

CONFINEMENT AND DUALITY IN QCD

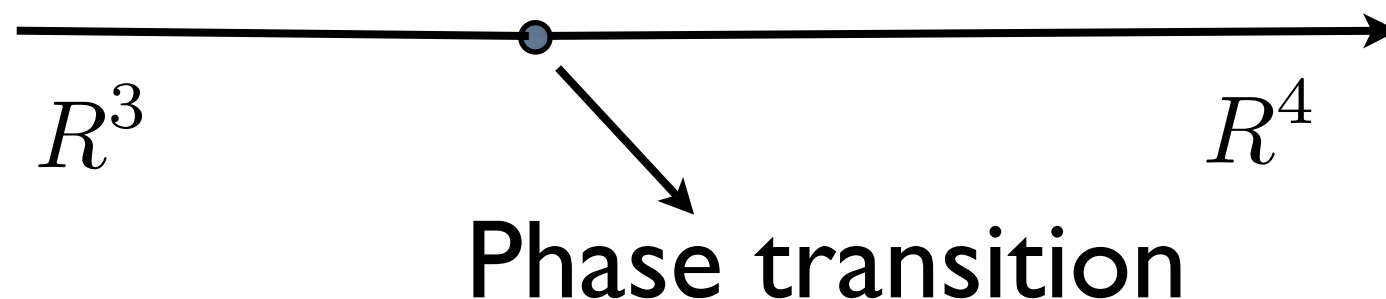
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(SLAC)

Large N parts in collaboration with
L.G.Yaffe,

Finite N , with M.Shifman

- Are there any QCD-like gauge theories which are analytically tractable in 4d?
- Meaning of the question? (like Polyakov model on R^3 or Seiberg-Witten)
- pure YM, Vector-like, chiral ? Obvious answer: No!
- Strong coupling gauge dynamics may also be relevant to (multi)-TeV scale physics.

Thermal vs nonthermal QCD on $\mathcal{R}^3 \times S^1$



- Thermal versus quantum fluctuations.
- Non-thermal compactifications: not all QCD-like theories alike.
- QCD(adj) with periodic spin connection. Center symmetry **never** breaks! (complex reps, not so.)

- QCD(adj) is solvable on small circle (in the same sense as SW or Polyakov model.)
- Exhibits (linear) confinement without continuous chiral symmetry breaking on small circle. Discrete chiral symmetry is always broken.
- There must exist a non-thermal chiral transition in the absence of **any** change in center symmetry realization!
- Massless fermions at small circle, massless Goldstone bosons at large!

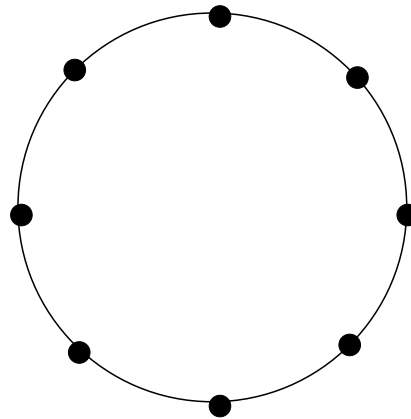
QCD(adj)

$$S = \int_{R^3 \times S^1} \frac{1}{g^2} \text{tr} \left[\frac{1}{4} F_{MN}^2 + i \bar{\lambda}^I \bar{\sigma}^M D_M \lambda_I \right] \quad \text{short distance}$$

