

Spinor–Vector Duality and Sterile Neutrinos in String Derived Models



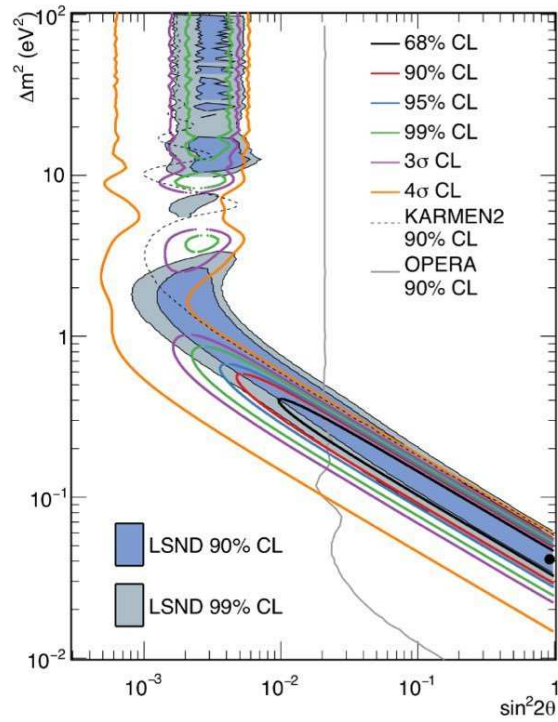
- Spinor–vector duality:

With: Costas Kounnas, John Rizos, Carlo Angelantonj, Mirian Tsulaia,
Ioannis Florakis, Thomas Mohaupt, Panos Athanasopoulos,
Doron Gepner

- Sterile neutrinos:

AEF, European Phys Journal C78 (2018) 867.

DISCRETE2018, Austrian Academy of Sciences, Vienna, 28 December 2018



LSND 1993: Evidence for sterile neutrinos

MiniBooNE 2018: Further evidence for sterile neutrinos

Sterile neutrinos in string vacua?

String Phenomenology: An answer in search of a question

The Answer : The Standard Model and its BSM extensions

A question : What is the true string vacuum?

A question : Can we identify signatures of classes of string compactifications in the experimental particle data?

In this talk:

Light sterile neutrinos in heterotic string vacua require a light Z'

A light Z' is hard to implement in heterotic string constructions

PHENOMENA

DATA → STANDARD MODEL

EWX → PERTUBATIVE

STANDARD MODEL → UNIFICATION

EVIDENCE: 16 of SO(10), Log running, proton stability, neutrino masses

+ GRAVITY < -- > STRINGS

PRIMARY GUIDES:

3 generations
SO(10) embedding

REALISTIC STRING MODELS :

heterotic 10D \rightarrow heterotic 4D

6D compactifications $(T^2 \times T^2 \times T^2)$

Orbifold – twists of flat 6D torus



FREE FERMIONIC MODELS –

$Z_2 \times Z_2$ Orbifold $\rightarrow U(1)_Y \in SO(10)$

$$\frac{6}{2} = 1+1+1$$

Realistic free fermionic models

'Phenomenology of the Standard Model and Unification'

- Minimal Superstring Standard Model NPB 335 (1990) 347
(with Nanopoulos & Yuan)
- Top quark mass $\sim 175\text{--}180\text{GeV}$ PLB 274 (1992) 47
- Generation mass hierarchy NPB 407 (1993) 57
- CKM mixing NPB 416 (1994) 63 (with Halyo)
- Stringy seesaw mechanism PLB 307 (1993) 311 (with Halyo)
- Gauge coupling unification NPB 457 (1995) 409 (with Dienes)
- Proton stability NPB 428 (1994) 111
- Squark degeneracy NPB 526 (1998) 21 (with Pati)
- Moduli fixing NPB 728 (2005) 83
- Classification & Exophobia 2003 – . . .
(with Nooij, Assel, Christodoulides, Kounnas, Rizos & Sonmez)

Other approaches

Geometrical

Greene, Kirklin, Miron, Ross (1987)

Donagi, Ovrut, Pantev, Waldram (1999)

Blumenhagen, Moster, Reinbacher, Weigand (2006)

Heckman, Vafa (2008)

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Orbifolds

Ibanez, Nilles, Quevedo (1987)

Bailin, Love, Thomas (1987)

Kobayashi, Raby, Zhang (2004)

Lebedev, Nilles, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter (2007)

Blaszczyk, Groot-Nibbelink, Ruehle, Trapletti, Vaudrevange (2010)

.....

