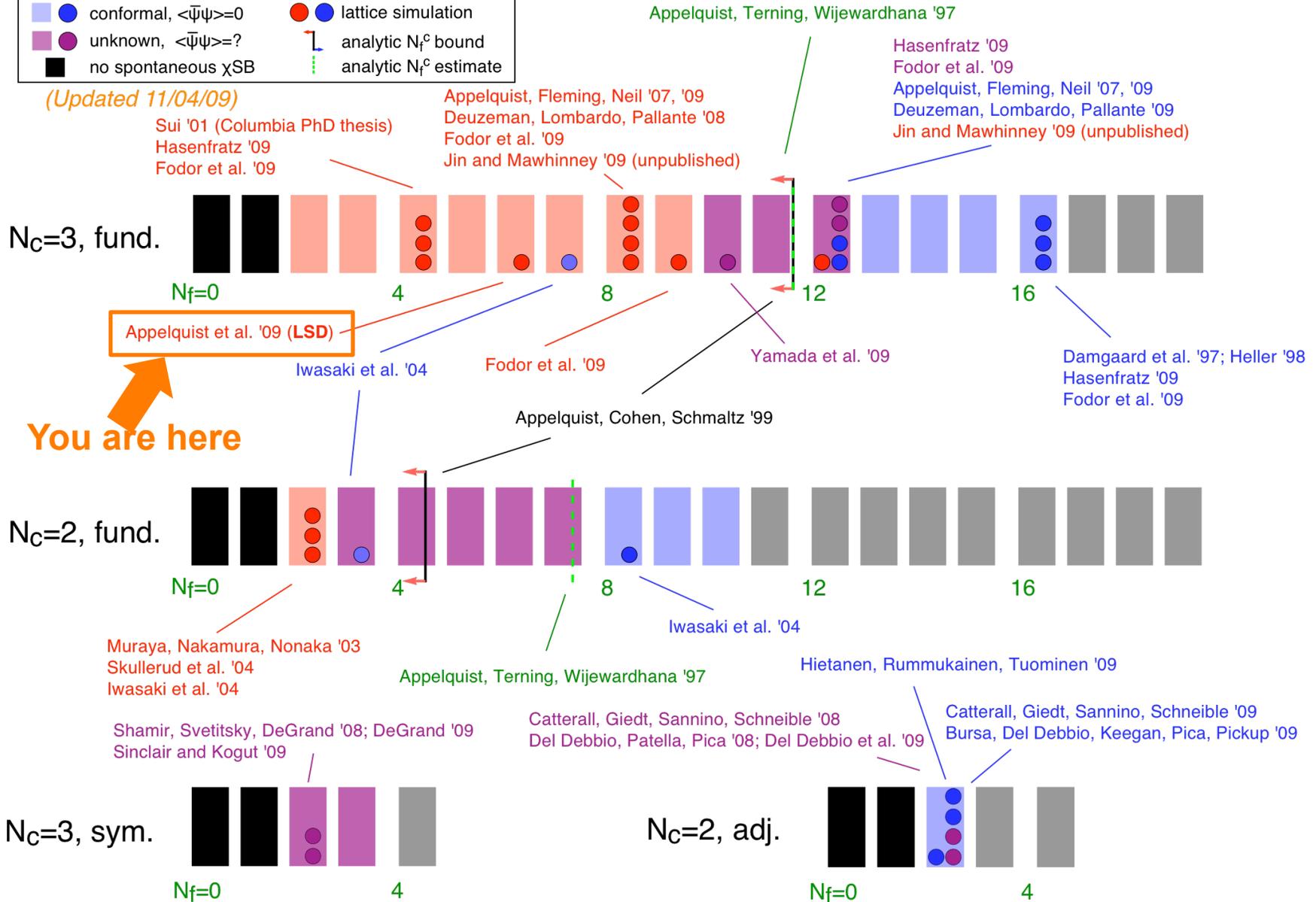
# Higher demands

- ❑ Computing cost increases as  $N_f^{3/2}$
- ❑ The lattice must have cutoff much larger than the confinement scale to take advantage of slower running. Larger lattice needed as we approach the IRFP.
- ❑ We do not know the answer