Center Z_{N_c}

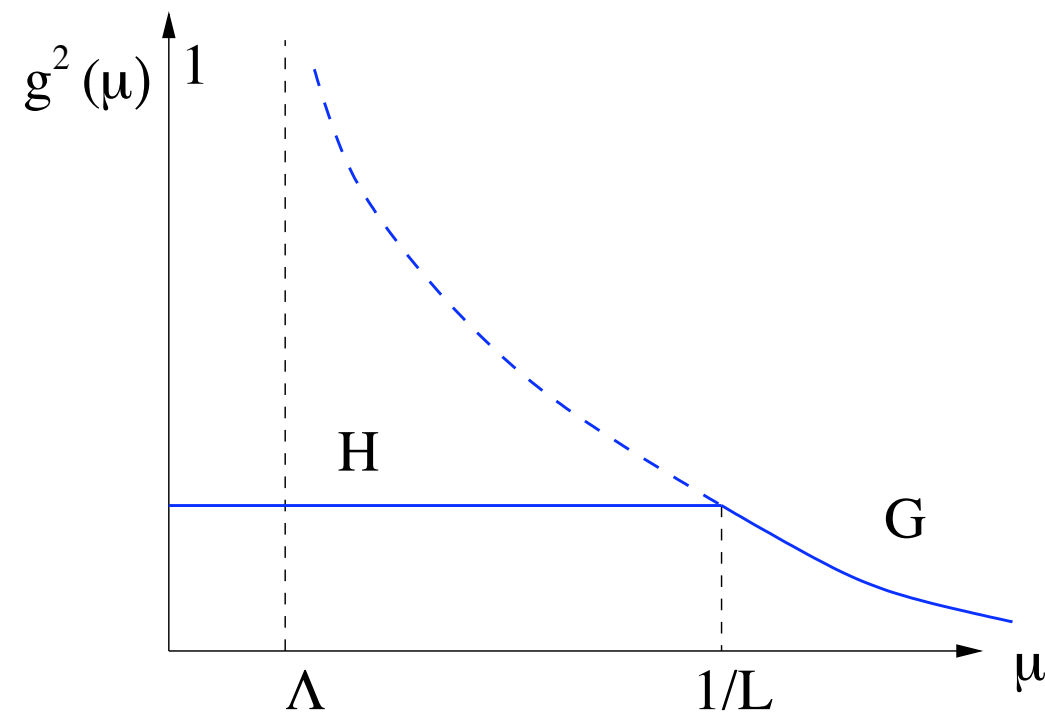
Chiral $(SU(n_f) \times Z_{2N_c n_f}) / Z_{n_f}$

Evaluate the one loop effective potential for the Wilson line.
Eigenvalues repel. Minimum at



At weak coupling, the fluctuations are frozen “Higgs regime”

Perturbation theory



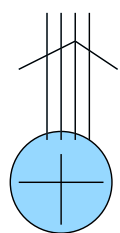
$$G = SU(2), \quad H = U(1)$$

IR in perturbation theory is a free theory of fermions and “photons”. Is this perturbative fixed point destabilized non-perturbatively?

$$\left(\int_{S^2} F, \int_{R^3 \times S^1} F \tilde{F} \right)$$

Magnetic Monopoles

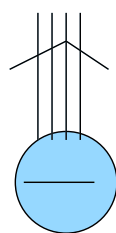
Magnetic Bions



BPS

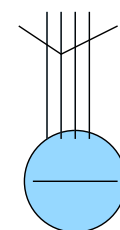
$(1, 1/2)$

$$e^{-S_0} e^{i\sigma} \det_{I,J} \psi^I \psi^J,$$



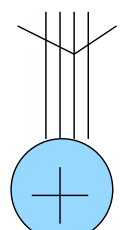
KK

$(-1, 1/2)$



$\overline{\text{BPS}}$

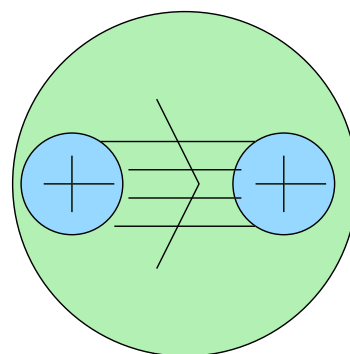
$(-1, -1/2)$



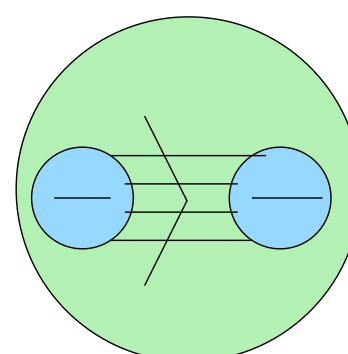
$\overline{\text{KK}}$

$(1, -1/2)$

$$e^{-S_0} e^{i\sigma} \det_{I,J} \bar{\psi}^I \bar{\psi}^J$$



$(2,0)$




$(-2, 0)$


$$e^{-2S_0} (e^{2i\sigma} + e^{-2i\sigma})$$

Discrete shift symmetry : $\sigma \rightarrow \sigma + \pi$

$$L^{\text{dQCD}} = \frac{1}{2}(\partial\sigma)^2 - b e^{-2S_0} \cos 2\sigma + i\bar{\psi}^I \gamma_\mu \partial_\mu \psi_I + c e^{-S_0} \cos \sigma (\det_{I,J} \psi^I \psi^J + \text{c.c.})$$