Other CFTs

Gepner (1987)

Schellekens, Yankielowicz (1989)

Gato-Rivera, Schellekens (2009)

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Orientifolds

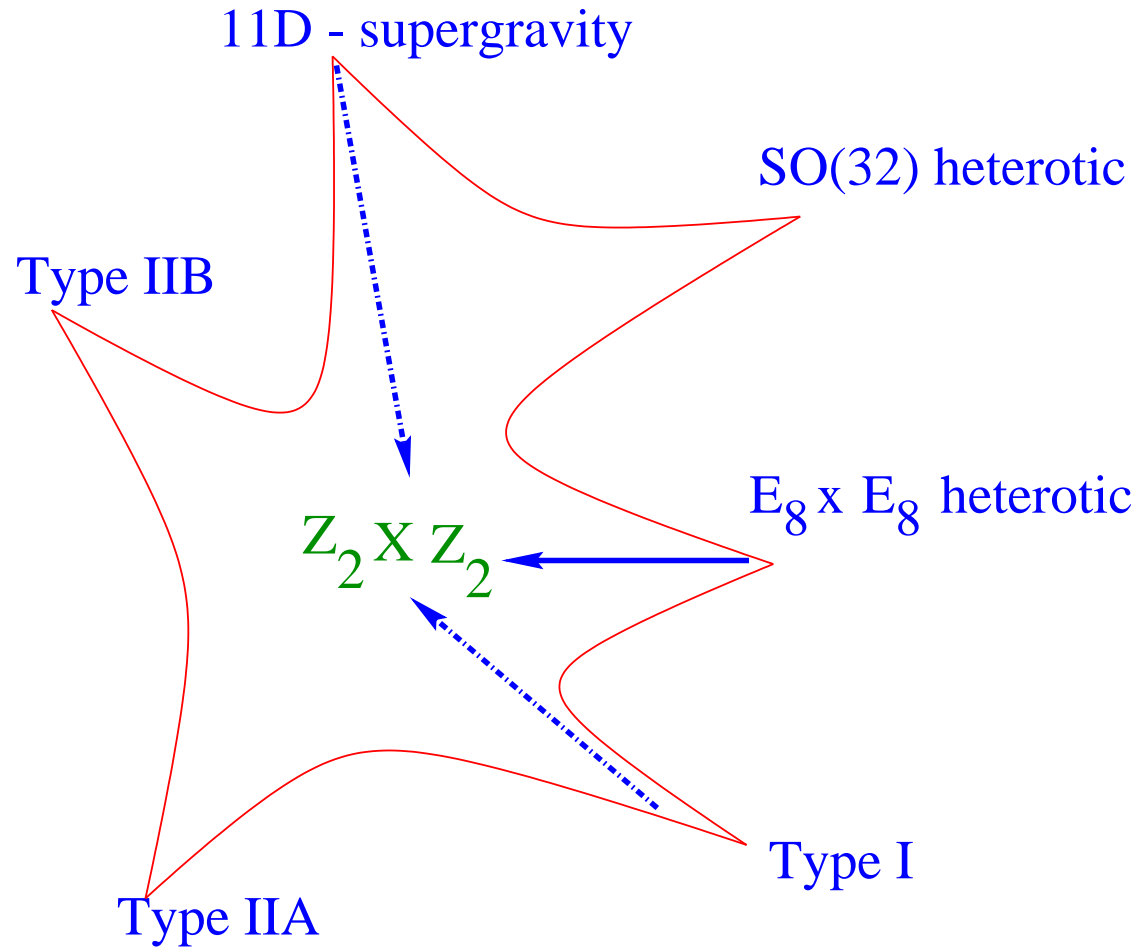
Cvetic, Shiu, Uranga (2001)