# Current landscape



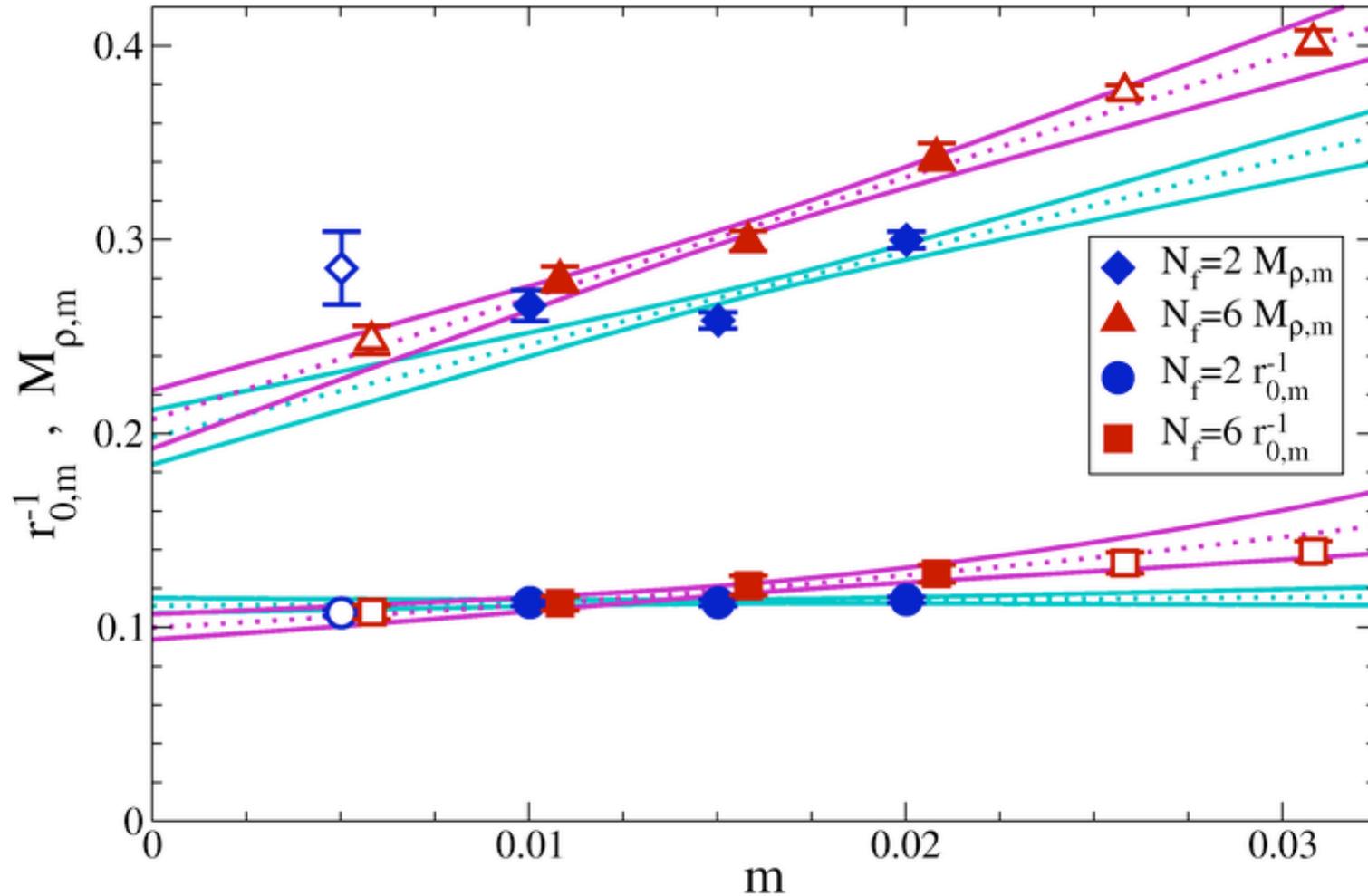
(Updated 11/04/09)



# Simulations

- ★ Lattice Volume is  $32^3 \times 64$
- ★ Iwasaki gauge action with DWF at  $L_s = 16$
- ★ Input fermion masses  $m_f = 0.005$  to  $0.03$
- ★  $m_{\text{res}} \sim 8 \times 10^{-4}$  (6f),  $3 \times 10^{-5}$  (2f)  $\rightarrow m = m_f + m_{\text{res}}$
- ★  $M_m L > 4$
- ★ HMC, multi-level symplectic integrator  
mass preconditioning  
chronological inversion  
CPS
- ★ 6-flavor  $\beta = 2.1 \leftrightarrow$  2-flavor  $\beta = 2.7$
- ★ About 1,000 configurations per point

# Scales



Reasonable distance from cutoff with  $M_{\rho} \sim \text{cutoff} / 5$

# Chiral perturbation theory

$$M_m^2 = \frac{2m\langle\bar{\psi}\psi\rangle}{F^2} \left\{ 1 + zm \left[ \alpha_M + \frac{1}{N_f} \log(zm) \right] \right\}$$

$$F_m = F \left\{ 1 + zm \left[ \alpha_F - \frac{N_f}{2} \log(zm) \right] \right\}$$