magnetic bions



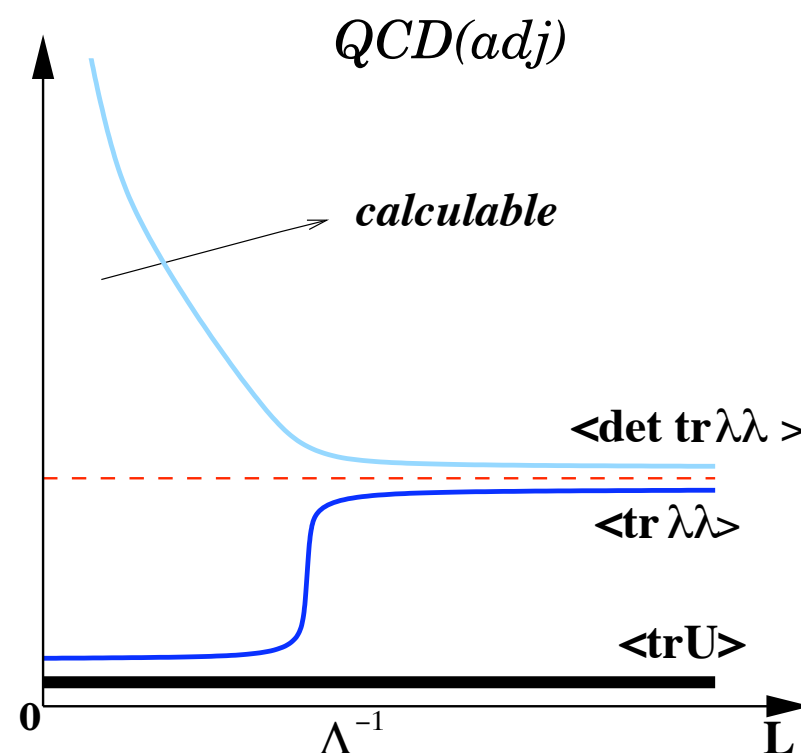
magnetic monopoles

Same mechanism in N=1 SYM, unrecognized previously. Beware of many erroneous statements in literature.

Important point in the solution of N=1 SYM is unbroken center symmetry,
not supersymmetry

[See Giedt's and Catterall's talks for progress in susy lattice formulations.]

- A) Mass gap in gauge sector due to magnetic bion mechanism, so is linear confinement, and stable flux tubes.
- B) Discrete chiral symmetry is always broken.
- C) Continuous chiral symmetry is unbroken at small radius.



Red line $N=1$ SYM.

Remark

- Not same as Polyakov model with massless adjoint fermions which neither confines, nor has a mass gap. The masslessness of the photon is protected by $U(1)$ shift symmetry. $U(1)$ breaks spontaneously, and photon is the Goldstone boson. (Affleck, Harvey, Witten 1982)
- Distinguishing notion between QCD(adj) and Polyakov model with massless fermions: discrete versus continuous topological symmetry. (Not explained in this talk.)