Ibanez, Marchesano, Rabadan (2001)

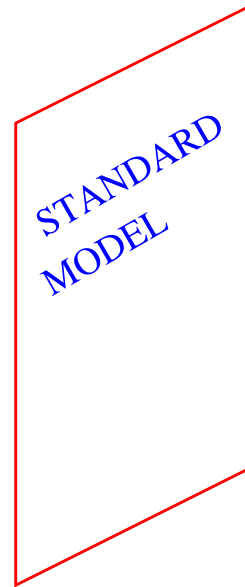
Kiristis, Schellekens, Tsulaia (2008)

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Point, String, Membrane



Sterile neutrinos in large volume scenarios



RHN
●

$$\nu_R^{(c)}(x, y) = \sum_n \frac{1}{\sqrt{2\pi r}} \nu_{Rn}^{(c)}(x) e^{iny/r}$$

$$S^{\text{int}} = \int d^4x \lambda l(x) h^*(x) \nu_R(x, y=0)$$

$$\lambda_{(4)} = \frac{\lambda}{\sqrt{r^n M_*^n}},$$

plus tower of KK modes \longrightarrow sterile neutrinos

String GUT models in the Free Fermionic Construction:

Left-Movers: $\psi_{1,2}^\mu$, χ_i , y_i , ω_i ($i = 1, \dots, 6$)

Right-Movers

$$\bar{\phi}_{A=1, \dots, 44} = \left\{ \begin{array}{ll} \bar{y}_i, \bar{\omega}_i & i = 1, \dots, 6 \\ \bar{\eta}_i & U(1)_i \quad i = 1, 2, 3 \\ \bar{\psi}_{1, \dots, 5} & SO(10) \\ \bar{\phi}_{1, \dots, 8} & SO(16) \end{array} \right.$$

Models \longleftrightarrow Basis vectors + one-loop phases

Free Fermionic Models:

$Z_2 \times Z_2$ orbifolds
with discrete Wilson lines

Sterile neutrinos in free Fermionic models

Analyse mass terms contributing to the neutrino mass matrix

AEF & Edi Halyo, PLB 307 (1993) 311

AEF & Claudio Coriano, PLB 581 (2004) 99

The generic form:

$$\begin{pmatrix} \nu_i & N_i & \phi_i \end{pmatrix} \begin{pmatrix} 0 & (M_D)_{ij} & 0 \\ (M_D)_{ij} & 0 & \langle \bar{\mathcal{N}} \rangle_{ij} \\ 0 & \langle \bar{\mathcal{N}} \rangle_{ij} & \langle \phi \rangle_{ij} \end{pmatrix} \begin{pmatrix} \nu_j \\ N_j \\ \phi_j \end{pmatrix},$$

$$m_{\nu_j} \sim \left(\frac{k M_u^j}{\langle \bar{\mathcal{N}} \rangle} \right)^2 \langle \phi \rangle, \quad m_{N_j}, m_\phi \sim \langle \bar{\mathcal{N}} \rangle.$$
$$\langle \bar{\mathcal{N}} \rangle > 10^{14} \text{GeV}$$

No Light sterile neutrino

Specific example:

	L_3	L_2	L_1	N_3	N_2	N_1	H_{23}	H_{25}	Φ_{13}	Φ_{45}	Φ_2^+	$\bar{\Phi}_2^+$
L_3	0	0	0	0	0	r	0	0	0	0	0	0
L_2	0	0	0	r	0	r	0	0	0	0	0	0
L_1	0	0	0	r	0	v	0	0	0	0	0	0
N_3	0	r	r	0	0	0	0	x	0	0	0	0
N_2	0	0	0	0	0	0	z	0	u	u	z	u
N_1	r	r	v	0	0	0	0	w	0	0	0	0
H_{23}	0	0	0	0	z	0	p	0	x	x	x	x
H_{25}	0	0	0	x	0	w	0	0	0	0	0	0
Φ_{13}	0	0	0	0	u	0	x	0	q	y	0	y
Φ_{45}	0	0	0	0	z	0	p	0	x	x	x	x
Φ_2^+	0	0	0	0	z	0	x	0	0	q	0	x
$\bar{\Phi}_2^+$	0	0	0	0	0	0	x	0	y	q	x	q

mass eigenvalues $\{1.7 \times 10^{13}, \dots, 2.4^{-8}\} \text{GeV}$

No Light sterile neutrinos \rightarrow non-chiral matter \rightarrow heavy

Sterile neutrinos \rightarrow Chiral under and extra $U(1)$ symmetry

Low scale Z' in free fermionic models:

- $\frac{3}{2}U(1)_{B-L} - 2U(1)_R \in SO(10) @ 1TeV$ MPL A6 (1991) 61
(with Nanopoulos)
- But $m_t = m_{\nu_\tau}$ & $1TeV Z' \Rightarrow m_{\nu_\tau} \approx 10MeV$ PLB 245 (1990) 435
- $E_6 \rightarrow SO(10) \times U(1)_A$ $\Rightarrow U(1)_A$ is anomalous!
 $\Rightarrow U(1)_A \notin \text{low scale } U(1)_{Z'}$
- 1996-2013, Pati, AEF, Guzzi, Mehta, Athanasopoulos, $U(1) \notin E_6$
- On the other hand(AEF, Viraf Mehta, PRD88 (2013) 025006)
 $\sin^2 \theta_W(M_Z), \alpha_s(M_Z) \Rightarrow U(1)_{Z'} \in E_6$
- Z' string derived model, (with Rizos) NPB 895 (2015) 233

Basis vectors:

$$1 = \{\psi^\mu, \chi^{1,\dots,6}, y^{1,\dots,6}, \omega^{1,\dots,6} \mid \bar{y}^{1,\dots,6}, \bar{\omega}^{1,\dots,6}, \bar{\eta}^{1,2,3}, \bar{\psi}^{1,\dots,5}, \bar{\phi}^{1,\dots,8}\}$$

$$S = \{\psi^\mu, \chi^{1,\dots,6}\},$$

$$z_1 = \{\bar{\phi}^{1,\dots,4}\},$$

$$z_2 = \{\bar{\phi}^{5,\dots,8}\},$$

$$e_i = \{y^i, \omega^i \mid \bar{y}^i, \bar{\omega}^i\}, \quad i = 1, \dots, 6,$$

$N = 4$ Vacua

$$b_1 = \{\chi^{34}, \chi^{56}, y^{34}, y^{56} \mid \bar{y}^{34}, \bar{y}^{56}, \bar{\eta}^1, \bar{\psi}^{1,\dots,5}\},$$

$N = 4 \rightarrow N = 2$

$$b_2 = \{\chi^{12}, \chi^{56}, y^{12}, y^{56} \mid \bar{y}^{12}, \bar{y}^{56}, \bar{\eta}^2, \bar{\psi}^{1,\dots,5}\},$$

$N = 2 \rightarrow N = 1$

$$\alpha = \{\bar{\psi}^{4,5}, \bar{\phi}^{1,2}\} \quad \& \quad SO(10) \rightarrow SO(6) \times SO(4) \times \dots$$

$$\beta = \{\bar{\psi}^{1,\dots,5} \equiv \frac{1}{2}, \dots\} \quad \& \quad SO(10) \rightarrow SU(5) \times U(1) \times \dots$$

Independent phases $c_{[v_i|v_j]}^{[v_i]} = \exp[i\pi(v_i|v_j)]:$ **upper block**

$$\begin{array}{c}
 1 \\
 S \\
 e_1 \\
 e_2 \\
 e_3 \\
 e_4 \\
 e_5 \\
 e_6 \\
 z_1 \\
 z_2 \\
 b_1 \\
 b_2 \\
 \alpha
 \end{array}
 \left(
 \begin{array}{cccccccccccccc}
 1 & S & e_1 & e_2 & e_3 & e_4 & e_5 & e_6 & z_1 & z_2 & b_1 & b_2 & \alpha \\
 -1 & -1 & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm \\
 & & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & 1 & 1 & -1 \\
 & & & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm \\
 & & & & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm & \pm \\
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 & & & & & & & & & & \pm & \pm & \pm \\
 & & & & & & & & & & & \pm & \pm \\
 & & & & & & & & & & & -1 & \pm \\
 & & & & & & & & & & & & \pm
 \end{array}
 \right)$$