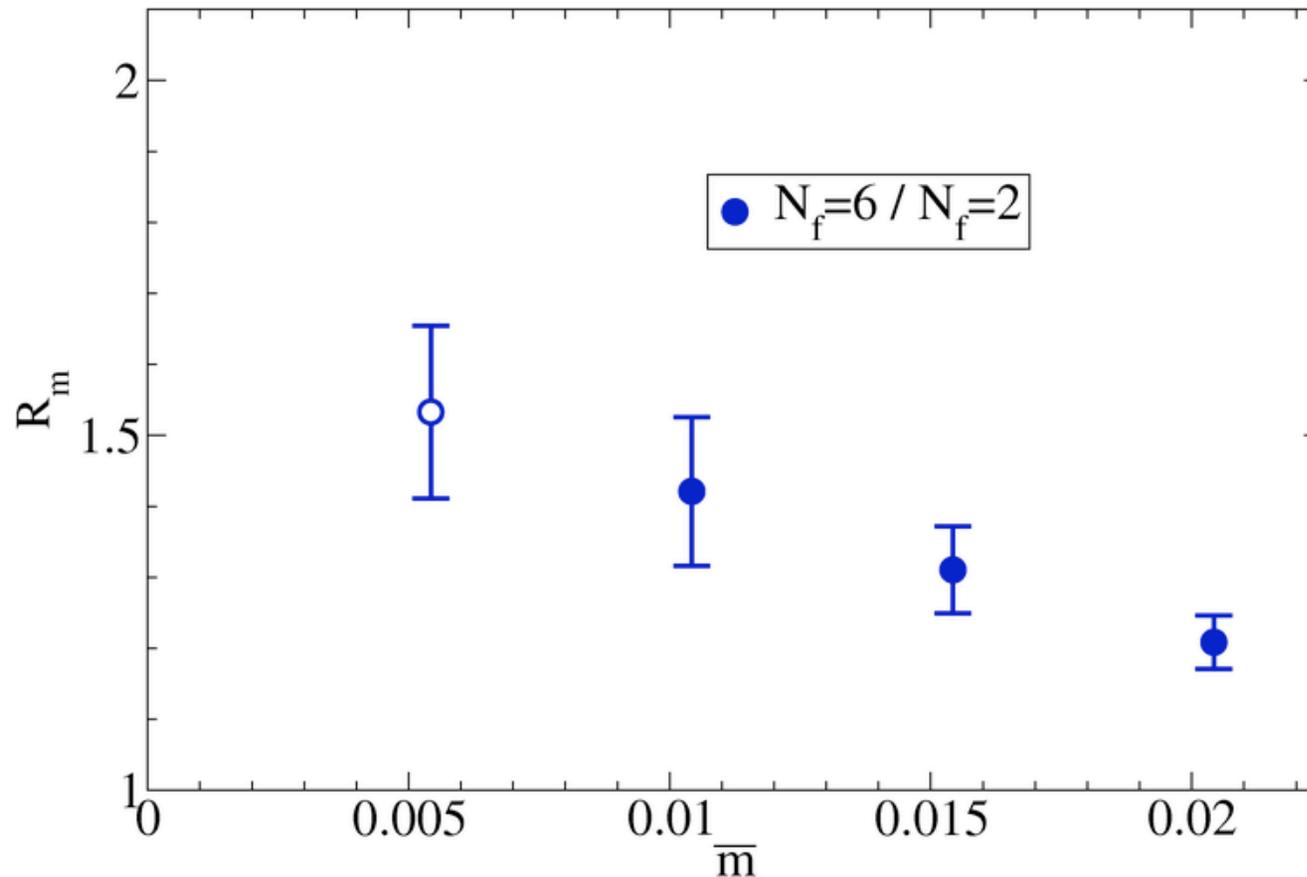
$$\langle\bar{\psi}\psi\rangle_m = \langle\bar{\psi}\psi\rangle \left\{ 1 + zm \left[ \alpha_C - \frac{N_f^2 - 1}{N_f} \log(zm) \right] \right\}$$

★ Log coefficients of  $F_m, \langle\bar{\psi}\psi\rangle_m \sim N_f$

★  $\alpha_C \sim 1/a^2 \rightarrow \langle\bar{\psi}\psi\rangle_m$  difficult to measure

★ Instead measure (GMOR)  $\frac{M_m^2}{2mF_m} \rightarrow \frac{\langle\bar{\psi}\psi\rangle}{F^3}$  at  $m \rightarrow 0$