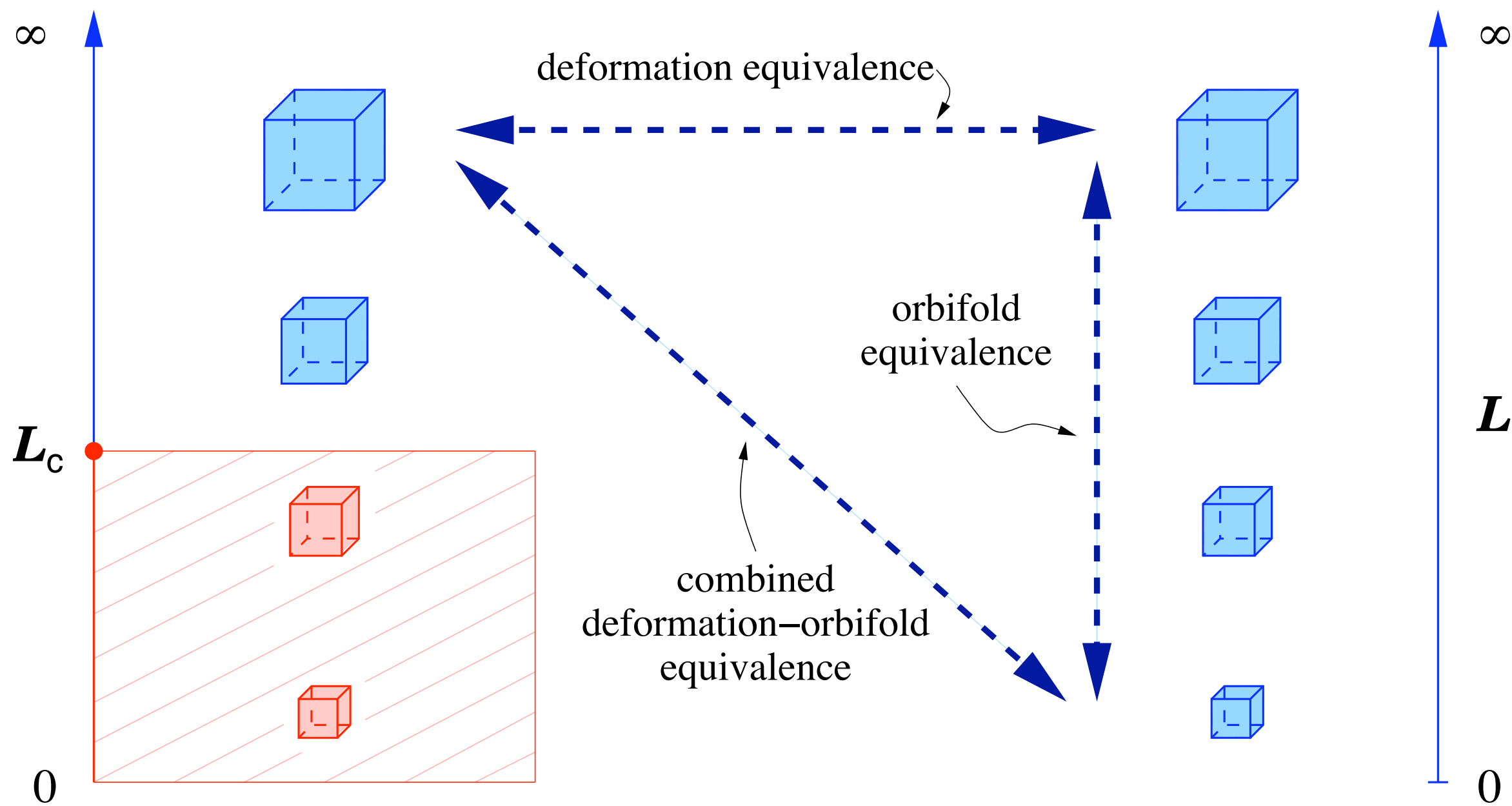
Region of validity of dual formulation

- $LN_c\Lambda \ll 1$, why not $L\Lambda \ll 1$?
- Separation of scales between W-bosons and dual photons.
- Deeper reason: Large N volume independence EK reduction
- The large N volume independence holds provided unbroken center symmetry. Thus, the chiral transition scale must move to arbitrarily small radius at large N.
- New dynamical scale in QCD: Λ^{-1}/N

- Complex representation fermions, chiral theories, pure YM? Center is **always** broken at small radius.
- **New idea:** Add center stabilizing double trace deformations. Different theory? Not so fast.

ordinary Yang–Mills

deformed Yang–Mills



At large N , the deformation is a new cure to the old EK problem, and is a useful tool for QCD-like theories (with Yaffe).

[See Barak Bringoltz's talk for progress in this direction.]

At finite N , (with Shifman): **Conjecture**: For the deformed theories with only discrete global symmetries, the physics of the theory at large and small radius are **smoothly** connected.

- Deformed theories, 1-flavor QCD* (F/BF/AS/S) and YM* are analytically tractable at small radius. Confinement, mass gap, discrete chiral symmetry breaking can be shown analytically.
- There are difficulties for complex rep fermions, since one has both electrically and magnetically charged relevant excitations in the IR. However, this is surmountable.
- Double trace deformations are also useful for a large class of chiral gauge theories. It is fair to say that our current knowledge of such theories is next to nothing. (in progress, with Shifman.)
- The dynamics of chiral theories are really bizarre (or unique), and we have some promising analytical results. (to appear.)