A priori 66 independent coefficients $\rightarrow 2^{66}$ distinct vacua

The twisted matter spectrum:

$$B_{l_3^1 l_4^1 l_5^1 l_6^1}^1 = S + b_1 + l_3^1 e_3 + l_4^1 e_4 + l_5^1 e_5 + l_6^1 e_6$$

$$B_{l_1^2 l_2^2 l_5^2 l_6^2}^2 = S + b_2 + l_1^2 e_1 + l_2^2 e_2 + l_5^2 e_5 + l_6^2 e_6$$

$$B_{l_1^3 l_2^3 l_3^3 l_4^3}^3 = S + b_3 + l_1^3 e_1 + l_2^3 e_2 + l_3^3 e_3 + l_4^3 e_4 \quad l_i^j = 0, 1$$

sectors $B_{pqrs}^i \rightarrow 16$ or $\overline{16}$ of $SO(10)$ with multiplicity $(1, 0, -1)$

$B_{pqrs}^i + x \rightarrow 10$ of $SO(10)$ with multiplicity $(1, 0)$

$x = \{\bar{\psi}^{1, \dots, 5}, \bar{\eta}^1, \bar{\eta}^2, \bar{\eta}^3\}$ x -map \leftrightarrow spinor-vector map

Algebraic formulas for $S = \sum_{i=1}^3 S_+^{(i)} - S_-^{(i)}$ and $V = \sum_{i=1}^3 V^{(i)}$

Spinor–vector duality:

Duality under exchange of spinors and vectors.

First Plane			Second plane			Third Plane			# of models
s	\bar{s}	v	s	\bar{s}	v	s	\bar{s}	v	
2	0	0	0	0	0	0	0	0	1325963712
0	2	0	0	0	0	0	0	0	1340075584
1	1	0	0	0	0	0	0	0	3718991872
0	0	2	0	0	0	0	0	0	6385031168

of models with $\#(16 + \overline{16}) = \#$ of models with $\#(10)$

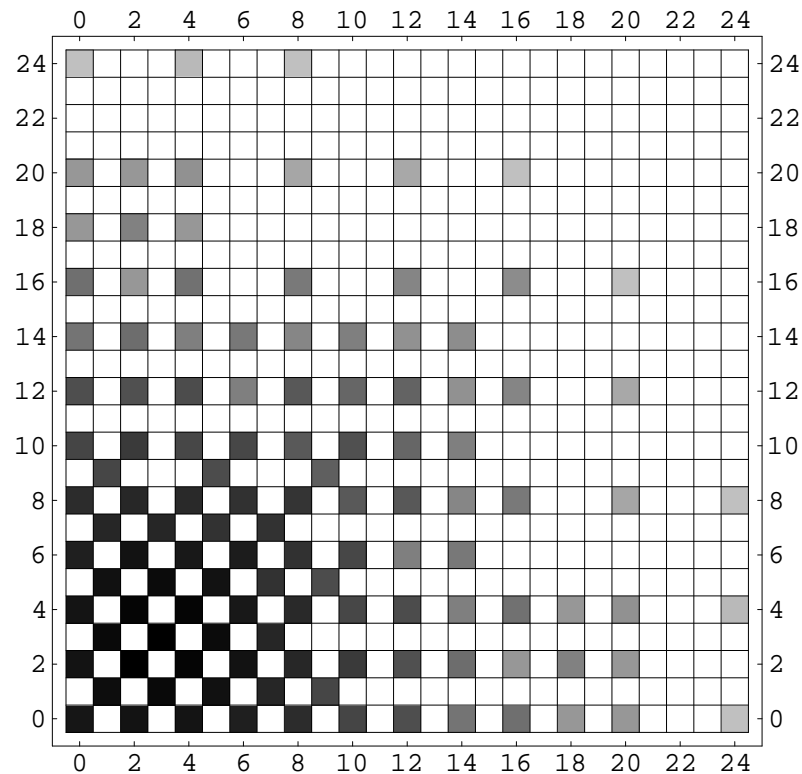
For every model with $\#(16 + \overline{16})$ & $\#(10)$