# 6-flavor vs. 2-flavor enhancement

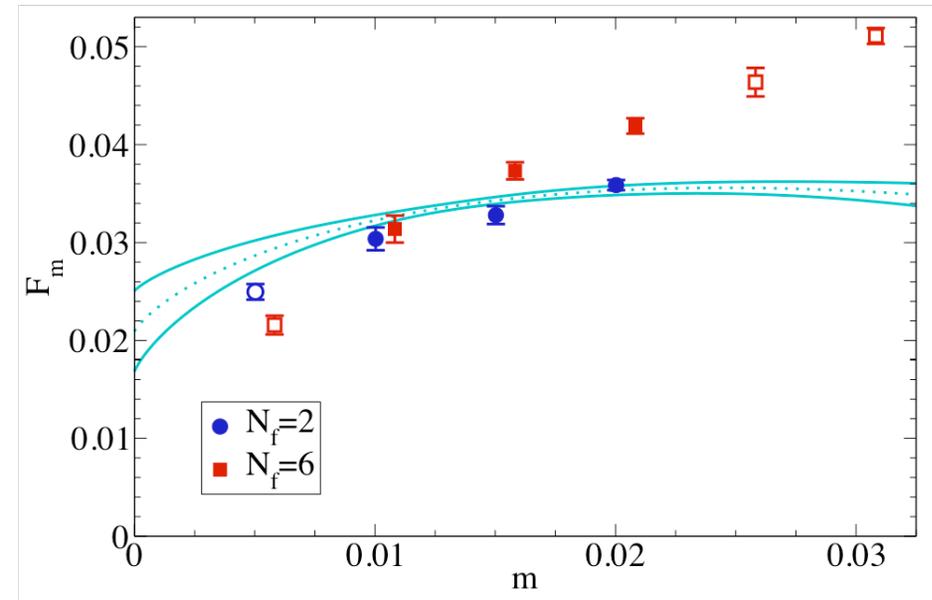
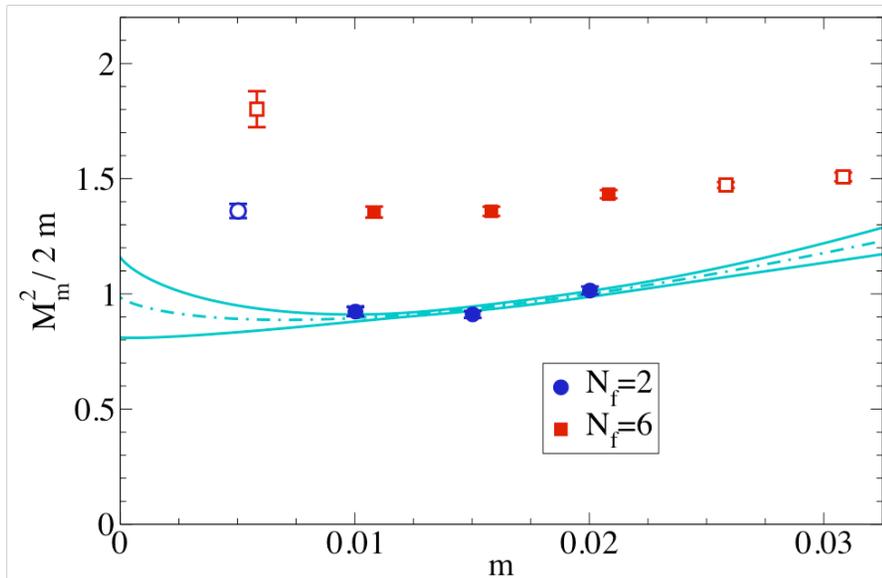