There exist another model in which they are interchanged

Reflects discrete exchange of phases

Spinor–vector duality:

Invariance under exchange of $\#(16 + \overline{16}) < - > \#(10)$



Symmetric under exchange of rows and columns

$$E_6 : \quad 27 = 16 + 10 + 1 \quad \overline{27} = \overline{16} + 10 + 1$$

Self-dual: $\#(16 + \overline{16}) = \#(10)$ without E_6 symmetry

light Z' heterotic-string model $c \begin{bmatrix} v_i \\ v_j \end{bmatrix} = \exp[i\pi(v_i|v_j)]:$

$$(v_i|v_j) = \begin{matrix} & 1 & S & e_1 & e_2 & e_3 & e_4 & e_5 & e_6 & b_1 & b_2 & z_1 & z_2 & \alpha \\ \begin{matrix} 1 \\ S \\ e_1 \\ e_2 \\ e_3 \\ e_4 \\ e_5 \\ e_6 \\ b_1 \\ b_2 \\ z_1 \\ z_2 \\ \alpha \end{matrix} & \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 \end{pmatrix} \end{matrix}$$

Observable gauge group: $SO(6) \times SO(4) \times U(1)_{1,2,3}$

$U(1)_\zeta = U(1)_1 + U(1)_2 + U(1)_3$ is anomaly free

sector	field	$SU(4) \times SU(2)_L \times SU(2)_R$	$U(1)_1$	$U(1)_2$	$U(1)_3$	$U(1)_\zeta$
$S + b_1$	\bar{F}_{1R}	$(\bar{4}, \mathbf{1}, \mathbf{2})$	1/2	0	0	1/2
$S + b_1 + e_3 + e_5$	F_{1R}	$(4, \mathbf{1}, \mathbf{2})$	1/2	0	0	1/2
$S + b_2$	F_{1L}	$(4, \mathbf{2}, \mathbf{1})$	0	1/2	0	1/2
$S + b_2 + e_1 + e_2 + e_5$	F_{2L}	$(4, \mathbf{2}, \mathbf{1})$	0	1/2	0	1/2
$S + b_2 + e_1$	\bar{F}_{2R}	$(\bar{4}, \mathbf{1}, \mathbf{2})$	0	1/2	0	1/2
$S + b_2 + e_2 + e_5$	\bar{F}_{3R}	$(\bar{4}, \mathbf{1}, \mathbf{2})$	0	1/2	0	1/2
$S + b_3 + e_1 + e_2$	F_{3L}	$(4, \mathbf{2}, \mathbf{1})$	0	0	1/2	1/2
$S + b_3 + e_2$	\bar{F}_{4R}	$(\bar{4}, \mathbf{1}, \mathbf{2})$	0	0	1/2	1/2
$S + b_3 + x$	h_1	$(\mathbf{1}, \mathbf{2}, \mathbf{2})$	-1/2	-1/2	0	-1
$S + b_2 + x + e_5$	h_2	$(\mathbf{1}, \mathbf{2}, \mathbf{2})$	-1/2	0	-1/2	-1
$S + b_2 + x + e_1 + e_2$	h_3	$(\mathbf{1}, \mathbf{2}, \mathbf{2})$	-1/2	0	-1/2	-1
$S + b_3 + x + e_1$	D_4	$(\mathbf{6}, \mathbf{1}, \mathbf{1})$	-1/2	-1/2	0	-1
	χ_1^+	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	1/2	1	+2
	χ_1^-	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	1/2	-1	0
	$\zeta_a, a = 2, 3$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	-1/2	0	0
	$\bar{\zeta}_a, a = 2, 3$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1/2	1/2	0	0
$S + b_2 + x + e_1 + e_5$	D_5	$(\mathbf{6}, \mathbf{1}, \mathbf{1})$	-1/2	0	-1/2	-1
	χ_2^+	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	1	1/2	+2
	χ_2^-	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	-1	1/2	0
	$\zeta_a, a = 4, 5$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	0	-1/2	0
	$\bar{\zeta}_a, a = 4, 5$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1/2	0	1/2	0
$S + b_2 + x + e_2$	D_6	$(\mathbf{6}, \mathbf{1}, \mathbf{1})$	-1/2	0	-1/2	-1
	χ_3^+	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	1	1/2	+2
	χ_3^-	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	-1	1/2	0
	$\zeta_a, a = 6, 7$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	0	-1/2	0
	$\bar{\zeta}_a, a = 6, 7$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1/2	0	1/2	0
$S + b_1 + x + e_3$	\bar{D}_6	$(\mathbf{6}, \mathbf{1}, \mathbf{1})$	0	1/2	1/2	+1
	$\bar{\chi}_4^+$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1	-1/2	-1/2	-2
	$\bar{\chi}_4^-$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1	-1/2	-1/2	0
	$\zeta_a, a = 8, 9$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	1/2	-1/2	0
	$\bar{\zeta}_a, a = 8, 9$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	-1/2	1/2	0
$S + b_1 + x + e_5$	D_7	$(\mathbf{6}, \mathbf{1}, \mathbf{1})$	0	-1/2	-1/2	-1
	χ_5^+	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1	1/2	1/2	+2
	χ_5^-	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1	1/2	1/2	0
	$\zeta_a, a = 10, 11$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	1/2	-1/2	0
	$\bar{\zeta}_a, a = 10, 11$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	-1/2	1/2	0
$S + b_3 + x + e_2 + e_3$	ζ_1	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	1/2	-1/2	0	0
	$\bar{\zeta}_1$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	-1/2	1/2	0	0
$S + b_1 + x + e_3 + e_4 + e_6$	ϕ_1	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	1/2	1/2	+1
	$\bar{\phi}_1$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	-1/2	-1/2	-1
$S + b_1 + x + e_4 + e_5 + e_6$	ϕ_2	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	1/2	1/2	+1
	$\bar{\phi}_2$	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	0	-1/2	-1/2	-1