★  $R_m = [M_m^2 / 2mF_m]_{6f} / [M_m^2 / 2mF_m]_{2f}$

★ Can compare directly 6f to 2f because they have same cutoff

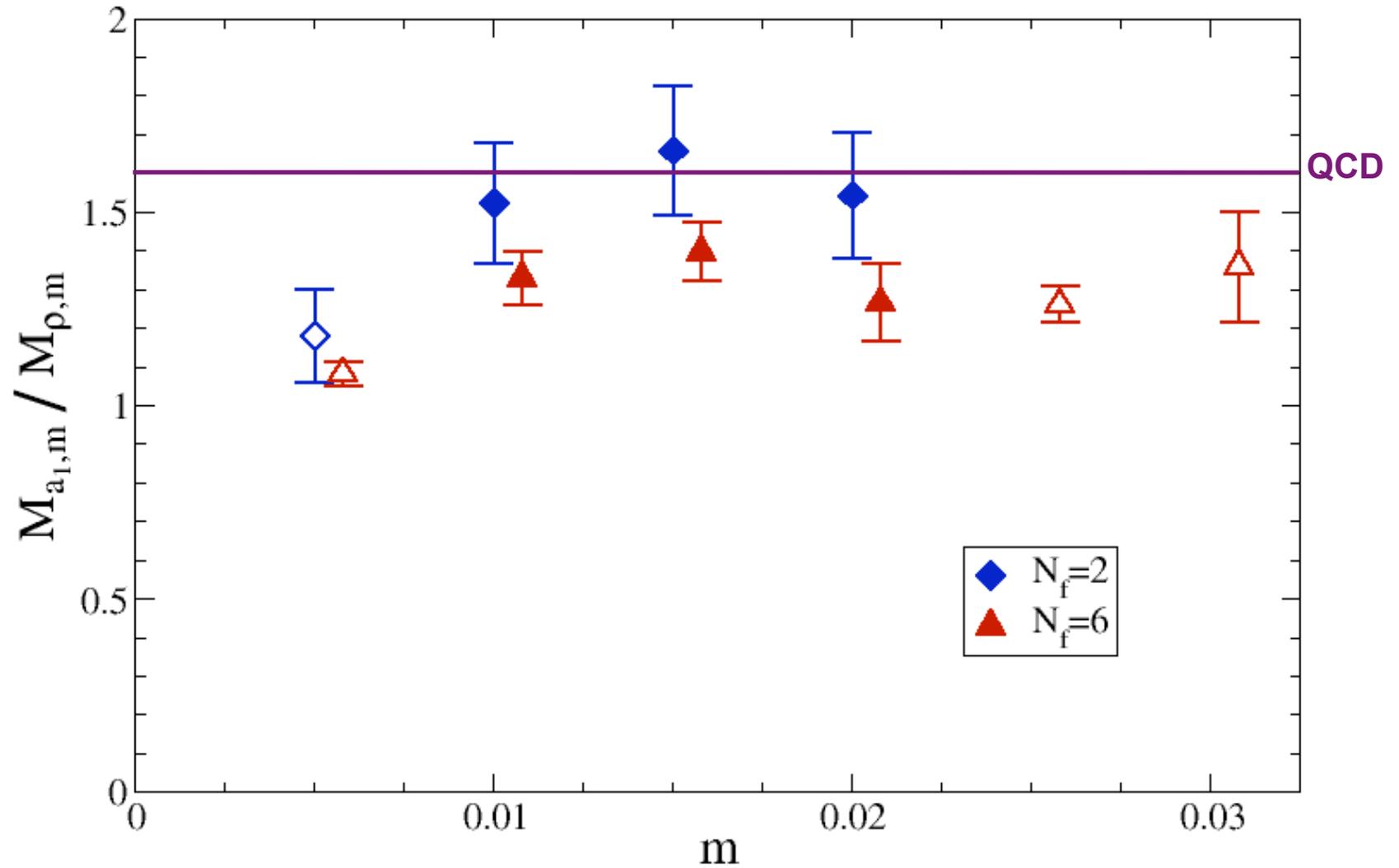
★ Observing ~ **50% enhancement**

# xPT fits and bound

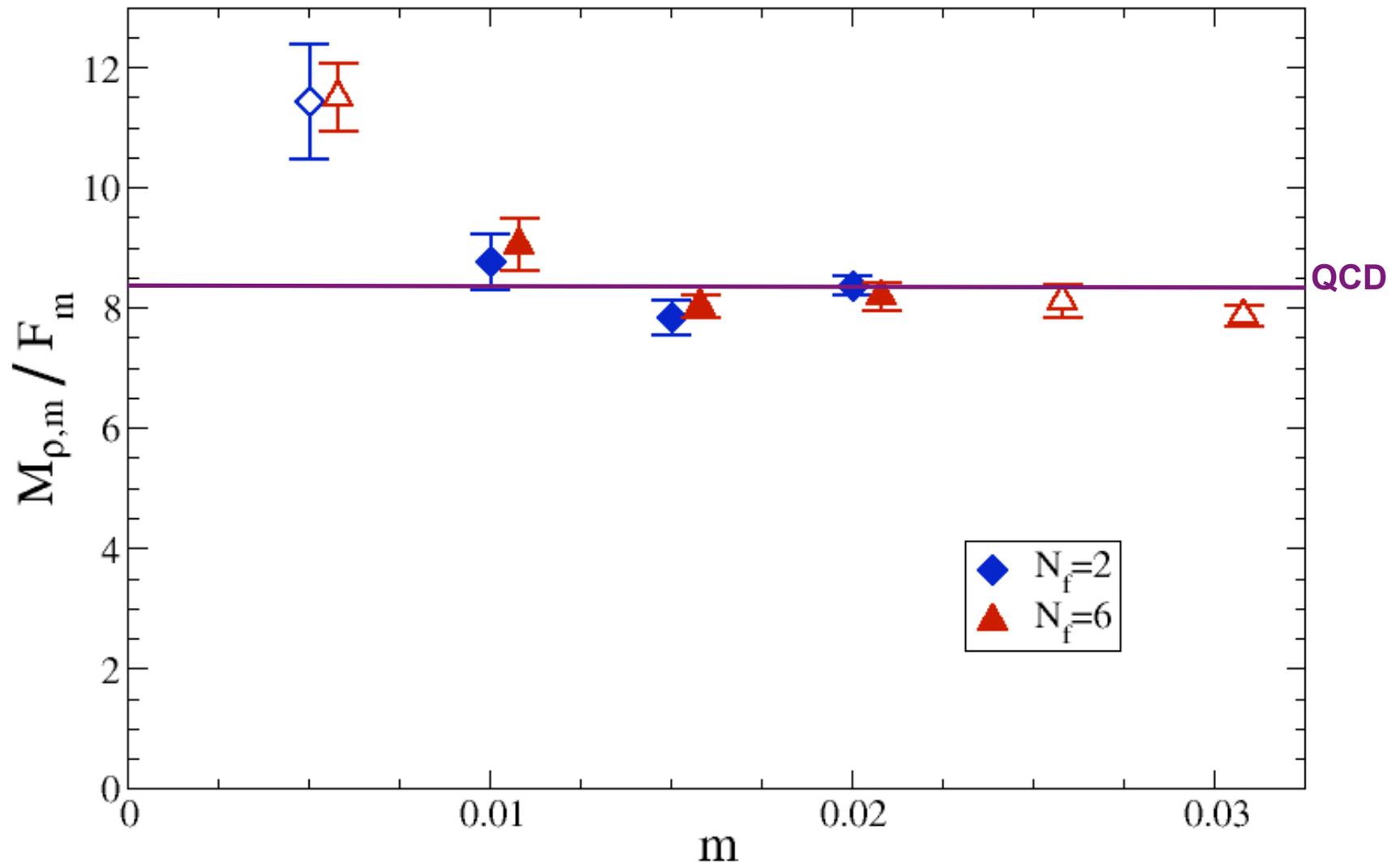


- ★ 2f give a reasonable combined fit for  $M_m^2/2m$ ,  $F_m$ ,  $\langle\bar{\psi}\psi\rangle_m$
- ★ 2f agree with phenomenology:  $\langle\bar{\psi}\psi\rangle/F^3 = 47.1(17.6)_{\text{latt}} = 36.2(6.5)_{\overline{\text{MS}}}$
- ★ 6f because of larger slope need smaller masses ( $\rightarrow$  larger lattices)
- ★ Linear fits on the 6-flavor data give a bound:  
 28% increase:  $[ = 47.1(17.6)]_{2f} [ > 60.0(8.0)]_{6f}$   
 absence of enhancement excluded at 73% confidence level