Table 1: Observable twisted matter spectrum and $SU(4) \times SU(2)_L \times SU(2)_R \times U(1)^3$ quantum numbers.

The chiral spectrum is self-dual under spinor-vector duality

maintains the E_6 embedding $\Rightarrow U(1)_\zeta$ is anomaly free

Exophobic, three generations + heavy and light higgs + $\lambda_t \sim 1$

$$U(1)_{Z'} = \frac{1}{5} U(1)_C - \frac{1}{5} U(1)_L - U_\zeta$$

$Z' \Rightarrow$ Additional matter at the Z' breaking scale

Exotic $SO(10)$ singlets with non-standard $U(1)_\zeta$ charges

\Rightarrow Natural Wilsonian dark-matter candidates

Z' model at low scales

Heavy Higgs $\langle \mathcal{N} \rangle \sim M_{\text{String}} \rightarrow$ high seesaw \rightarrow

Field	$SU(3)_C$	$\times SU(2)_L$	$U(1)_Y$	$U(1)_{Z'}$
Q_L^i	3	2	$+\frac{1}{6}$	$-\frac{2}{5}$
u_L^i	$\bar{3}$	1	$-\frac{2}{3}$	$-\frac{2}{5}$
d_L^i	$\bar{3}$	1	$+\frac{1}{3}$	$-\frac{4}{5}$
e_L^i	1	1	+1	$-\frac{2}{5}$
L_L^i	1	2	$-\frac{1}{2}$	$-\frac{4}{5}$
D^i	3	1	$-\frac{1}{3}$	$+\frac{4}{5}$
\bar{D}^i	$\bar{3}$	1	$+\frac{1}{3}$	$+\frac{6}{5}$
H^i	1	2	$-\frac{1}{2}$	$+\frac{6}{5}$
\bar{H}^i	1	2	$+\frac{1}{2}$	$+\frac{4}{5}$
S^i	1	1	0	-2
h	1	2	$-\frac{1}{2}$	$-\frac{4}{5}$
\bar{h}	1	2	$+\frac{1}{2}$	$+\frac{4}{5}$
ϕ	1	1	0	-1
$\bar{\phi}$	1	1	0	+1
ζ^i	1	1	0	0

Additional matter states at $U(1)_{Z'}$ breaking scale

Neutrino mass spectrum

a plausible scenario

$$\begin{matrix} L_i \\ S_i \\ H_i \\ \bar{H}_i \\ N_i \end{matrix} \begin{pmatrix} L_i & S_i & H_i & \bar{H}_i & N_i \\ 0 & 0 & 0 & \lambda n & \lambda v \\ 0 & 0 & \lambda v_2 & \lambda v_3 & 0 \\ 0 & \lambda v_2 & 0 & z' & 0 \\ \lambda n & \lambda v_3 & z' & 0 & 0 \\ \lambda v & 0 & 0 & 0 & \mathcal{N}^2/M \end{pmatrix},$$

$$\begin{aligned} \lambda v &= 1\text{GeV}; & \lambda n &= 5 \times 10^{-4}\text{GeV}; \approx m_e; \\ \lambda v_2 &= 5 \times 10^{-4}\text{GeV} \approx m_e; & \lambda v_3 &= 5 \times 10^{-4}\text{GeV}; \approx m_e; \\ z' &= 5 \times 10^4\text{GeV} = 50\text{TeV}; & \bar{\mathcal{N}} &= 5 \times 10^{14}\text{GeV}, \end{aligned}$$

$$m_{1,2} = \{10^{-2}\text{eV}, 10^{-3}\text{eV}\} \quad \text{mix of } \nu_L^i \text{ and } S_i, \text{ with } \sin \theta \approx 0.98.$$

$$m_{3,4,5} = \{50\text{TeV}, 50\text{TeV}, 2.5 \times 10^{11}\text{GeV}\}.$$

$$m_5 \leftrightarrow N_i \quad m_{3,4} \leftrightarrow \text{equal mix of } H_i \text{ and } \bar{H}_i$$

Spinor–Vector Duality from a Novel Basis

$$S = \{\psi^\mu, \chi^{1,\dots,6}\},$$

$$z_1 = \{\bar{\phi}^{1,\dots,4}\},$$

$$z_2 = \{\bar{\phi}^{5,\dots,8}\},$$

$$z_3 = \{\bar{\psi}^{1,\dots,4}\},$$

$$z_4 = \{\bar{\eta}^{0,\dots,3}\},$$

$$e_i = \{y^i, \omega^i | \bar{y}^i, \bar{\omega}^i\}, \quad i = 1, \dots, 6,$$

$$\bar{\eta}^0 \equiv \bar{\psi}^5$$

$N = 4$ Vacua

$$1 = S + \sum e_i + z_1 + z_2 + z_3 + z_4$$

$$b_1 = \{\chi^{34}, \chi^{56}, y^{34}, y^{56} | \bar{y}^{34}, \bar{y}^{56}, \bar{\eta}^1, \bar{\psi}^{1,\dots,5}\},$$

$$N = 4 \rightarrow N = 2$$

Vector bosons: NS, $z_{1,2,3,4}$, $z_i + z_j$

$$\text{NS} \rightarrow SO(8)^4$$

$SO(12)$ –GUT \rightarrow from enhancement

Duality picture is facilitated

Spinor \longleftrightarrow Vector map $\longrightarrow B \longleftrightarrow B + z_4$

$SO(12)$ enhancement $\longrightarrow B \longleftrightarrow B + z_3$

A convenient basis to study dualities; modular properties

$\rightarrow 2D \rightarrow 24$ dimensional lattices

GUT structure is obscured

Conclusions

- DATA \longrightarrow UNIFICATION
- STRINGS \longrightarrow GAUGE & GRAVITY UNIFICATION
- Free fermionic models \longrightarrow A Fertile Crescent \longleftrightarrow $Z_2 \times Z_2$ orbifolds
- Sterile neutrinos \longrightarrow chiral matter charged under low scale extra $U(1)$
- Low scale Z' \longrightarrow hard to implement in string GUT constructions
- Spinor–vector duality (alternatively: extended GUT embeddings)
- String Phenomenology \longrightarrow Physics of the third millenium
e.g. Aristarchus to Copernicus