# Hadron spectrum



# Hadron spectrum

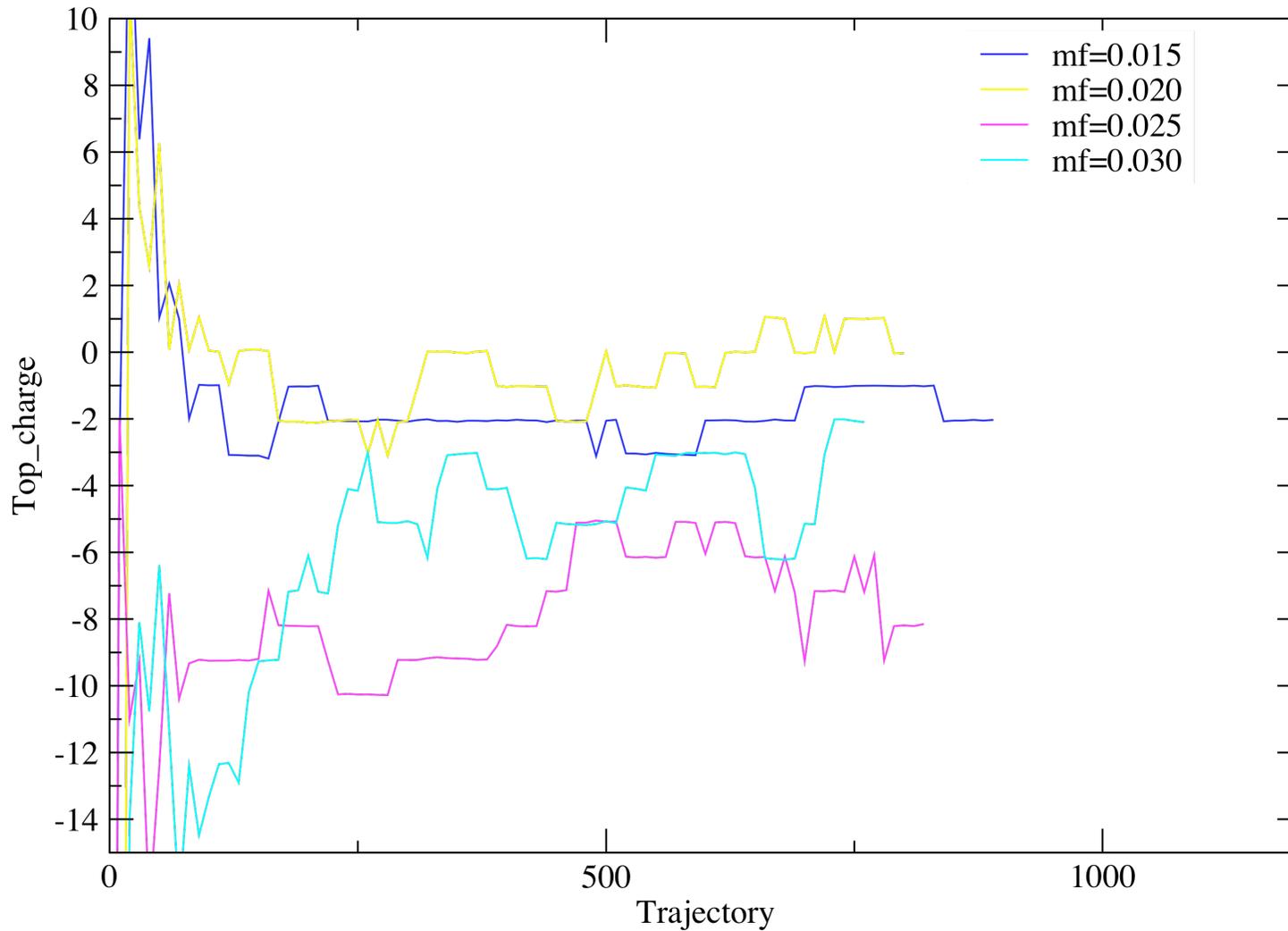


# Salient features: Topology

- ⌘ At small lattice spacing the barriers between TC sectors are large
- ⌘ At small  $m$  DWF HMC encounter barriers in changing global topology  $Q$
- ⌘ At large volume  $Q$  is irrelevant but for us it is a finite size effect
- ⌘ For  $0.01 \leq m$ ,  $Q$  evolves sufficiently: for  $m = 0.005$  it does not

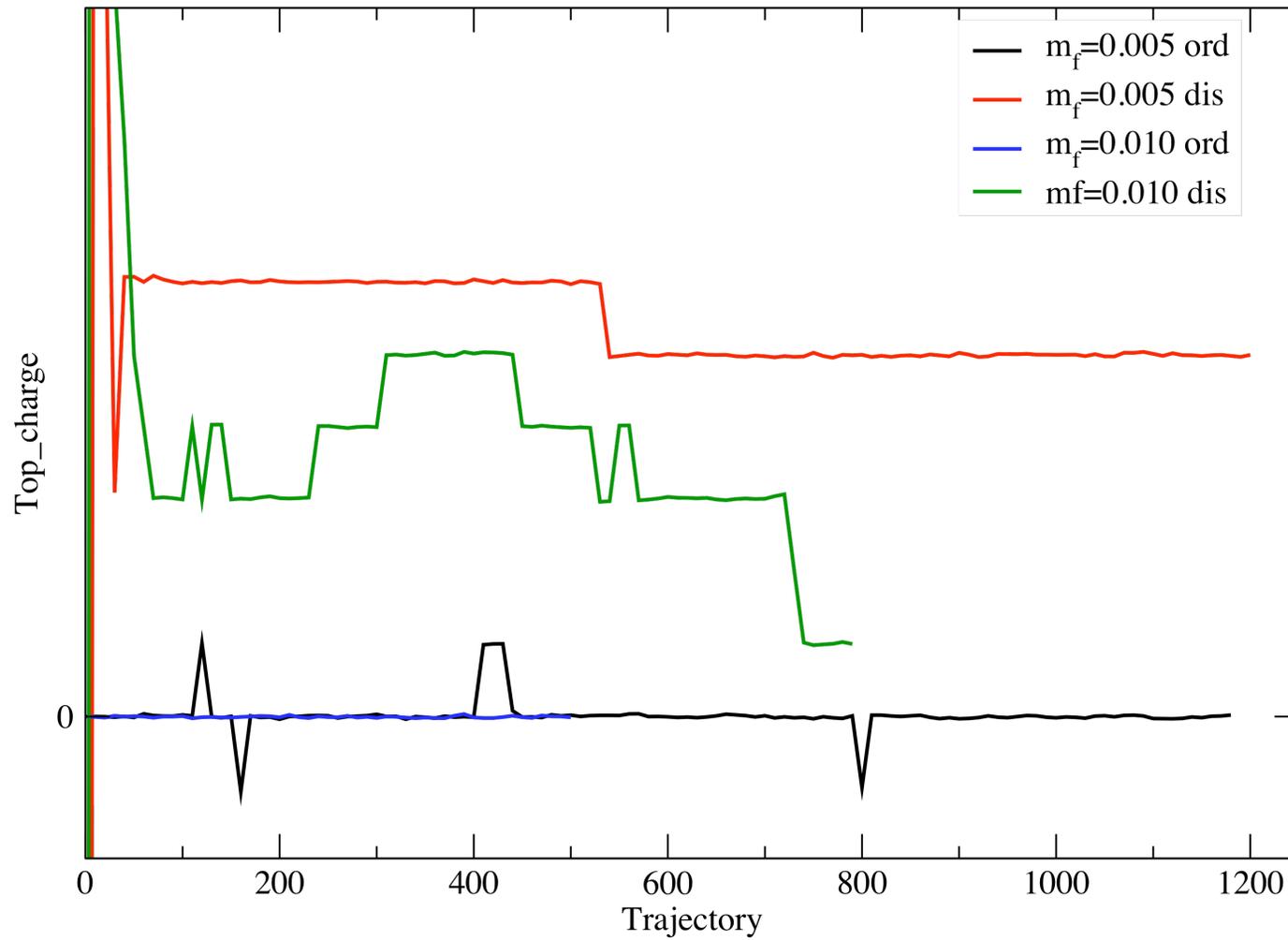
# Topology (preliminary)

6 flavors, beta = 2.10 topological charge



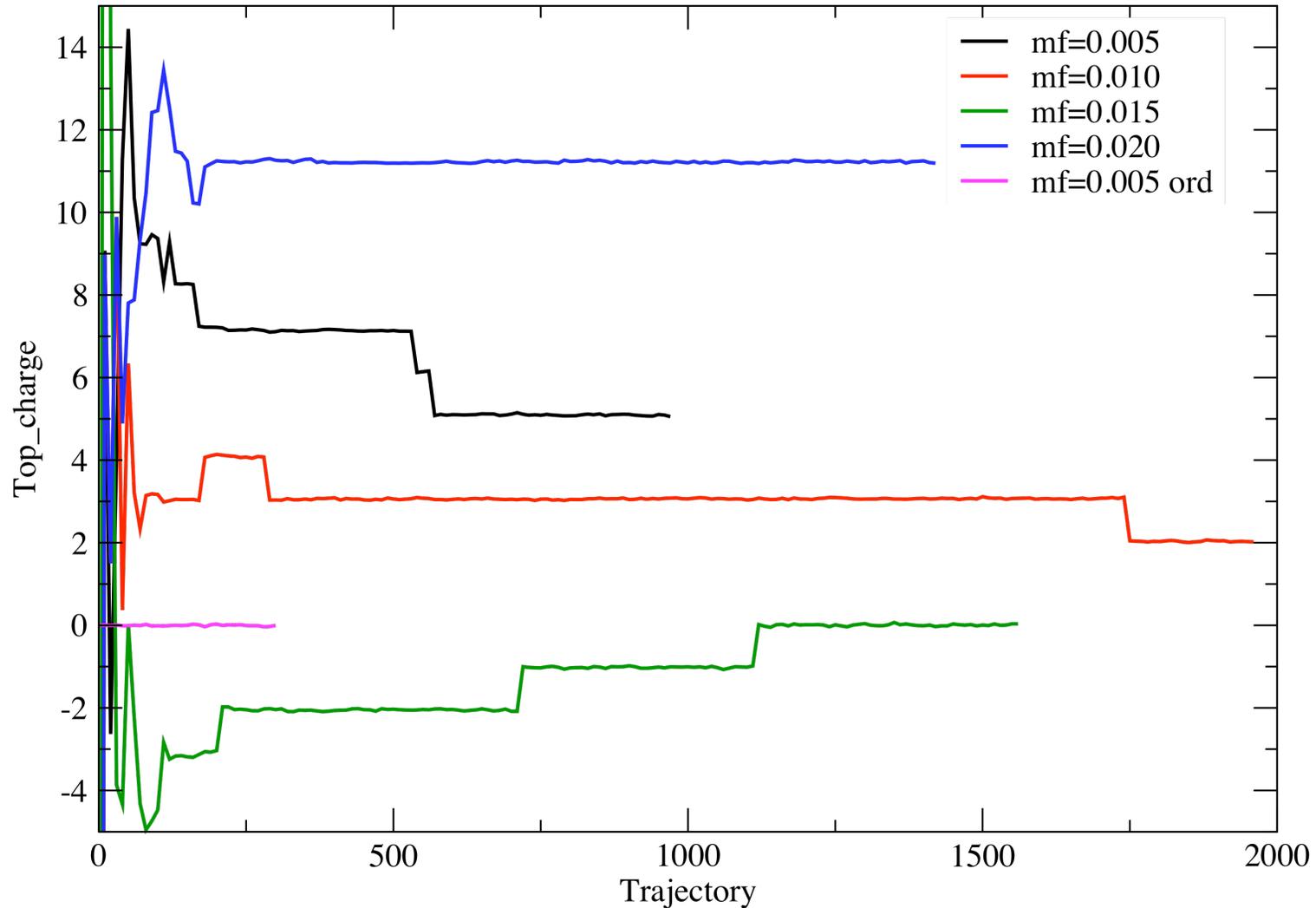
# Topology (preliminary)

6 flavors, beta = 2.10 topological charge



# Topology (preliminary)

2 flavors, beta = 2.70 topological charge



# 150 million core hours on LLNL BG/L



# Near term LSD plans

- ★ **9-flavors  $SU(3)_c$  fundamental at the same lattice spacing**
- ★ **Measure S at 2, 6 and 9 flavors**
- ★ **Measure Dirac spectrum at 2, 6 and 9 flavors**
- ★ **Fundamental  $SU(2)_c$**

# Conclusions

- ⌘ **2 and 6 flavors  $SU(3)_c$  fundamental at same lattice spacing**
- ⌘ **Condensate enhancement larger than 50%**  
**Excluded no-enhancement at 73% confidence level**
- ⌘ **Hadron spectrum deviations**